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# One-Round Attribute-Based Key Exchange in the Multi-party Setting

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**Abstract.** Attribute-based authenticated key exchange (AB-AKE) is a useful primitive that allows a group of users to establish a shared secret key and at the same time enables fine-grained access control. A straightforward approach to design an AB-AKE protocol is to extend a key exchange protocol using attribute-based authentication technique. However, insider security is a challenge security issue for AB-AKE in the multi-party setting and cannot be solved using the straightforward approach. In addition, many existing key exchange protocols for the multi-party setting (e.g., the well-known Burmester-Desmedt protocol) require multiple broadcast rounds to complete the protocol. In this paper, we propose a novel one-round attribute-based key exchange (OAKE) protocol in the multi-party setting. We define the formal security models, including session key security and insider security, for OAKE, and prove the security of the proposed protocol under some standard assumptions in the random oracle model.

**Keywords:** Attribute-based cryptography · One-round key exchange · Multi-party setting · Insider security

## 1 Introduction

Authenticated key exchange (AKE) protocols are a central building block in many network security standards such as IPsec, TLS/SSL, SSH, and so on. AKE aims to share a common secret key among multiple users over an insecure communication channel, such that the users can authenticate each other by using the respective identities or public keys. AKE has been further explored in the attribute-based context recently [16, 26]. Attribute-based AKE (AB-AKE), as a new general form of AKE, enables fine-grained access control between authenticated users. The AB-AKE mechanism is significantly useful in many

real-world applications, such as distributed collaborative systems [16]. In practice, sometimes it is necessary for users to communicate with each other based on their role/responsibility. For instance, an individual user should be allowed to establish a secure communication with another user if and only if the former's role/responsibility can satisfy the latter's expectation.

The anonymity property naturally exists in attribute-based systems since people with different attribute sets may all satisfy an access policy. This brings a security issue for AB-AKE in the multi-party setting where it might be possible that a malicious authorized member can successfully impersonate other authorized members (i.e., insider attacks). Specifically, a malicious user Alice (attacker) attempts to impersonate an honest user Bob to establish a conversion with another user, say Charlie, but the impersonated user Bob was not actually involved in the particular conversion with Charlie. Such an attack is possible due to the inherent anonymous property of attribute-based systems. Therefore, achieving insider security is a non-trivial task for AB-AKE under the multi-party setting. Although there are some existing works on AB-AKE [16, 26], they didn't consider the issue of insider attacks in the multi-party setting.

In order to achieve the insider security for AB-AKE in the multi-party setting, in this paper, we propose a novel hybrid signcryption (HSC) scheme to address the issue, where the hybrid signcryption scheme is built on top of a combination of key-policy attribute-based encryption (KP-ABE) [17] and identity-based signature (IBS) [14, 19]. In addition to insider security and fine-grained authentication for key exchange, it is also desirable to share a secret key with less communication rounds. Many existing multi-party (or group) AKE protocols, such as the well-known Burmester-Desmedt protocol [12], require multiple broadcast rounds in order to complete the protocol. In this paper we tackle this problem by making use of the (generic) multilinear maps [10] to establish a session key with only one broadcast round for a group of users.

### 1.1 This Work

In this paper, we introduce the notion of one-round attribute-based broadcast key exchange in the multi-party setting, allowing all users to agree on a common session key in only one broadcast round. Our contributions are as follows:

1. We present the formal security definitions for OAKE. In particular, we extend the model of [26] to define session key security and propose a new insider security model to capture malicious insider attacks.
2. We introduce a new primitive named hybrid signcryption (HSC), and propose a concrete scheme that is built on top of an identity-based signature scheme and Goyal et al.'s [17] key-policy attribute-based encryption scheme. We also prove that the proposed HSC scheme can achieve existential unforgeability in the random oracle model.
3. We present a one-round AB-AKE protocol in the multi-party setting based on our proposed HSC scheme and the generic multilinear maps [10]. We further prove that the proposed protocol can achieve both session key security and insider security.

## 1.2 Related Work

*Key Exchange.* Burmester and Desmedt [12] introduced several key exchange protocols in the multi-party setting, including star-based, tree-based, broadcast-based and cyclic-based protocols. Later, a few generic transformations [8, 20, 21] were proposed to convert passive-secure group key exchange protocols into active-secure ones. Bellare and Rogaway [5] introduced the first complexity-theoretic security model for key exchange under the symmetric-key setting. The model was later extended and enhanced under different contexts [3, 4, 6]. Canetti and Krawczyk [13] later refined the previous models and proposed a new model, known as the CK model, which is widely used in the analysis of many well-known key exchange protocols. Some variants [22, 23] of CK model were also proposed to allow an adversary to obtain either long term secret key or ephemeral secret key of the challenge session. In [26] an extension of the eCK (extended CK) model proposed in [23] was introduced for the attribute-based setting. It strengthens the session key security model by allowing adversary to gain access to the master secret key.

*Signcryption.* Zheng [27] introduced the concept of signcryption that provides an efficient way of achieving both message confidentiality and authenticity. The security of the scheme was later proven in [2]. An et al. [1] formally analyzed three generic constructions of signcryption in the public key setting, namely “encrypt then sign” (*EtS*), “sign then encrypt” (*StE*), and “commit then encrypt and sign” (*CtE&S*). Meanwhile, Haber and Pinkas [18] proposed a combined public key scheme under the joint security model, where encryption schemes and signature schemes shared the common public parameters and secret key. Boyen [11] introduced an efficient identity-based signcryption (IBSC) scheme based on the Boneh–Franklin IBE [9] scheme and the Cha–Cheon IBS [14] scheme.

*Attribute-based Cryptography.* For achieving fine-grained access control over the encrypted data, Sahai and Waters [25] proposed the fuzzy identity-based encryption, in which users must match at least a certain threshold of attributes before data decryption. Later, two types of attribute-based encryption (ABE) systems were proposed: Key-policy ABE [17] and Ciphertext-policy ABE [7]. In KP-ABE, a ciphertext is labeled with an attribute set, while a secret key is associated with the access structure specifying which ciphertext a user is able to decrypt. The roles of attribute set and access structure are swapped in the CP-ABE context. Inspired by the attribute-based cryptography, several attribute-based signcryption schemes [15, 24] have been proposed in the literature where both signing and encryption functions are attribute-based. We should note that such kind of attribute-based signcryption schemes are not suitable for our purpose since they cannot address the insider attacks.

## 2 Security Models

In this section, we present the security models for OAKE. As mentioned in the introduction, a secure OAKE protocol in the multi-party setting should

achieve both session key security and insider security. Below we present the corresponding security models to capture the above requirements. Specifically, the session key security model is a *modified* version of Yoneyama’s model [26] which is an extension of eCK model [23] in the attribute-based setting.

**States.** We define a system user set  $\mathcal{U}$  with  $n$  users, i.e.  $|\mathcal{U}| = n$ . We say an oracle  $\Pi_U^i$  may be *used* or *unused*. The oracle is considered as unused if it has never been initialized. Each unused oracle  $\Pi_U^i$  can be initialized with a secret key  $x$ . The oracle is initialized as soon as it becomes part of a group. After the initialization the oracle is marked as *used* and turns into the *stand-by* state where it waits for an invocation to execute a protocol operation. Upon receiving such invocation the oracle  $\Pi_U^i$  learns its partner id  $\text{pid}_U^i$  and turns into a *processing* state where it sends, receives and processes messages according to the description of the protocol. During that stage, the internal state information  $\text{state}_U^i$  is maintained by the oracle. The oracle  $\Pi_U^i$  remains in the *processing* state until it collects enough information to compute the session key  $k_U^i$ . As soon as  $k_U^i$  is computed  $\Pi_U^i$  *accepts* and *terminates* the protocol execution meaning that it would not send or receive further messages. If the protocol execution fails then  $\Pi_U^i$  terminates without having accepted.

**Partnering.** We denote the  $i$ -th session established by an user  $U$  by  $\Pi_U^i$ , the attribute set of the user by  $\delta_U$ , and the access structure of the user by  $\Lambda_U$ . Let the partner identifier  $\text{pid}_U^i$  includes the identities of participating users (including  $U$ ) in the  $i$ -th session established by the user  $U$  with the condition that  $\forall U_j \in \text{pid}_U^i, \Lambda_U(\delta_{U_j}) = 1$ , where  $\delta_{U_j}$  denotes the attribute set of the user  $U_j$ , and  $\Lambda_U(\delta_{U_j}) = 1$  means that the attribute set  $\delta_{U_j}$  is satisfied by the access structure  $\Lambda_U$ . In other words,  $\text{pid}_U^i$  is a collection of *recognized* participants by the instance oracle  $\Pi_U^i$ . We also define  $\text{sid}_U^i$  as the unique session identifier belonging to the session  $i$  established by the user  $U$ . Specifically,  $\text{sid}_U^i = (\text{pid}_U^i, \{m_j\}_{j=1}^n)$ , where  $m_j \in \{0, 1\}^*$  is the message transcript among users in  $\text{pid}_U^i$ . We say two instance oracles  $\Pi_U^i$  and  $\Pi_{U'}^j$  are *partners* if and only if  $\text{sid}_U^i = \text{sid}_{U'}^j$ .

## 2.1 Session Key Security

We define the session key security model for key-policy AB-AKE protocols, in which each user obtains a secret key associating with his/her access structure from the trusted authority (TA), and establishes a session key depending on the partners’ attribute sets. The model is defined via a game between a probabilistic polynomial time (PPT) adversary  $\mathcal{A}$  and a simulator  $\mathcal{S}$ .  $\mathcal{A}$  is an active attacker with full control of the communication channel among all the users.

- Setup:  $\mathcal{S}$  first generates master public/secret key pair  $(\mathcal{K}_0, x_0)$  for the TA and long term secret keys  $\{x_i\}_{i=1}^n$  for  $n$  users by running the corresponding key generation algorithms, where  $x_i$  denotes the secret key of user  $i$ , such that  $x_i$  ( $i \neq 0$ ) is corresponding to the access structure  $\Lambda_i$  and identity  $ID_i$  of user  $i$ .  $\mathcal{S}$  also tosses a random coin  $b$  which will be used later in the game.
- Training:  $\mathcal{A}$  can make the following queries in arbitrary sequence to simulator  $\mathcal{S}$ .

- **Establish:**  $\mathcal{A}$  is allowed to register a user  $U'$  with an access structure  $A'$ . If a party is registered by the  $\mathcal{A}$ , then we call the user  $i$  *dishonest*; Otherwise, it is *honest*.
- **Send:** If  $\mathcal{A}$  issues a send query in the form of  $(U, i, m)$  to simulate a network message for the  $i$ -th session of user  $U$ , then  $\mathcal{S}$  would simulate the reaction of instance oracle  $\Pi_U^i$  upon receiving message  $m$ , and returns to  $\mathcal{A}$  the response that  $\Pi_U^i$  would generate; If  $\mathcal{A}$  issues a send query in the form of  $(U, 'start', \delta_U)$ , then  $\mathcal{S}$  creates a new instance oracle  $\Pi_U^i$  and returns to  $\mathcal{A}$  the first protocol message under the attribute set  $\delta_U$ .
- **Session key reveal:**  $\mathcal{A}$  can issue session key reveal query to an accepted instance oracle  $\Pi_U^i$ . If the session is accepted, then  $\mathcal{S}$  will return the session key to  $\mathcal{A}$ ; Otherwise, a special symbol ' $\perp$ ' is returned to  $\mathcal{A}$ .
- **Ephemeral secret key reveal:** If  $\mathcal{A}$  issues an ephemeral secret key reveal query to (possibly unaccepted) instance oracle  $\Pi_U^i$ , then  $\mathcal{S}$  will return all ephemeral secret values contained in  $\Pi_U^i$  at the moment the query is asked.
- **Long term secret key reveal:** If  $\mathcal{A}$  issues a long term secret key reveal (or corrupt, for short) query to user  $i$ , then  $\mathcal{S}$  will return the long term secret key  $x_i$  to  $\mathcal{A}$ .
- **Master secret key reveal:** If  $\mathcal{A}$  issues a master secret key reveal query to TA, then  $\mathcal{S}$  will return the master secret key  $x_0$  to  $\mathcal{A}$ .
- **Test:** This query can only be made to an accepted and *fresh* (as defined below) session  $i$  of a user  $U$ . Then  $\mathcal{S}$  does the following:
  - \* If the coin  $b = 1$ ,  $\mathcal{S}$  returns the real session key to the adversary;
  - \* Otherwise, a random session key is drawn from the session key space and returned to the adversary.

It is also worth noting that  $\mathcal{A}$  can continue to issue other queries after the Test query. However, the test session must maintain *fresh* throughout the entire game.

Finally,  $\mathcal{A}$  outputs  $b'$  as its guess for  $b$ . If  $b' = b$ , then the simulator outputs 1; Otherwise, the simulator outputs 0.

**Freshness.** We say an *accepted* instance oracle  $\Pi_U^i$  is *fresh* if  $\mathcal{A}$  does not perform any of the following actions during the game:

- $\mathcal{A}$  issues *establish* query, where the new user  $U' \in \text{pid}_U^i$ ;
- $\mathcal{A}$  issues a *session key reveal* query to  $\Pi_U^i$  or its accepted partnered instance oracle  $\Pi_{U'}^j$ , (if the latter exists);
- $\mathcal{A}$  issues both *long term secret key reveal* query to  $U'$  s.t.  $U' \in \text{pid}_U^i$  and *ephemeral secret key reveal* query for an instance  $\Pi_{U'}^j$ , partnered with  $\Pi_U^i$ .
- $\mathcal{A}$  issues *long term secret key reveal* query to user  $U'$  s.t.  $U' \in \text{pid}_U^i$  prior to the acceptance of instance  $\Pi_U^i$  and there exists no instance oracle  $\Pi_{U'}^j$ , partnered with  $\Pi_U^i$ .

Note that the *master key reveal query* is equivalent to the *long term secret key reveal* to all users in  $\mathcal{U}$ .

We define the advantage of an adversary  $\mathcal{A}$  in the above game as

$$\text{Adv}_{\mathcal{A}}(k) = \Pr[\mathcal{S} \rightarrow 1] - 1/2.$$

**Definition 1.** We say an OAKE protocol has session key security if for any probabilistic polynomial-time (PPT)  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}(k)$  is a negligible function of the security parameter  $k$ .

## 2.2 Insider Security

Informally, a PPT adversary  $\mathcal{A}$  attempts to impersonate one honest user to communicate with other honest users, whereas the impersonated honest user is not actually involved in that conversion. We define the insider security game between a PPT insider adversary  $\mathcal{A}$  and a simulator  $\mathcal{S}$  as follows.

- Training:  $\mathcal{A}$  is allowed to issue establish, send, ephemeral secret key reveal, at most  $n-1$  long term secret key reveal, and session key reveal queries to the simulator. Let  $\mathcal{U}'$  denotes the set of *uncorrupted* users (the established users are excluded from  $\mathcal{U}'$ ). At the end of training stage,  $\mathcal{A}$  outputs  $(U, U', s)$ , such that  $U \in \mathcal{U}'$ , i.e.,  $U$  denotes an *impersonated* but honest user who is *not corrupted*, and  $U' \in \mathcal{U}$  can be a *corrupted* user who has a used oracle  $\Pi_{U'}^s$ . Note that  $\mathcal{A}$  is not allowed to issue the master key reveal query, otherwise all users are *corrupted*.
- Attack:  $\mathcal{A}$  wins the game if all of the following conditions hold.
  - $\Pi_{U'}^s$ , accepted, it implies  $\text{sid}_{U'}$  exist;
  - $U \in \text{pid}_{U'}^s$ , it implies  $\Lambda_{U'}(\delta_U) = 1$ ;
  - $m_U \in \text{sid}_{U'}^s$ , but there exists no  $\Pi_U^i$  which has sent  $m_U$  ( $m_U$  denotes the message transcript from the user  $U$ ).

We define the advantage of an adversary  $\mathcal{A}$  in the above game as

$$\text{Adv}_{\mathcal{A}}(k) = \Pr[\mathcal{A} \text{ wins}].$$

**Definition 2.** We say a OAKE protocol has insider security if for any probabilistic polynomial-time (PPT)  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}(k)$  is an negligible function of the security parameter  $k$ .

## 3 OAKE Protocol

In this section, we firstly review the preliminaries and the building blocks that will be used in the proposed hybrid signcryption scheme and the OAKE protocol, and then introduce our constructions.

### 3.1 Preliminaries

**(Generic) Multilinear Maps [10].** It assumes the existence of a group generator  $g$ , which takes a security parameter  $k$  and the number of levels  $\mathcal{K}$  as input, outputs a sequence of groups  $(\mathbb{G}_1, \dots, \mathbb{G}_{\mathcal{K}})$  with the corresponding canonical generators  $(g_1, \dots, g_{\mathcal{K}})$ , each of them with large prime order  $q$ . The multilinear maps  $\hat{e} : \mathbb{G}_i \times \mathbb{G}_j \rightarrow \mathbb{G}_{i+j} | i, j \geq 1; i + j \leq \mathcal{K}$  satisfies the following relation:

$$\hat{e}(g_i^{\alpha_i}, g_j^{\alpha_j}) = g_{i+j}^{\alpha_i \cdot \alpha_j} : \forall \alpha_i, \alpha_j \in_R \mathbb{Z}_q, i + j \leq \mathcal{K}$$

**Bilinear Maps.** The bilinear maps (i.e.,  $\mathcal{K} = 2$ )  $e : \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}_T$  has the following properties:

1. **Bilinearity:**  $e(g^{\alpha_i}, g^{\alpha_j}) = e(g, g)^{\alpha_i \cdot \alpha_j} : \forall \alpha_i, \alpha_j \in \mathbb{Z}_q, g \in \mathbb{G}$ .
2. **Non-degeneracy:**  $e(g, g) \neq 1$ .
3. **Computable:** There exists an efficient algorithm for computing the bilinear maps.

Note that the maps  $e$  is symmetric since  $e(g^{\alpha_i}, g^{\alpha_j}) = e(g, g)^{\alpha_i \cdot \alpha_j} = e(g^{\alpha_j}, g^{\alpha_i})$ .

**$\mathcal{K}$ -Multilinear Decisional Diffie-Hellman ( $\mathcal{K}$ -MDDH) Assumption [10]:** Given  $g_1, g_1^{c_1}, \dots, g_1^{c_{\mathcal{K}}}$  where  $c_1, \dots, c_{\mathcal{K}} \in_R \mathbb{Z}_q$ , we define the advantage of the adversary in solving the  $\mathcal{K}$ -MDDH problem as

$$\text{Adv}_{\mathcal{A}}(k) = \Pr[b \in \{0, 1\}, \mathcal{A}(g_1^{c_1}, \dots, g_1^{c_{\mathcal{K}}}, T_b = g_{\mathcal{K}-1}^{\prod_{i=1}^{\mathcal{K}} c_i}, T_{1-b} \in \mathbb{G}_{\mathcal{K}-1}) = b].$$

The  $\mathcal{K}$ -MDDH assumption holds if for any PPT  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}(k)$  is a *negligible* function of the security parameter  $k$ .

**Computational Diffie-Hellman (CDH) Assumption [22]:** Given  $g, g^a, g^b \in \mathbb{G}$  where  $a, b \in_R \mathbb{Z}_q$ , we define the advantage of the adversary in solving the CDH problem as

$$\text{Adv}_{\mathcal{A}}^{CDH}(k) = \Pr[\mathcal{A}(g, g^a, g^b) = g^{ab} \in \mathbb{G}].$$

The CDH assumption holds if for any PPT  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}(k)$  is a *negligible* function of the security parameter  $k$ .

### 3.2 Building Blocks

**Key-Policy Attribute-based Encryption Access Structure [17].** Let  $\{P_1, \dots, P_n\}$  be a set of parties. A collection  $\Lambda \subseteq 2^{\{P_1, \dots, P_n\}}$  is monotone if  $\forall B, C : \text{if } B \in \Lambda \text{ and } B \subseteq C \text{ then } C \in \Lambda$ . An access structure (i.e., monotone access structure) is a collection of non-empty subsets of  $\{P_1, \dots, P_n\}$  (i.e.,  $\Lambda \subseteq 2^{\{P_1, \dots, P_n\}} \setminus \{\emptyset\}$ ). The sets in  $\Lambda$  are called the authorized sets, and the sets not in  $\Lambda$  are called the unauthorized sets.

**Access Tree  $\Lambda$  [17].** Let  $\Lambda$  be a tree representing an access structure. Each non-leaf node of the tree represents a threshold gate, described by its children



and a threshold value. If  $num_i$  is the number of children of a node  $x$  and  $k_x$  is its threshold value, then  $1 \leq k_x \leq num_x$ . If  $k_x = 1$ , it is an OR gate; If  $k_x = num_x$ , it is an AND gate. Each leaf node  $x$  of the tree is described by an attribute and a threshold value  $k_x = 1$ .

We define the parent of the node  $x$  in the tree by  $parent(x)$ , the attribute associates with the leaf node  $x$  in the tree by  $att(x)$ , the ordering between the children of every node  $x$  in the tree by  $index(x)$  (numbered from 1 to  $num$ ).

**Satisfying An Access Tree.** Let  $A$  be an access tree with root  $R$ . The  $A_x$  denotes the subtree of  $A$  rooted at the node  $x$  (e.g.,  $A = A_R$ ). If a set of attributes  $\delta$  satisfies the access tree  $A_x$ , we denote it as  $A_x(\delta) = 1$ . We compute  $A_x(\delta)$  as follows: If  $x$  is a leaf node, then  $A_x(\delta)$  returns 1 iff  $att(x) \in \delta$ ; If  $x$  is a non-leaf node, evaluate  $A_{x'}(\delta)$  for all children  $x'$  of node  $x$ .  $A_x(\delta)$  returns 1 iff at least  $k_x$  children return 1.

**Key-Policy Attribute-Based Encryption Scheme:** It consists of four algorithms [17]: KP-ABE=(Setup, KeyGen, Encrypt, Decrypt).

- **Setup:** The algorithm takes the security parameter  $k$  as input, outputs the master public parameters  $mpk$  and the master secret key  $msk$ .
- **KeyGen:** The algorithm takes the master secret key  $msk$  and an access structure  $A$  as input, outputs a secret key  $sk$ .
- **Encrypt:** The algorithm takes the master public parameters  $mpk$ , a message  $M$  and a set of attributes  $\delta$  as input, outputs a ciphertext  $C$ . The  $C$  implicitly contains  $\delta$ .
- **Decrypt:** The algorithm takes the master public parameters  $mpk$ , a ciphertext  $C$  and the secret key  $sk$  as input, outputs the message  $M$  if and only if the attribute set  $\delta$  satisfies the access structure  $A$ .

**Identity-Based Signature.** An identity-based signature (IBS) scheme [14, 19] consists of four algorithms: IBS=(Setup, KeyGen, Sign, Verify).

- **Setup:** The algorithm takes the security parameter  $k$  as input, outputs the master public parameters  $mpk$  and the master secret key  $msk$ .
- **KeyGen:** The algorithm takes the master secret key  $msk$  and an identity  $ID$  as input, outputs a secret signing key  $sk$ .
- **Sign:** The algorithm takes a message  $M$  and the signing key  $sk$  as input, outputs a signature  $\sigma$  on the message  $M$ .
- **Verify:** The algorithm takes the signature  $\sigma$ , the message  $M$  and the identity  $ID$  as input, outputs 1 if  $\sigma$  is valid on  $M$ , otherwise reject.

**Hybrid Signcryption.** A hybrid signcryption (HSC) scheme consists of four algorithms: HSC=(Setup, KeyGen, Sigcrypt, Unsigcrypt).

- **Setup:** The algorithm takes the security parameter  $k$  as input, and outputs the master key pair  $(mpk, msk)$ .

- **KeyGen**: The algorithm takes an identity  $ID$ , an access structure  $\Lambda$  and the master secret key  $msk$  as input, and outputs the decryption/signing key pair  $(dk, sk)$ , where  $dk$  is corresponding to  $\Lambda$  and  $sk$  is corresponding to  $ID$ .
- **Signcrypt**: The randomized algorithm takes the master public key  $mpk$ , a message  $M$ , a sender’s identity  $ID$ , the signing key  $sk$  and an attribute set  $\delta$  as input, and outputs a signcryption  $CT$ .
- **Unsigncrypt**: The deterministic algorithm takes the master public key  $mpk$ , a signcryption  $CT$ , the decryption key  $dk$  as input, and outputs the message  $M$  and sender’s identity  $ID$  if  $CT$  is valid, otherwise it outputs reject.

We define an unforgeability game between an insider adversary  $\mathcal{A}$  and a simulator  $\mathcal{S}$  in the multiple party setting, which proceeds as follows:

- **Setup**:  $\mathcal{S}$  runs  $(mpk, msk) \leftarrow \text{Setup}(1^k)$ , where  $k$  is the security parameter, returns  $mpk$  to  $\mathcal{A}$ .
- **Training**:  $\mathcal{A}$  is allowed to issue **Signcrypt**, **Unsigncrypt** and **KeyGen** queries. Note that  $\mathcal{S}$  will return the secret key pair  $(dk, sk)$  to  $\mathcal{A}$  when issuing the **KeyGen** query.
- **Forgery**:  $\mathcal{A}$  outputs a signcryption  $CT^*$  and an access structure  $\Lambda^*$ .
- **Outcome**:  $\mathcal{A}$  wins if all of the following conditions hold.
  - $\text{Unsigncrypt}(mpk, CT^*, dk^*) = (M^*, ID^*)$  where  $dk^*$  denotes the decryption key corresponding to  $\Lambda^*$ ;
  - no **KeyGen** query was made on  $ID^*$ ;
  - no **Signcrypt** query was made on  $M^*$  and  $ID^*$ .

We define the advantage of the adversary as

$$\text{Adv}_{\mathcal{A}}(k) = \Pr[\mathcal{A} \text{ wins}].$$

**Definition 3.** We say that the HSC scheme is existentially unforgeable under chosen message attacks (EUF-CMA) if for any PPT  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}(k)$  is a negligible function of the security parameter  $k$ .

### 3.3 A Novel Hybrid Signcryption Scheme

We construct a hybrid signcryption scheme based on the KP-ABE scheme proposed in [17]. We define the Lagrange coefficient  $\Delta_{i,N}$  for  $i \in \mathbb{Z}_q$  and a set,  $N$ , of elements in  $\mathbb{Z}_q$ :  $\Delta_{i,N}(x) = \prod_{j \in N, j \neq i} \frac{x - j}{i - j}$ . The data will be signcrypted under a set  $\delta$  of  $n$  elements of  $\mathbb{Z}_q$ . The proposed hybrid signcryption scheme works as follows:

- **Setup**: It takes the security parameter  $k$  as input, outputs the master public key  $mpk = (g, T_1 = g^{t_1}, \dots, T_{n+1} = g^{t_{n+1}}, g^\alpha, g^\beta, e(g, h)^\alpha, h \in_R \mathbb{G})$  and the master secret key  $msk = (t_1, \dots, t_{n+1}, \alpha, \beta \in_R \mathbb{Z}_q)$ . It also generates hash functions  $H_1 : \{0, 1\}^* \rightarrow \mathbb{G}, H_2 : \mathbb{G}_1 \rightarrow \mathbb{G}$  and chooses a pseudo-random generator  $G$ . We let  $N$  be the set  $\{1, 2, \dots, n + 1\}$  and denote the bilinear pairing  $e : \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}_T$ . We define a function  $T$  as  $T(X) = h^{X^n} \cdot \prod_{i=1}^{n+1} T_i^{\Delta_{i,N}(X)}$ .

– **KeyGen**: It takes the identity  $ID \in \{0, 1\}^*$ , the access tree  $\Lambda$  as input, outputs the signing key  $sk = H_1(ID)^\beta$  and the decryption key  $dk$ .

1. It chooses a polynomial  $q_x$  for each node  $x$  (including the leaf nodes) in the tree  $\Lambda$ . These polynomials are chosen in the following way in a top-down manner, starting from the root node  $R$ . For each node  $x$  in the tree, set the degree  $d_x$  of the polynomial  $q_x$  to be one less than the threshold value  $k_x$  of that node (i.e.,  $d_x = k_x - 1$ ). Starting with the root node  $R$ , the algorithm will set  $q_R(0) = \alpha$ . Then it chooses  $d_R$  other points of the polynomial  $q_R$  randomly to define it completely. For other nodes  $x$ , it sets  $q_x(0) = q_{parent(x)}(index(x))$  and chooses  $d_x$  other points randomly to completely define  $q_x$ . We define  $L$  as the set of leaf nodes in  $\Lambda$ , and proceed as follows:

2.  $\forall l \in L : D_l = h^{q_x(0)} \cdot T(i)^{r_l}, R_l = g^{r_l}$ , where  $i = att(l)$  and  $r_l \in_R \mathbb{Z}_q$  is corresponding to leaf node  $l$  in  $\Lambda$ . Set  $dk = \{D_l, R_l\}_{l \in L}$ .

– **Signcrypt**: It takes a message  $m \in \mathbb{G}_1$  and a set of attributes  $\delta$  as input, then

1. Computes  $\widehat{C} = (m || ID) \oplus G(e(g, h)^{\alpha \cdot s}), C = g^s, \{C_i = T(i)^s\}_{i \in \delta}$ , where  $s \in_R \mathbb{Z}_q$ ;
2. Computes  $S = sk \cdot H_2(m)^s$ ;
3. Outputs the signcryption:  $CT = \{\delta, \widehat{C}, C, \{C_i\}_{i \in \delta}, S\}$ .

– **Unsigncrypt**:

1. We define a recursive algorithm **DecryptNode**( $CT, dk, x$ ), such that  $dk$  is associated with an access tree  $\Lambda$  and a node  $x$  from  $\Lambda$ .
  - If  $x$  is a leaf node, we let  $i = att(x)$ .
    - \* If  $i \in \delta$ , compute

$$\begin{aligned}
 \text{DecryptNode}(CT, dk, x) &= \frac{e(D_x, C)}{e(R_x, C_i)} \\
 &= \frac{e(h^{q_x(0)} \cdot T(i)^{r_x}, g^s)}{e(g^{r_x}, T(i)^s)} \\
 &= \frac{e(h^{q_x(0)}, g^s) \cdot e(T(i)^{r_x}, g^s)}{e(g^{r_x}, T(i)^s)} \\
 &= e(g, h)^{s \cdot q_x(0)};
 \end{aligned}$$

\* If  $i \notin \delta$ , abort.

- If  $x$  is a non-leaf node, for all nodes  $z$ , which are children of  $x$ , call **DecryptNode**( $CT, dk, z$ ) and store the output as  $C_z$ . Let  $S_x$  be an arbitrary  $k_x$ -sized set of child nodes  $z$  such that  $C_z \neq \perp$ . If no such set exists, the node is not satisfied and the algorithm aborts. Otherwise, compute:

$$\begin{aligned}
 C_x &= \prod_{z \in S_x} (e(g, h)^{s \cdot q_z(0)})^{\Delta_{i, S'_x}(0)} \\
 &= \prod_{z \in S_x} (e(g, h)^{s \cdot q_{\text{parent}(z)}(\text{index}(z))})^{\Delta_{i, S'_x}(0)} \\
 &= \prod_{z \in S_x} e(g, h)^{s \cdot q_x(i) \cdot \Delta_{i, S'_x}(0)} \\
 &= e(g, h)^{s \cdot q_x(0)}.
 \end{aligned}$$

Note that  $i = \text{index}(z)$ ,  $S'_x = \{\text{index}(z) : z \in S_x\}$ , and the computation  $\Delta_{i, S'_x}(0)$  is computed via the polynomial interpolation according to access tree  $A$ .

2. If the attribute set associated with the ciphertext satisfies the tree  $A$ , we get  $e(g, h)^{s \cdot q_R(0)} = e(g, h)^{\alpha \cdot s}$ , and next compute  $(m \| ID) = \widehat{C} \oplus \mathbf{G}(e(g, h)^{\alpha \cdot s})$ ;
3. If  $e(S, g) = e(\mathbf{H}_1(ID), g^\beta) \cdot e(\mathbf{H}_2(m), C)$ , it returns  $m$ ; Otherwise, reject.

**Lemma 1.** *The proposed HSC scheme achieves EUF-CMA security under the CDH assumption.*

*Proof.* Let  $\mathcal{S}_{CDH}$  denotes a Computational Diffie-Hellman problem solver, who is given  $g, g^a, g^b$  and aims to find  $g^{ab}$ . Let  $\mathcal{A}$  denotes a forger against the proposed HSC scheme.  $\mathcal{S}_{CDH}$  plays the EUF-CMA security game with  $\mathcal{A}$  as follows.

- Setup Stage: Let  $\mathcal{K}$  denotes the maximum number of users that will occur in the game.  $\mathcal{S}_{CDH}$  randomly selects two indices  $i$  and  $j$  and guesses that the **Forge** event will happen with regard to user  $i$  and the  $j$ -th query (denote it by  $m^*$ ) to the random oracle  $\mathbf{H}_2$ .  $\mathcal{S}_{CDH}$  further sets  $g^\beta = g^a$ , and generates master secret/public keys  $(msk = (\alpha, t_1, \dots, t_{\mathcal{K}+1}), mpk = (T_1 = g^{t_1}, \dots, T_{\mathcal{K}+1} = g^{t_{\mathcal{K}+1}}, g^\alpha, e(g, h)^\alpha, h = g^\theta))$  as in the real scheme.  $\mathcal{S}_{CDH}$  finally sends  $mpk$  to  $\mathcal{A}$ . Note that  $\theta \in_R \mathbb{Z}_q$  is chosen by  $\mathcal{S}_{CDH}$ .
- $\mathcal{S}_{CDH}$  answers  $\mathcal{F}$ 's queries as follows.
  - If  $\mathcal{A}$  issues  $ID_i$  to random oracle  $\mathbf{H}_1$ , then  $\mathcal{S}_{CDH}$  chooses  $b_i \in_R \mathbb{Z}_q$  and returns  $g^b \cdot g^{b_i}$  as the public key of user  $i$ ; Otherwise,  $\mathcal{S}_{CDH}$  chooses  $b_j \in_R \mathbb{Z}_q$  returns the value  $g^{b_j}$  to  $\mathcal{F}$ .
  - If  $\mathcal{A}$  queries the random oracle  $\mathbf{H}_2$  with regard to the message  $m^*$ , then  $\mathcal{S}_{CDH}$  chooses  $c_i \in_R \mathbb{Z}_q$  and returns  $g^{c_i}$  as the response to  $\mathbf{H}_2(m^*)$ . If  $\mathcal{A}$  queries the random oracle  $\mathbf{H}_2$  with regard to other messages (e.g.,  $m_i$ ), then  $\mathcal{S}_{CDH}$  chooses  $c_i \in_R \mathbb{Z}_q$  and returns  $g^{c_i - a}$  as the response.
  - If  $\mathcal{A}$  issues a KeyGen query for the user  $i$ , **abort**. If  $\mathcal{A}$  issues a KeyGen query of a user  $ID_j$  (whereby  $j \neq i$ ),  $\mathcal{S}_{CDH}$  returns the value  $g^{a \cdot b_j}$  as the signing key to  $\mathcal{A}$ , and further simulates the decryption key exactly same as in the algorithm KeyGen.  $\mathcal{A}$  is given both the signing key and the decryption key of the user  $j$ .

- $\mathcal{S}_{CDH}$  simulates the Signcrypt oracle for the user  $i$  as follows. Firstly,  $\mathcal{S}_{CDH}$  chooses  $k_i \in_R \mathbb{Z}_q$ , generates  $\widehat{C} = (m_i \| ID_i) \oplus \mathbb{G}(e(g, h)^{\alpha \cdot (b+k_i)})$ ,  $C = g^{b+k_i}$ ,  $S_i = g^{b \cdot c_i} \cdot g^{a \cdot (b_i - k_i)} \cdot g^{c_i \cdot k_i}$ , where the randomness  $s$  is implicitly sets as  $b + k_i$ . Secondly,  $\mathcal{S}_{CDH}$  generates  $\{C_i\}_{i \in \delta} = \{T(i)^{b+k_i}\}_{i \in \delta}$  using the knowledge of  $t_i$  and  $\theta$ . Finally,  $\mathcal{S}_{CDH}$  returns the signcryption  $CT = \{\delta, \widehat{C}, C, \{C_i\}_{i \in \delta}, S_i\}$  to  $\mathcal{A}$ . One can verify that the signcryption is valid since  $g^{c_i - a} = \mathbb{H}_2(m_i)$  and  $e(S_i, g) = e(g^b \cdot g^{b_i}, g^a) \cdot e(g^{c_i - a}, g^{b+k_i})$ .  
 Note that if  $\mathcal{A}$  issues the Signcrypt query for other users, e.g., user  $l$  ( $l \neq i$ ),  $\mathcal{S}_{CDH}$  can simulate it perfectly since the simulator knows the signing key.
  - If  $\mathcal{A}$  issues an Unsigncrypt query,  $\mathcal{S}_{CDH}$  answers the query as usual since  $\mathcal{S}_{CDH}$  has the knowledge of  $\alpha$ .
- If  $\mathcal{A}$  successfully forges a signcryption  $CT^*$  including a valid forgery  $C^* = g^{s^*}$ ,  $S^* = g^{(b+b_i) \cdot a} \cdot \mathbb{H}_2(m^*)^{s^*}$  (notice that the randomness  $s^*$  is chosen by  $\mathcal{A}$ ) satisfying the validity check,  $\mathcal{S}_{CDH}$  can compute  $g^{a \cdot b} = \frac{S^*}{C^{* \cdot c_i} \cdot g^{a \cdot b_i}}$  ( $c_i$  is known to  $\mathcal{S}_{CDH}$  who programmed the random oracle  $g^{c_i} = \mathbb{H}_2(m^*)$ ) as the solution of the Computational Diffie-Hellman problem.

Probability analysis: Let  $q_{h_i}$  denotes the number of queries that  $\mathcal{F}$  asks to the random oracles  $\mathbb{H}_i$ ,  $i = 1, 2$ . If  $\mathcal{S}_{CDH}$  guesses the challenge user  $i$  and challenge message correctly, then the simulation is perfect. Therefore we have

$$\Pr[\mathbf{Forge}] \leq \mathcal{K} \cdot q_{h_2} \cdot \text{Adv}_S^{CDH}(k).$$

### 3.4 Our OAKE Protocol

Now we present our proposed one-round authenticated key exchange protocol in the multiple party setting. It works as follows:

- **Setup:** TA takes the security parameter  $k$  and the number of users  $\mathcal{K}$  as input, outputs the master public key  $mpk = (T_1 = g^{t_1}, \dots, T_{n+1} = g^{t_{n+1}}, g^\alpha, g^\beta, e(g, h)^\alpha, \{\mathbb{G}, \mathbb{G}_1, \dots, \mathbb{G}_\mathcal{K}\}, \{g, g_1, \dots, g_\mathcal{K}\}, h \in_R \mathbb{G})$  and the master secret key  $msk = (t_1, \dots, t_{n+1}, \alpha, \beta \in_R \mathbb{Z}_q)$ . In addition, let  $\hat{e} : \mathbb{G}_i \times \mathbb{G}_j \rightarrow \mathbb{G}_{i+j}$  denotes the  $\mathcal{K}$ -linear maps and  $e : \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}_T$  denotes the bilinear maps. TA also generates three hash functions  $\mathbb{H}_1 : \{0, 1\}^* \rightarrow \mathbb{G}, \mathbb{H}_2 : \{0, 1\}^* \rightarrow \mathbb{Z}_q, \mathbb{H}_3 : \{0, 1\}^* \rightarrow \mathbb{G}$ . We let  $N$  be the set  $\{1, 2, \dots, n + 1\}$  and define a function  $T$  as  $T(X) = h^{X^n} \cdot \prod_{i=1}^{n+1} T_i^{\Delta_i, N(X)}$ .
- **KeyGen:** Run the KeyGen algorithm described in the HSC scheme.
- **KeyExchange:** User  $i$  performs the following steps.
  1. Choose the ephemeral secret key  $r_i \in_R \mathbb{Z}_q$ , computes  $x_i = \mathbb{H}_2(r_i \| dk_i \| sk_i)$  and  $m_i = g_1^{x_i}$ ;
  2. Run the Signcrypt algorithm described in the HSC scheme, but the algorithm sets the randomness as  $x_i$ ;
  3. Compute  $S_i = sk \cdot \mathbb{H}_3(m_i \| ts_i)^{x_i}$ , where  $ts_i \in_R \mathbb{Z}_q$  is the current timestamp generated by user  $i$ ;
  4. **Broadcast** the signcryption:  $CT = \{ts_i, \delta_i, \widehat{C}, C, \{C_i\}_{i \in \delta}, S_i\}$ .

- **SharedKey**: After receiving the ciphertext  $CT_j = \{ts_j, \delta_j, \widehat{C}, C, \{C_j\}_{j \in \delta}, S_j\}$  from user  $j$ , user  $i$  does the following operations.
  1. Check the time-stamp: If  $|ts_i - ts_j| > \varrho$  ( $ts_i$  is the current time-stamp generated by user  $i$  and  $\varrho$  denotes the time window), then **reject**;
  2. Run the **Unsigncrypt** algorithm described in the HSC scheme, then get the message  $m_j = g_1^{x_j}$  and  $ID_j$ , and verify: If  $e(S_j, g) = e(\mathbf{H}_1(ID_j), g^\beta) \cdot e(\mathbf{H}_3(m_j || ts_j), C)$ , it returns  $m_j$ ; Otherwise, it rejects the session;
  3. **Compute** the session key:  $SK_i = \widehat{e}(g_1^{x_1}, \dots, g_1^{x_{i-1}}, g_1^{x_{i+1}}, \dots, g_1^{x_{\mathcal{K}}})^{x_i} = g_{\mathcal{K}-1}^{\prod_{j=1}^{\mathcal{K}} x_j}$ .

**Design Rational.** The proposed Hybrid Signcrypton scheme has been used in the OAKE protocol for preventing the insider attacks in the multi-party setting. In addition, the Hybrid Signcryption scheme also ensures the user privacy in the proposed OAKE protocol. More details will be given in the full version of the paper.

## 4 Security Analysis

**Theorem 1.** *The proposed OAKE protocol achieves session key security (Definition 1) if the  $\mathcal{K}$ -MDDH assumption hold in the underlying group  $\mathbb{G}_{\mathcal{K}-1}$ , the proposed signcryption scheme HSC is EUF-CMA secure.*

*Proof.* We define a sequence of games  $G_i, i = 0, \dots, 3$  and let  $\text{Adv}_i^{\text{OAKE}}$  denotes the advantage of the adversary in game  $G_i$ . Assume that  $\mathcal{A}$  activates at most  $m$  sessions in each game.

- $G_0$  This is original game  $\text{Game}_{\mathcal{A}}^{\text{OAKE}}$  for session key security.
- $G_1$  This game is identical to game  $G_0$  except that  $\mathcal{S}$  will output a random bit if **Forge** event happens where  $\mathcal{A}$  makes a send query in the form of  $CT_i$ , such that  $S_i$  is a valid signature of user  $i$  who is not corrupted (i.e., no long term key reveal query to user  $i$  or master secret key reveal query) when the send query is made, and  $S_i$  is not previously generated by the simulator. Therefore we have:

$$|\text{Adv}_0^{\text{OAKE}} - \text{Adv}_1^{\text{OAKE}}| \leq \Pr[\mathbf{Forge}] \quad (1)$$

**Lemma 2.** *The **Forge** event happens only with a negligible probability when our proposed signcryption scheme HSC is EUF-CMA secure.*

Let  $\mathcal{F}$  denotes a forger against signcryption scheme HSC with EUF-CMA security, who has access to the Signcrypt oracle, the Unsigncrypt oracle and the KeyGen oracle, and aims to forge a valid signature  $S^*$ .  $\mathcal{F}$  simulates the game for  $\mathcal{A}$  as follows.

- Setup Stage:  $\mathcal{F}$  sets up the game for  $\mathcal{A}$  by creating  $\mathcal{K}$  users with the corresponding identity set  $\prod_{i=1}^{\mathcal{K}} \{ID_i\}$ .  $\mathcal{F}$  randomly selects an index  $i$  and guesses that the **Forge** event will happen with regard to user  $i$ .  $\mathcal{F}$  then sends the

master public keys and the identity set to  $\mathcal{A}$ .  $\mathcal{F}$  obtains all the user secret keys except the secret key of  $ID_i$  via the **KeyGen** oracle. It is obvious that  $\mathcal{F}$  can answer all the queries made by  $\mathcal{A}$  except user  $i$ . Below we mainly focus on the simulation of user  $i$  only.

- $\mathcal{F}$  answers  $\mathcal{A}$ 's queries as follows.
  - \* If  $\mathcal{A}$  issues a send query in the form of a signcryption  $CT$  to user  $i$ , then  $\mathcal{F}$  will perform the simulation as follows:  $\mathcal{F}$  firstly can get the message  $g_1^x$  and the identity  $ID$  after submitting the received signcryption  $CT$  to his **Unsigncrypt** oracle. If  $\mathcal{A}$  makes a send query in the form of an activation request,  $\mathcal{F}$  randomly chooses  $r_i \in_R \mathbb{Z}_q$  and programs the  $H_2$  oracle to get  $x_i$ , computes the message  $g_1^{x_i}$  and generates the signcryption  $CT_i$  using his **Signcrypt** oracle on the message  $g_1^{x_i} || ID_i$  and returns  $CT_i$  to  $\mathcal{A}$ .
  - \* If  $\mathcal{A}$  issues an ephemeral secret key reveal query to user  $i$ , then  $\mathcal{F}$  returns  $r_i \in_R \mathbb{Z}_q$  to  $\mathcal{A}$ .
  - \* If  $\mathcal{A}$  issues long term secret key reveal query to user  $i$  or master secret key reveal query, then  $\mathcal{F}$  aborts.
  - \*  $\mathcal{F}$  answers the session key reveal query and test query by using the session key it has derived during the protocol simulation described above.
- If a **Forge** event with respect to user  $i$  occurs, then  $\mathcal{F}$  outputs whatever  $\mathcal{A}$  outputs as its own forgery; Otherwise,  $\mathcal{F}$  aborts the game. Therefore we have:

$$\Pr[\mathbf{Forge}] \leq \mathcal{K} \cdot \text{Adv}_{\mathcal{F}}^{\text{HSC}}(k) \tag{2}$$

- $G_2$ : This game is identical to game  $G_1$  except the following difference:  $\mathcal{S}$  randomly chooses  $g \in [1, m]$  as a guess for the index of the test session.  $\mathcal{S}$  will output a random bit if  $\mathcal{A}$ 's test query does not occurred in the  $g$ -th session (denote this event by **Guess**). Therefore we have

$$\text{Adv}_1^{\text{OAKE}} = m \cdot \text{Adv}_2^{\text{OAKE}} \tag{3}$$

- $G_3$  This game is identical to game  $G_2$  except that in the test session, we replace the session key  $SK = g_{\mathcal{K}-1}^{\prod_{j=1}^{\mathcal{K}} x_j}$  by a random value  $R \in_R \mathbb{G}_{\mathcal{K}-1}$ . Below we show that the difference between  $G_2$  and  $G_3$  is negligible under the  $\mathcal{K}$ -MDDH assumption is hold in the group  $G_{\mathcal{K}-1}$ .

Let  $\mathcal{S}_{\mathcal{K}\text{-MDDH}}$  denotes a distinguisher against the  $\mathcal{K}$ -MDDH assumption, who is given  $(g_1^{c_1}, \dots, g_1^{c_{\mathcal{K}}})$  and aims to distinguish the value  $T = g_{\mathcal{K}-1}^{\prod_{j=1}^{\mathcal{K}} c_j}$  from a random value  $R \in_R \mathbb{G}_{\mathcal{K}-1}$ .  $\mathcal{S}_{\mathcal{K}\text{-MDDH}}$  simulates the game for  $\mathcal{A}$  as follows.

- Setup Stage:  $\mathcal{S}_{\mathcal{K}\text{-MDDH}}$  sets up the game for  $\mathcal{A}$  by creating  $\mathcal{K}$  users.  $\mathcal{S}_{\mathcal{K}\text{-MDDH}}$  then generates the master public/secret key pair  $(mpk, msk)$  and the secret keys  $\{(dk_i, sk_i)\}$  for all the users, where the  $dk_i$  is corresponding to an access tree  $\Lambda_i$  and  $sk_i$  is corresponding to the identity  $ID_i$  of user  $i$ .  $\mathcal{S}_{\mathcal{K}\text{-MDDH}}$  then sends the master public key and the identity set to  $\mathcal{A}$ .
- It is easy to see that all queries to a user can be simulated perfectly using the user secret keys. In the  $g$ -th (i.e., test) session,  $\mathcal{S}_{\mathcal{K}\text{-MDDH}}$  sets  $m_1 =$

$g_1^{c_1}, \dots, m_{\mathcal{K}} = g_1^{c_{\mathcal{K}}}$  for all the users which implicitly sets  $H(r_i \| dk_i \| sk_i) = c_i$  where  $r_i$  denotes the ephemeral key of user  $i$  in the  $g$ -th session. Since  $\mathcal{A}$  is not allowed to ask both ephemeral and long term secret keys of a user in the test session, the simulation is perfect.

- $\mathcal{S}_{\mathcal{K}-MDDH}$  answers the Test query by using its own challenge as the session key of the  $g$ -th session.
- If  $\mathcal{A}$  wins the game, then  $\mathcal{S}_{\mathcal{K}-MDDH}$  outputs that the challenge is  $g_{\mathcal{K}-1}^{\prod_{j=1}^{\mathcal{K}} c_j}$ ; Otherwise  $\mathcal{S}_{\mathcal{K}-MDDH}$  outputs that the challenge is a random element.

If the challenge of  $\mathcal{S}_{\mathcal{K}-MDDH}$  is  $g_{\mathcal{K}-1}^{\prod_{j=1}^{\mathcal{K}} c_j}$ , then the simulation is consistent with  $G_2$ ; Otherwise, the simulation is consistent with  $G_3$ . If the advantage of  $\mathcal{A}$  is significantly different in  $G_2$  and  $G_3$ , then  $\mathcal{S}_{\mathcal{K}-MDDH}$  can break the  $\mathcal{K}$ -MDDH assumption. Therefore we have

$$|\text{Adv}_2^{OAKE} - \text{Adv}_3^{OAKE}| \leq \text{Adv}_{\mathcal{S}_{\mathcal{K}-MDDH}}^{\mathcal{K}-MDDH}(k) \quad (4)$$

It is easy to see that in game  $G_3$ ,  $\mathcal{A}$  has no advantage, i.e.,

$$\text{Adv}_3^{OAKE} = 0 \quad (5)$$

Combining the above results together, we have

$$\text{Adv}_{\mathcal{A}}^{OAKE}(k) \leq \mathcal{K} \cdot \text{Adv}_{\mathcal{F}}^{HSC}(k) + m \cdot \text{Adv}_{\mathcal{S}_{\mathcal{K}-MDDH}}^{\mathcal{K}-MDDH}(k)$$

**Theorem 2.** *The proposed OAKE protocol achieves insider security (Definition 2) if the proposed signcryption scheme HSC is EUF-CMA secure.*

The proof of insider security can be obtained from the proof of Lemma 2 since if an attacker can break the insider security with a non-negligible probability, then a **Forge** event would occur also with a non-negligible probability. We omit the details of the proof here.

## 5 Conclusion

In this paper, we proposed a one-round attribute-based key exchange (OAKE) protocol in the multi-party setting. In order to address the insider security issue, we proposed a new primitive named hybrid signcryption which is a combination of attribute-based encryption and identity-based signature. We used this new primitive and the multilinear maps as major building block in constructing our OAKE protocol. We also defined the formal security models for session key security and insider security, and proved the security of the proposed OAKE protocol in the random oracle model.

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