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# Exploring relationship between indistinguishability-based and unpredictability-based RFID privacy models

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## HIGHLIGHTS

- We show an imperfection of un<sup>\*</sup>-privacy model.
- We re-investigate the relationship between un<sup>\*</sup>-privacy and ind-privacy.
- We present a new unpredictability-based privacy model called un<sup>τ</sup>-privacy.
- We explore the relations among the three privacy notions with formal proofs.
- We design a new RFID mutual authentication protocol and prove its security under the un<sup>τ</sup>-privacy model.

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## ABSTRACT

A comprehensive privacy model plays a vital role in the design of privacy-preserving RFID authentication protocols. Among various existing RFID privacy models, indistinguishability-based (ind-privacy) and unpredictability-based (unp-privacy) privacy models are the two main categories. Unp<sup>\*</sup>-privacy, a variant of unp-privacy has been claimed to be stronger than ind-privacy. In this paper, we focus on studying RFID privacy models and have three-fold contributions. We start with revisiting unp<sup>\*</sup>-privacy model and figure out a limitation of it by giving a new practical traceability attack which can be proved secure under unp<sup>\*</sup>-privacy model. To capture this kind of attack, we improve unp<sup>\*</sup>-privacy model to a stronger one denoted as un<sup>τ</sup>-privacy. Moreover, we prove that our proposed privacy model is stronger than ind-privacy model. Then, we explore the relationship between unp<sup>\*</sup>-privacy and ind-privacy, and demonstrate that they are actually not comparable, which is in contrast to the previous belief. Next, we present a new RFID mutual authentication protocol and prove that it is secure under un<sup>τ</sup>-privacy model. Finally, we construct a RFID mutual authentication model denoted as MA model, and show that un<sup>τ</sup>-privacy implies MA, which gives a reference to design a privacy-preserving RFID mutual authentication protocol. That is, if we propose a scheme that satisfies un<sup>τ</sup>-privacy, then it also supports mutual authentication.

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## 1. Introduction

Radio Frequency Identification (RFID) allows automatic identification and track of tags attached to objects by utilizing electromagnetic induction. Due to its many attractive features compared with barcodes such as high throughput, not requiring line of light of the reader and supporting cryptographic algorithms to provide security, RFID has been extensively adopted in our daily life like

personal identity identification cards, payments, and supply chain management.

While the scope of RFID applications is growing fast nowadays, it may also introduce kinds of serious security and privacy concerns [1–5]. Since each tag may contain some information of its owners or bearers, once the tag is corrupted, its owners' or bearers' privacy will also be disclosed consequently. Moreover, standard cryptographic techniques are too resource-consuming to be implemented on low-cost RFID tags. Therefore, it is desirable to employ less computationally expensive cryptographic functions when designing protocols for RFID systems. In this paper, we mainly look into the privacy issues of RFID tags. Generally, a

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tag's privacy is guaranteed if the attacker cannot link or trace the tag.

A lot of efforts have been made to address the RFID tags' privacy concerns, which produces two different methods. The first one is designing privacy-preserving RFID authentication protocols, which has attracted a large number of researchers' attention [6–19]. Most of these protocols employ symmetric encryption technique for the sake of efficiency but may lose security, while a few works build secure authentication protocols based on efficient public key cryptography like Elliptic curve cryptography (ECC). Very recently, some nice works for lightweight implementation of ECC protocols on sensor nodes are done [20,21]. It will be interesting to investigate whether those protocols can be employed on low-cost RFID tags. The other one is constructing formal RFID privacy models [22–36]. Among these models, two categories stand out: one based on the indistinguishability of two tags [32], denoted as ind-privacy, and the other one based on the unpredictability of RFID protocol's outputs [26], denoted as un<sup>p</sup>-privacy. Ind-privacy is reasonably good while it is difficult to apply ind-privacy model to prove whether a given protocol is ind-private. To deal with this issue, Ha et al. [26] proposed the un<sup>p</sup>-privacy model and it has been rectified to the eun<sup>p</sup>-privacy model by Ma et al. [23]. Later, Li et al. [24] presented an improved version of the eun<sup>p</sup>-privacy model called un<sup>p\*</sup>-privacy.

In this paper, we continue studying the privacy models for RFID authentication protocols, beginning with revisiting the un<sup>p\*</sup>-privacy model. After that, we put forward a new RFID privacy model as well as exploring the relations among our model and previous ones. Moreover, we come up with a new RFID mutually authenticated protocol and prove its security under our proposed privacy model. Finally, as an interesting extension, we formalize a mutual authentication model and delve into its relationship with the proposed privacy model. The detailed contributions are as follows.

### 1.1. Our contributions

- (1) We review the un<sup>p\*</sup>-privacy model, and demonstrate a practical attack to a counterexample protocol which can be proved secure under the un<sup>p\*</sup>-privacy model. It indicates that un<sup>p\*</sup>-privacy is not enough for capturing this kind of attacks. In particular, the adversary can utilize the observation of the reactions of the reader and the tag in a concrete protocol to win the security game, while this capability is not considered in un<sup>p\*</sup>-privacy.
- (2) We re-investigate the relationship between un<sup>p\*</sup>-privacy and ind-privacy and prove that un<sup>p\*</sup>-privacy is not comparable with ind-privacy, which is in contrast to the previous claim that un<sup>p\*</sup>-privacy was stronger than ind-privacy in [24]. In the original ind-privacy model [32], the adversary has the ability to recognize whether or not the tag is accepted, which can be derived from the implications of the privacy experiment in Juels et al.'s paper [32] after the experiment definition. In our paper, we also suppose the adversary can observe whether or not a tag accepts the reader since we consider a mutual authentication. When giving proof of the fact that un<sup>p\*</sup>-privacy can imply ind-privacy in [24], the authors ignored the adversary's ability of observing those results. Therefore, we can find a counterexample that is un<sup>p\*</sup>-private but not ind-private, which means un<sup>p\*</sup>-privacy cannot imply ind-privacy, either.

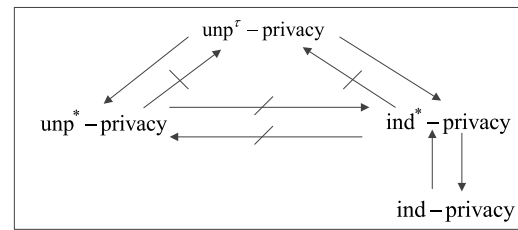


Fig. 1. Relations among privacy models.

- (3) We present the unpredictability-based un<sup>p\*</sup>-privacy model, and provide a formal analysis of its capability of handling the above mentioned practical attacks.
- (4) We revisit the relations among the three notions and formally prove that un<sup>p\*</sup>-privacy implies ind-privacy and un<sup>p</sup>-privacy while not vice versa. This means that our proposed un<sup>p\*</sup>-privacy is stronger than the other two.
- (5) We design a new RFID mutual authentication protocol and prove that it is secure under the un<sup>p\*</sup>-privacy model.
- (6) Upon making further analysis on un<sup>p\*</sup>-privacy, we figure out an interesting and useful result, that is, any protocol satisfying un<sup>p\*</sup>-privacy must support mutual authentication. To verify that point, we first construct a mutual authentication model, denoted as MA, and then prove that un<sup>p\*</sup>-privacy implies MA. This gives us a reference to design a secure RFID mutual authentication protocol with tag privacy.

In order to make it clearer to see our contributions, we give a figure to depict the relations among three recently proposed privacy models including our new un<sup>p\*</sup>-privacy model in Fig. 1. Since it is hard to directly investigate the relationship between ind-privacy and un<sup>p\*</sup>-privacy, we build the ind\*-privacy model that can be shown equivalent to ind-privacy and act as a “bridge” to discovering the relations.

### 1.2. Related work

In 2005, Avoine [22] proposed an adversary model for RFID systems and made the first step towards the formalization of the privacy of RFID protocols in terms of traceability. After that, based on Avoine's adversary model, in 2007, Juels and Weis [32] constructed a strong privacy model based on the indistinguishability of two tags, denoted as ind-privacy, for two-round RFID authentication protocols. In Juels and Weis's privacy model, the target tags are chosen by the adversary itself rather than the Challenger, which intuitively gives the adversary more powerful capability. However, it is difficult to apply ind-privacy model in security analysis of an RFID protocol. In ESORICS 2010 [25], Deng et al. proposed a zero-knowledge based privacy model, denoted as ZK-privacy, and they proved that their model is stronger than ind-privacy model; however, Moriyama et al. have shown that ZK-privacy is equivalent to ind-privacy in ESORICS 2012 [34]. In ASIACRYPT 2007 [30], Vaudenay proposed a framework and classified the privacy models into eight categories by considering the side-channel attacks. After this work, Paise and Vaudenay [31] extended Vaudenay's model to address mutual authentication.

Ha et al. [26] proposed a new privacy model based on the unpredictability of the tag's outputs, denoted as un<sup>p</sup>-privacy. In CCS 2009, Ma et al. [23] refined the un<sup>p</sup>-privacy to an enhanced version called eun<sup>p</sup>-privacy. In Ma et al.'s paper, the authors also proved that a pseudorandom function family is the minimal requirement on an RFID tag's computational power to preserve strong privacy. This explains why lots of existing lightweight RFID authentication

protocols suffer from privacy problems [6,8–10]. Li et al. [24] improved  $\text{unp}^*$ -privacy to  $\text{unp}^*$ -privacy that can be applied to three round RFID protocols, and investigated the relation between  $\text{unp}^*$ -privacy and ind-privacy and proved that  $\text{unp}^*$ -privacy was stronger than ind-privacy.

This article is an extended version of our previous conference paper [35] in which we revisited  $\text{unp}^*$ -privacy and demonstrated a practical attack to a counterexample protocol that is  $\text{unp}^*$ -privacy secure. This shows that  $\text{unp}^*$ -privacy cannot capture this kind of practical attack. Therefore, we presented a new unpredictability-based privacy model for RFID which can handle the new attacks and has been proved to be stronger than  $\text{unp}^*$ -privacy. Except for these results, we also added sufficient extra work to this article as follows. First, we explored the relationship between  $\text{unp}^*$ -privacy and ind-privacy and proved that  $\text{unp}^*$ -privacy is not comparable with ind-privacy, which is in contrast to the previous claim that  $\text{unp}^*$ -privacy was stronger than ind-privacy in [24]. Moreover, we designed a new RFID mutual authentication protocol and proved that it is secure under the  $\text{unp}^*$ -privacy model. Finally, we built a mutual authentication model  $MA$ , and formally analysed its relationship with  $\text{unp}^*$ -privacy.

### 1.3. Organization

We organize the remainder of this paper as follows. In Section 2, we give definitions of the RFID system model, the adversary model and some mathematical notations used in the paper. In Section 3, we revisit existing privacy models, i.e., ind-privacy and  $\text{unp}^*$ -privacy, and we also explored the relation between ind-privacy and  $\text{unp}^*$ -privacy. In Section 4, we present our new privacy model  $\text{unp}^*$ -privacy and establish its relation with ind-privacy and  $\text{unp}^*$ -privacy. In Section 5, we propose a new RFID mutual authentication protocol with  $\text{unp}^*$ -privacy. In Section 6, we construct a mutual authentication model  $MA$  and explore the relation between  $\text{unp}^*$ -privacy and  $MA$ . Finally, in Section 7, we make a conclusion of this paper.

## 2. Definitions

### 2.1. RFID system model

An RFID system is constituted of a set of tags  $\mathcal{T}_1, \mathcal{T}_2, \dots, \mathcal{T}_n$ , a database and a reader  $R$  connected to the database. A tag  $\mathcal{T}_i$  with an identity  $ID_i$  shares a secret key  $k_i$  and possibly some state information  $st_i$  with  $R$ . The database stores  $(k_i, st_i, ID_i)$  for  $\mathcal{T}_i$  and  $R$ .

**Definition 1.** An RFID authentication system RAS consists of a tuple  $(R, \mathcal{T}, \text{SetupReader}, \text{SetupTag}, \text{ReaderStart}, \text{TagCompute}, \text{ReaderCompute}, \pi)$ , where

**SetupReader:** the initialization algorithm to set up the reader with system parameters  $\pi$ .

**SetupTag:** the initialization algorithm to set up the tag such as the identity, the secret key and the initial state information.

**ReaderStart:** the algorithm run by the reader to generate a session identifier of a fresh session, denoted as  $sid$ , and a fresh challenge message  $c_{sid}$  of this session.

**TagCompute**( $\mathcal{T}_i, sid, c_{sid}$ ): the algorithm run by the tag  $\mathcal{T}_i$  to calculate the response  $r_{sid}$ , with inputs of  $sid$  and  $c_{sid}$ .

**ReaderCompute**( $sid, c_{sid}, r_{sid}$ ): the algorithm run by the reader to calculate the final information  $f_{sid}$ , with inputs of  $sid, c_{sid}$  and  $r_{sid}$ .

**Protocol**  $\pi(R, \mathcal{T}_i)$ : a polynomial time interactive protocol run by the reader  $R$  and the tag  $\mathcal{T}_i$ . Upon running the protocol, the algorithms of ReaderStart, TagCompute, ReaderCompute may be invoked.

A protocol  $\pi(R, \mathcal{T}_i, sid)$  is executed successfully if and only if the reader and the tag accept each other.

We define the completeness and soundness of RAS in accordance with Li et al. [24]. In particular, a RAS is complete if legitimate parties including tags and reader can always pass the protocol. Suppose  $(c_{sid}, r_{sid}, \dots)$  is the output of session  $sid$ , where  $r_{sid}$  is correctly generated by a legitimate tag, then completeness means that the reader  $R$  and the tag accepts each other with probability 1 for any such session. A RAS is sound if only legitimate tags/reader can pass the protocol, that is, any adversary cannot impersonate a tag or a reader successfully. Actually, in a practical RFID protocol, soundness means this protocol should provide tag/reader authentication. Li et al. only considered the soundness for tag authentication which requires an adversary cannot impersonate a tag. In our paper, we also consider the soundness for reader authentication, that is we consider the mutual authentication of RFID protocols. We will design a general model for mutual authentication in Section 6.

**Remark 1.** In this paper, we assume that at any time a tag can only involve one protocol session and it will remove its old secret key and state information upon updating them.

### 2.2. Adversary model

The adversary  $\mathcal{A}$  has computation capability of probabilistic polynomial time (PPT), and can control the wireless communication channel which means it can intercept or modify messages transmitted in the air. It can also observe the protocol results, i.e. the reaction of the reader or the tag ('accept' or 'reject'). To sum up, the adversary can adaptively query the following oracles.

**InitReader.** This oracle allows the adversary to know the initialization result of the reader for a new protocol session, and it will return a fresh  $sid$  and a fresh  $c_{sid}$ .

**SendTag** ( $\mathcal{T}_i, sid, c_{sid}$ ). On input of a tag  $\mathcal{T}_i$ , a session identifier  $sid$  and a challenge message  $c_{sid}$ , this oracle returns a message  $r_{sid}$ .

**SendReader** ( $sid, c_{sid}, r_{sid}$ ). On input of a session identifier  $sid$ , a challenge message  $c_{sid}$ , and the message  $r_{sid}$ , this oracle returns a message  $f_{sid}$ .

**Result** ( $sid, f_{sid}$ ). On input of a session identifier  $sid$  and a message  $f_{sid}$ , this oracle returns the reaction of the tag ('reject' or 'accept').

**SetTag** ( $\mathcal{T}_i$ ). On input of a tag  $\mathcal{T}_i$ , this oracle returns the tag's secret key and internal state information.

Hereafter, for simplicity, we use  $O_1, O_2, O_3, O_4, O_5$  to denote **InitReader**, **SendTag**, **SendReader**, **Result**, **SetTag** oracles respectively. And the following are some parameters:

- $\kappa$ : security parameter;
- $n$ : the number of tags in  $\mathcal{T}$ ;
- $q$ : the number of **InitReader** queries allowed;
- $s$ : the number of **SendTag** queries allowed;
- $u$ : the number of **SendReader** queries allowed;
- $v$ : the number of **Result** queries allowed;
- $w$ : the number of **SetTag** queries allowed;

Experiment  $\text{Exp}_T^{PTT}(F, m, n, p)$

1. Select  $b \in_R \{0, 1\}$ ;
2. If  $b = 1$ , select a random  $k \in \mathcal{K}$  and set  $f = F_k$ ; else if  $b = 0$ , select a random  $f' \in RF(\cdot)$  and set  $f = f'$ ;
3.  $b' \leftarrow T^{O_f}$ ;
4. The experiment outputs 1 if  $b' = b$ , 0 otherwise.

Fig. 2. Polynomial time test for  $F$ .

Experiment  $\text{Exp}_A^{ind}[\kappa, n, q, s, u, w]$

1. Initialize the RFID system with a reader  $R$  and a set of tags  $\mathcal{T}$  with  $|\mathcal{T}| = n$ ;
2.  $\{\mathcal{T}_i, \mathcal{T}_j, st\} \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_5}(R, \mathcal{T})$ ; //learning stage
3. set  $\mathcal{T}' = \mathcal{T} - \{\mathcal{T}_i, \mathcal{T}_j\}$ ;
4.  $b \in_R \{0, 1\}$ ;
5. If  $b=0$ , let  $\mathcal{T}_c = \mathcal{T}_i$ , else  $\mathcal{T}_c = \mathcal{T}_j$ ;
6.  $b' \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_5}(R, \mathcal{T}', st, \mathcal{T}_c)$ ; //guess stage
7. the experiment outputs 1 if  $b' = b$ , 0 otherwise.

Fig. 3. Ind-privacy experiment.

### 2.3. Mathematical notations

**Definition 2.** A function  $f$  is negligible if for every polynomial  $p(\cdot)$  there exists an integer  $N$  such that for all integers  $n > N$  it holds that  $f(n) < \frac{1}{p(n)}$ .

Let  $F : \mathcal{K} \times \mathcal{D} \rightarrow \mathcal{R}$  be a family of functions, where  $\mathcal{K}$  is the set of indexes of  $F$ ,  $\mathcal{D}$  is the domain of  $F$  and  $\mathcal{R}$  is the range of  $F$ . Let  $|\mathcal{K}| = m$ ,  $|\mathcal{D}| = n$ ,  $|\mathcal{R}| = p$ . Let  $RF : \mathcal{D} \rightarrow \mathcal{R}$  be the family of all functions with domain  $\mathcal{D}$  and range  $\mathcal{R}$ . A polynomial time test (PTT) for  $F$  is an experiment, where a probabilistic polynomial time algorithm  $T$  with inputs  $m, n, p$  and access to an oracle  $O_f$ , guesses that the function  $f$  is chosen from whether  $F(\cdot)$  or  $RF(\cdot)$ .  $b \in_R \{0, 1\}$  means that  $b$  is chosen uniformly at random from  $\{0, 1\}$ . We illustrate the PTT experiment in Fig. 2.

**Definition 3.** An algorithm  $T$  passes the PTT experiment for the function family  $F$  if the advantage that it guesses the correct value of bit  $b$  is non-negligible, where the advantage of  $T$  is defined as  $Adv_T(m, n, p) = |\Pr[b' = b] - \frac{1}{2}|$ ,  $k$  and  $f$  are chosen uniformly at random from  $\mathcal{K}$  and  $RF(\cdot)$ , respectively.

**Definition 4.** A function family  $F : \mathcal{K} \times \mathcal{D} \rightarrow \mathcal{R}$  is a pseudorandom function family (PRF) if there is no probabilistic polynomial time algorithm which can pass the PTT experiment for  $F$  with non-negligible advantage.

## 3. Revision of Ind-privacy and un $\rho^*$ -privacy

### 3.1. Ind-privacy

Juels and Weis [32] proposed the first indistinguishability-based RFID privacy model (ind-privacy). The intuitive idea of this model is that there is no adversary with the ability to distinguish two different tags with limited computational power and functionality-call bounds.

The ind-privacy experiment is briefly illustrated in Fig. 3. In the initialization phase, a reader and  $n$  tags are set up with the system parameters, where for each tag  $\mathcal{T}_i$ , the identifier, the secret key

Experiment  $\text{Exp}_A^{unp^*}[\kappa, n, q, s, u, w]$

1. Initialize the RFID system with a reader  $R$  and a set of tags  $\mathcal{T}$  with  $|\mathcal{T}| = n$ ;
2.  $\{\mathcal{T}_c, st\} \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_5}(R, \mathcal{T})$ ; //learning stage
3.  $b \in_R \{0, 1\}$
4.  $b' \leftarrow \mathcal{A}^{O_1, O_2, O_3}(R, \mathcal{T}_c, st)$  //guess stage
  - 4.1 When  $\mathcal{A}$  queries  $O_1, O_2, O_3$  oracles, if  $b=1$ , run the algorithm **ReaderStart**, **TagCompute**, **ReaderCompute** respectively, and return the results  $(c, r, f)$ ;
  - 4.2 else  $b=0$  pick  $c, r, f$  randomly from their respective domains and return them to  $\mathcal{A}$ .
5. the experiment outputs 1 if  $b' = b$ , 0 otherwise.

Fig. 4. Un $\rho^*$ -privacy experiment.

and optionally the internal state are created and shared with the reader  $R$ . During the learning phase, the adversary  $\mathcal{A}$  is allowed to query  $O_1, O_2, O_3$ , and  $O_5$  oracles within  $q, s, u$  and  $w$  times, respectively. Then  $\mathcal{A}$  is required to choose two tags  $(\mathcal{T}_i, \mathcal{T}_j)$  that have not been compromised, i.e., have not been queried with  $O_5$  oracle. In the challenge phase, the experiment randomly picks a bit  $b$  and determines the challenge tag according to the value of  $b$ , i.e.,  $\mathcal{T}_c = \mathcal{T}_i$  if  $b = 0$ , and  $\mathcal{T}_c = \mathcal{T}_j$  otherwise. In the guessing stage,  $\mathcal{A}$  is allowed to query  $O_1, O_2, O_3$ , and  $O_5$  oracles on the set of tags again within  $q, s, u$  and  $w$  times in total, respectively, except for that it cannot query  $O_5$  on the challenge tag  $\mathcal{T}_c$ . Finally,  $\mathcal{A}$  outputs a bit  $b'$ .

Let  $\text{Exp}_A^{ind}$  stand for the ind-privacy experiment. Let

$$\text{Adv}_A^{ind}[\kappa, n, q, s, u, w] = |\Pr[\text{Exp}_A^{ind} = 1] - \frac{1}{2}|.$$

**Definition 5.** An RFID authentication system RAS is said to be ind-private if for any PPT adversary  $\mathcal{A}$ ,  $\text{Adv}_A^{ind}[\kappa, n, q, s, u, w]$  is negligible.

**Discussion.** Juels and Weis's experiment [32] did not explicitly state the adversary's capability of observing whether the reader and the tag accept or reject each other, while they discussed this kind of attack after their description of the experiment. Therefore, their model can actually capture this attack.

### 3.2. Un $\rho^*$ -privacy

The idea of ind-privacy is quite appealing; however, it is very difficult to apply the ind-privacy model to prove whether a given RFID protocol is ind-private. To address this issue, Ha et al. [26] proposed the un $\rho$ -privacy model. After several modification, un $\rho$ -privacy model is improved to un $\rho^*$ -privacy model by Li et al. [24].

The un $\rho^*$ -privacy experiment is briefly illustrated in Fig. 4. The initialization phase and the learning phase are the same as that of the ind-experiment, except that after the learning phase,  $\mathcal{A}$  chooses a challenge tag  $\mathcal{T}_c$  which has not been queried for  $O_5$ . In the challenge phase, the experiment selects a random bit  $b$ . During this phase,  $\mathcal{A}$  can query  $O_1, O_2, O_3$  oracles on  $R$  and  $\mathcal{T}_c$  without exceeding  $q, s$  and  $u$  overall calls, respectively. Upon receiving an oracle query, the challenger will respond to  $\mathcal{A}$  with different strings according to the value of  $b$  as shown in Fig. 4.

Let

$$\text{Adv}_A^{unp^*}[\kappa, n, q, s, u, w] = |\Pr[\text{Exp}_A^{unp^*} = 1] - \frac{1}{2}|.$$

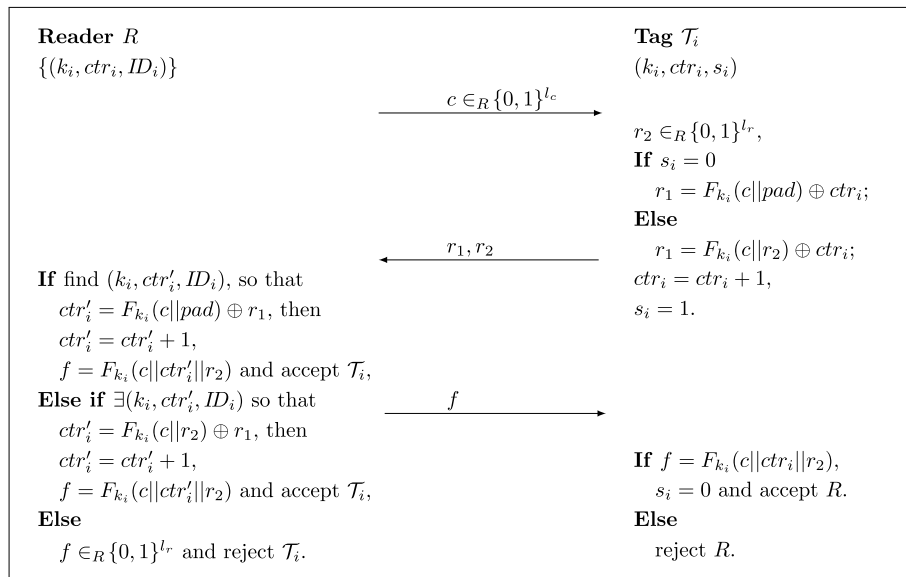


Fig. 5. A counterexample.

**Definition 6.** An RFID authentication system RAS is said to be  $unp^*$ -private if for any PPT adversary  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}^{unp^*}[\kappa, n, q, s, u, w]$  is negligible.

### 3.3. Revisiting $unp^*$ -privacy

As we have mentioned before, the adversary in the  $unp^*$ -privacy experiment has no idea of the reactions of the reader and the tag, whereas it is practical and easy to obtain this capability in most of RFID applications. For instance, a student with a student card can go into the library if the card is successfully authenticated; otherwise the student cannot enter if the card authentication fails. We will demonstrate a practical attack to a counterexample that is provably secure under the  $unp^*$ -privacy mode. This implies that  $unp^*$ -privacy is not enough to capture this kind of attacks against RFID authentication protocols.

#### 3.3.1. A counterexample

Let  $F : \{0, 1\}^{l_k} \times \{0, 1\}^{l_d} \rightarrow \{0, 1\}^{l_r}$  be a PRF family,  $ctr \in \{0, 1\}^{l_r}$  be a counter, and  $pad \in \{0, 1\}^{l_{pad}}$  be a padding so that  $l_r + l_{pad} = l_d$ . The values of  $ctr_i$  and  $s_i$  are initialized to be 1 and 0, respectively. The protocol works as follows depicted in Fig. 5.

- (1) The reader  $R$  randomly produces a challenge  $c$  and sends it to the tag  $\mathcal{T}_i$ .
- (2) The tag randomly generates a string  $r_2 \in \{0, 1\}^{l_r}$  and calculates  $r_1$  depending on the state information  $s_i$  that is initialized to be 0 at the setup phase.
- (3) The tag returns the response  $r_1, r_2$  to the reader, while meantime updating the values of  $ctr_i$  and  $s_i$ .
- (4) Upon receiving the response from the tag, the reader calculates and compares to find the matching tag according to the information stored in the database.
- (5) The final message from the reader will be verified by the tag. If the message is valid, the tag will update  $s_i$  and accept the reader; otherwise, the reader will be rejected.

**Theorem 1.** The counterexample is  $unp^*$ -private, given that the function family  $F : \{0, 1\}^{l_k} \times \{0, 1\}^{l_d} \rightarrow \{0, 1\}^{l_r}$  is a PRF family.

**Proof.** To prove the proposed counterexample in Fig. 5 is secure, we first assume it is not  $unp^*$ -private. Namely, a PPT adversary  $\mathcal{A}$

has the ability to pass the  $unp^*$ -privacy game with an advantage of more than  $\epsilon$  within time  $t$ . Then, we try to build an algorithm  $\mathcal{B}$  which invokes  $\mathcal{A}$  as a subroutine in order to win the  $PTT$  game defined for  $F$ . Due to the condition that  $F$  is a secure PRF family, there is supposed to be no PPT adversary that can pass the  $PTT$  game. Therefore, as long as we can reduce the problem of  $\mathcal{A}$  in  $unp^*$ -privacy experiment to the problem of  $\mathcal{B}$  in  $PTT$  experiment, then the proof is completed. In the following, we describe how  $\mathcal{B}$  simulates the  $unp^*$ -privacy game with  $\mathcal{A}$ .

*Simulate the initialization phase.* To simulate the setup phase,  $\mathcal{B}$  randomly chooses an index  $i \in [1, n]$  that will be considered as the index of the challenge tag, and initializes the value of  $ctr_i = 1$  and  $s_i = 0$ , respectively. Note that tag  $\mathcal{T}_i$ 's secret key  $k_i$  is set up implicitly, i.e.,  $\mathcal{B}$  has no idea of  $k_i$ . For the secret keys of the rest  $n - 1$  tags in  $\{\mathcal{T} - \mathcal{T}_i\}$ , they are randomly generated by  $\mathcal{B}$  according to the secret key space.

*Simulate the learning phase.* In the learning phase, to simulate the answers of queries  $O_1 \sim O_3$  and  $O_5$  by  $\mathcal{A}$ ,  $\mathcal{B}$  queries the oracle  $O_f$  in  $PTT$  experiment game and utilizes the keys  $\{k_j\}_{1 \leq j \leq n, j \neq i}$  to respond. If  $\mathcal{A}$  enquires  $O_5$  on the tag  $\mathcal{T}_i$ , then  $\mathcal{B}$  aborts the simulation.

*Simulate the challenge phase.* In the challenge phase,  $\mathcal{A}$  is required to submit a challenge tag  $\mathcal{T}_c$  that has not been queried with  $O_5$  (i.e., has not been corrupted). As in the initialization phase,  $\mathcal{B}$  has designated  $\mathcal{T}_i$  as the challenge tag, thus if  $\mathcal{T}_c \neq \mathcal{T}_i$ , then  $\mathcal{B}$  will abort the simulation.

*Simulate the guess phase.* To simulate the guess phase,  $\mathcal{B}$  utilize  $O_f$  query in the  $PTT$  game and the secret keys  $\{k_j\}_{1 \leq j \leq n, j \neq i}$  to respond the queries of  $O_1 \sim O_3$  by  $\mathcal{A}$  as shown in the following steps:

- ① Upon  $\mathcal{A}$  enquiring  $O_1$ ,  $\mathcal{B}$  randomly generates a session identifier  $sid$  and a challenge message  $c$  and returns  $(sid, c)$  to  $\mathcal{A}$ .
- ② Upon  $\mathcal{A}$  enquiring  $O_2$ ,  $\mathcal{B}$  first randomly generates  $r_2 \in_R \{0, 1\}^{l_r}$ . According to the value of the state  $s_i$ ,  $\mathcal{B}$  computes  $r_1$  with different methods, respectively. In particular, if  $s_i = 0$ , then  $\mathcal{B}$  queries  $O_f$  with the input of  $x = c||pad$ , obtaining the result  $y$  and computing  $r_1 = y \oplus ctr_i$ ; else  $\mathcal{B}$  queries  $O_f$  with the input of  $x = c||r_2$ , obtaining the result  $y$  and computing  $r_1 = y \oplus ctr_i$ . Finally,  $\mathcal{B}$  increases  $ctr_i$  by 1, updates  $s_i$  to be 1, and sends  $(r_1, r_2)$  to  $\mathcal{A}$ .

- ③ Upon  $\mathcal{A}$  enquiring  $O_3$ ,  $\mathcal{B}$  queries  $O_f$  with input of  $c||ctr_i||r_2$ , obtains the result  $f$  and returns  $f$  to  $\mathcal{A}$ .

**Output.** Finally,  $\mathcal{A}$  submits a bit  $b'$  as its output, and meantime  $\mathcal{B}$  also sets  $b'$  as its output.

It is not hard to see that if  $O_f = F_{k_i}$ , the simulation equals the  $\text{unp}^*$ -privacy game in the case of  $b = 1$ ; if  $O_f = RF$ , the simulation equals the  $\text{unp}^*$ -privacy game in the case of  $b = 0$ . Therefore, if the simulation is not aborted by  $\mathcal{B}$  specifically, then it is a perfect one. Note that the simulation will be aborted only if  $\mathcal{A}$  queries  $O_5$  on  $\mathcal{T}_c$  or submits a tag that is not  $\mathcal{T}_i$  as the challenge tag. Thus the probability that the simulation is not aborted can be calculated by  $(1 - \frac{w}{q+s+u+v+w}) \cdot \frac{1}{n}$ . This indicates that if  $\mathcal{A}$  can win the  $\text{unp}^*$ -privacy game with the advantage of more than  $\epsilon$ , then  $\mathcal{B}$  can win the PTT game with the advantage of more than  $(1 - \frac{w}{q+s+u+v+w}) \cdot \frac{\epsilon}{n}$ . Moreover, the running time of  $\mathcal{B}$  is approximate to that of  $\mathcal{A}$ . This contradicts the condition that  $F$  is a PRF family. And thus the proof is completed.  $\square$

### 3.3.2. A traceability attack

Although we have formally proved that the counterexample is secure under the  $\text{unp}^*$ -privacy model, we can demonstrate a practical traceability attack against it. Suppose the adversary  $\mathcal{A}$  can observe the protocol results, i.e., whether the reader and the tag accept each other, which is a common capability as we have stated before, then  $\mathcal{A}$  can obtain the state  $s_i$  of the tag  $\mathcal{T}_i$  trivially, since according to the protocol, if  $s_i$  equals 0, then  $r_1 = F_{k_i}(c||pad) \oplus ctr_i$  which indicates that the calculation of  $r_1$  does not depend on  $r_2$ . By this way,  $\mathcal{A}$  can intercept and modify  $r_2$  which will be transmitted to the reader  $R$ . Next,  $\mathcal{A}$  observes the result of the protocol. If  $\mathcal{T}_i$  is still accepted by  $R$ , then it shows that  $s_i$  is equivalent to 0; and else it shows that  $s_i$  is equivalent to 1. This attack can be used to trace the tag since normally each tag's state is initialized to be 0, and thus an active adversary could first flag a target tag's state by interfering with the final message sent from the reader, and then trace the tag.

### 3.4. Relation between $\text{unp}^*$ -privacy and Ind-privacy

In last section, we show the counterexample is secure under the  $\text{unp}^*$ -privacy model. In this section, we will demonstrate that it is not secure under the ind-privacy model and thus obtain the result that  $\text{unp}^*$ -privacy does not imply ind-privacy, which is in contrast to the previous belief that  $\text{unp}^*$ -privacy is stronger.

We have discussed that the adversary  $\mathcal{A}$  in the ind-privacy game can observe the protocol results. And  $\mathcal{A}$  can also flag a tag's state by an active attack. To win the ind-privacy game,  $\mathcal{A}$  has to distinguish two tags  $\mathcal{T}_i$  and  $\mathcal{T}_j$ . Before outputting the result,  $\mathcal{A}$  can flag one of the tags' state (say  $\mathcal{T}_i$ )  $s_i$  to be 1 by modifying  $f$ . Then  $\mathcal{A}$  can tell apart  $\mathcal{T}_i$  from  $\mathcal{T}_j$  trivially adopting the strategy used in the traceability attack. This indicates that  $\mathcal{A}$  can pass the ind-privacy game and the counterexample is not ind-private. Therefore, a protocol that can be proved secure under the  $\text{unp}^*$ -privacy model does not have to be proved secure under the ind-privacy model, that is,  $\text{unp}^*$ -privacy does not imply ind-privacy. Moreover, Li et al. [24] has proved that ind-privacy does not imply  $\text{unp}^*$ -privacy, either. According to the above results, we obtain the following claim.

**Claim 1.**  $\text{Unp}^*$ -privacy does not imply ind-privacy, and vice versa.

## 4. The proposed privacy model: $\text{unp}^\tau$ -privacy

According to the counterexample in Fig. 5, we know that  $\text{unp}^*$ -privacy cannot capture the traceability attack which is easily to be launched in practice. We propose a new RFID privacy model, denoted as  $\text{unp}^\tau$ -privacy, which can address this issue.

The  $\text{unp}^\tau$ -privacy experiment is briefly illustrated in Fig. 6. The initialization phase, the learning phase and the challenge phase are the same as that of the  $\text{unp}^*$ -privacy experiment, except that in the  $\text{unp}^\tau$ -privacy experiment, the adversary can query one more oracle ( $O_4$ ). In the guess phase,  $\mathcal{A}$  can query  $O_1 \sim O_4$  oracles on  $R$  and  $\mathcal{T}_c$  without exceeding  $q$ ,  $s$ ,  $u$  and  $v$  overall calls, respectively. Upon receiving an oracle query, the challenger will respond to  $\mathcal{A}$  with different ways according to the value of  $b$  as shown in Fig. 6.

Let

$$\text{Adv}_{\mathcal{A}}^{\text{unp}^\tau}[\kappa, n, q, s, u, v, w] = |\Pr[\text{Exp}_{\mathcal{A}}^{\text{unp}^\tau} = 1] - \frac{1}{2}|.$$

**Definition 7.** An RFID authentication system RAS is said to be  $\text{unp}^\tau$ -private if for any PPT adversary  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}^{\text{unp}^\tau}[\kappa, n, q, s, u, v, w]$  is negligible.

**Discussion.** Our proposed  $\text{unp}^\tau$ -privacy model can capture the practical traceability attack, that is, the given counterexample is not secure under the  $\text{unp}^\tau$ -privacy model, since the adversary with the ability of querying  $O_4$  can identify the value of  $b$  trivially. In particular,  $\mathcal{A}$  can manipulate the value of  $r_2$ , where in the case of  $b = 1$ , the challenge tag  $\mathcal{T}_c$  will be accepted with overwhelming probability due to the fact that the calculation of  $r_1$  is independent on  $r_2$ , whereas in the case of  $b = 0$ ,  $\mathcal{T}_c$  will be rejected definitely. This means the counterexample is not secure under the  $\text{unp}^\tau$ -privacy model.

### 4.1. Relation between $\text{unp}^\tau$ -privacy and Ind-privacy

Before studying the relationship between  $\text{unp}^\tau$ -privacy and ind-privacy, we first construct a variant of ind-privacy, named  $\text{ind}^*$ -privacy, which will be proved to equal ind-privacy and acts as a "bridge" that will be used for making the formal security proof.

#### 4.1.1. $\text{Ind}^*$ -privacy

The  $\text{ind}^*$ -privacy experiment is briefly depicted in Fig. 7. It is obvious that the  $\text{ind}^*$ -privacy experiment is the same as the ind-privacy experiment except that in the  $\text{ind}^*$ -privacy game, the adversary  $\mathcal{A}$  can only enquire oracles on the challenge tag  $\mathcal{T}_c$  in the guess phase. In addition, as we have discussed before,  $\mathcal{A}$  can actually observe the protocol results in the ind-privacy experiment. Here, we directly grant the right to query  $O_4$  to  $\mathcal{A}$  in the  $\text{ind}^*$ -privacy experiment. Essentially, the adversary in the ind-privacy has this capability, too.

Let

$$\text{Adv}_{\mathcal{A}}^{\text{ind}^*}[\kappa, n, q, s, u, v, w] = |\Pr[\text{Exp}_{\mathcal{A}}^{\text{ind}^*} = 1] - \frac{1}{2}|.$$

**Definition 8.** An RFID authentication system RAS is said to be  $\text{ind}^*$ -private if for any PPT adversary  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}^{\text{ind}^*}[\kappa, n, q, s, u, v, w]$  is negligible.

#### 4.1.2. $\text{Ind}^*$ -privacy $\iff$ Ind-privacy

We first prove that  $\text{ind}^*$ -privacy is actually identical to ind-privacy. Intuitively, the only difference between these two experiments is that in the guess phase, the adversary in the ind-privacy game is allowed to enquire oracles on all tags including  $\mathcal{T}_c$ , whereas the adversary in the  $\text{ind}^*$ -privacy game is only allowed to enquire oracles on  $\mathcal{T}_c$ . Namely,  $\text{ind}^*$ -privacy is essentially a restricted version of ind-privacy and hence it is trivial to see that ind-privacy implies  $\text{ind}^*$ -privacy. Nevertheless, the adversary in the  $\text{ind}^*$ -privacy game can enquire  $O_5$  on all tags except  $\mathcal{C}$  before the guess phase so that it can get all the secret keys and internal state of tags in  $\mathcal{T}' = \{\mathcal{T} - \mathcal{T}_c\}$  and store them in a list **TagKey-List**. This means that the adversary in the  $\text{ind}^*$ -privacy game has the same power as that of the ind-privacy game.



Experiment  $\text{Exp}_{\mathcal{A}}^{\text{unpr}}[\kappa, n, q, s, u, v, w]$

1. Initialize the RFID system with a reader  $R$  and a set of tags  $\mathcal{T}$  with  $|\mathcal{T}| = n$ ;
2.  $\{\mathcal{T}_c, st\} \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_4, O_5}(R, \mathcal{T})$ ; //learning stage
3.  $b \in_R \{0, 1\}$
4.  $b' \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_4}(R, \mathcal{T}_c, st)$  //guess stage
  - 4.1 When  $\mathcal{A}$  queries  $O_1, O_2, O_3, O_4$  oracles, if  $b=1$ , run the algorithm **ReaderStart, TagCompute, ReaderCompute, Result** respectively, and return the results; the challenger also returns the reaction of the reader  $R$  to  $\mathcal{A}$ , either *accept* or *reject*, when  $O_3$  is queried.
  - 4.2 else  $b=0$ 
    - 4.2.1 when  $\mathcal{A}$  queries  $O_1, O_2$  oracles, pick random elements  $sid, c$  and  $r$  from their respective domains, and return them to  $\mathcal{A}$ ;
    - 4.2.2 when  $\mathcal{A}$  queries  $O_3$ , the challenger compares whether  $r$  is equal to the output of  $O_2(\mathcal{T}_c, sid, c)$ . If yes, the challenger returns a random element  $f$  from its domain, and returns the reader's reaction as *accept*; else it returns a random element  $f$  from its domain and returns the reader's reaction as *reject*;
    - 4.2.3 when  $\mathcal{A}$  queries  $O_4$ , the challenger checks whether  $f$  is equal to the output of  $O_3(sid, c, r)$  and the reaction of the reader for this session  $sid$  is *accept*. If yes, the challenger returns the tag's reaction as *accept*; else it returns the tag's reaction as *reject*;
5. the experiment outputs 1 if  $b' = b$ , 0 otherwise.

Fig. 6. Unpr-privacy experiment.

Experiment  $\text{Exp}_{\mathcal{A}}^{\text{ind}^*}[\kappa, n, q, s, u, v, w]$

1. Initialize the RFID system with a reader  $R$  and a set of tags  $\mathcal{T}$  with  $|\mathcal{T}| = n$ ;
2.  $\{\mathcal{T}_i, \mathcal{T}_j, st\} \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_4, O_5}(R, \mathcal{T})$ ; //learning stage
3. set  $\mathcal{T}' = \mathcal{T} - \{\mathcal{T}_i, \mathcal{T}_j\}$ ;
4.  $b \in_R \{0, 1\}$ ;
5. If  $b=0$ , let  $\mathcal{T}_c = \mathcal{T}_i$ , else  $\mathcal{T}_c = \mathcal{T}_j$ ;
6.  $b' \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_4}(R, \mathcal{T}_c, st)$ ; //guess stage
7. the experiment outputs 1 if  $b' = b$ , 0 otherwise.

Fig. 7. Ind\*-privacy experiment.

**Theorem 2.** *Ind\*-privacy is identical to ind-privacy for an RAS.*

**Proof.** On the one hand, according to our above analyzation, it is trivial to see that  $\text{ind}^*\text{-privacy} \Leftarrow \text{ind-privacy}$ . On the other hand, we will formally prove that  $\text{ind}^*\text{-privacy} \Rightarrow \text{ind-privacy}$ .

Employing the same proof technique of [Theorem 1](#), we first assume that *RAS* is not secure under the ind-privacy model. Namely, a PPT adversary  $\mathcal{A}$  has the ability to pass the ind-privacy game with an advantage of more than  $\epsilon$  within time  $t$ . Then we try to build an algorithm  $\mathcal{B}$  which invokes  $\mathcal{A}$  as a subroutine in order to win the ind\*-privacy game. Due to the condition that *RAS* is ind\*-private, there is supposed to be no PPT adversary that can pass the ind\*-privacy game. Therefore, as long as we can reduce the problem of  $\mathcal{A}$  in the ind-privacy experiment to the problem of  $\mathcal{B}$  in the ind\*-privacy experiment, then the proof is completed. In the following, we illustrate how  $\mathcal{B}$  simulates the ind-privacy game with  $\mathcal{A}$ .

*Simulate the initialization phase* The same as the proof in [Theorem 1](#), except for that in this experiment two candidate challenge tags  $\mathcal{T}_i$  and  $\mathcal{T}_j$  are randomly designated, since the indistinguishability-based privacy model requires the adversary to distinguish two tags.

*Simulate the learning phase.* To simulate the answers of queries  $O_1 \sim O_3$  and  $O_5$  by  $\mathcal{A}$ ,  $\mathcal{B}$  enquires these oracles in the ind\*-privacy game and returns the received responses to  $\mathcal{A}$ . If  $\mathcal{A}$  queries  $O_5$  on  $\mathcal{T}_i$  or  $\mathcal{T}_j$ , then  $\mathcal{B}$  aborts the simulation.

*Simulate the challenge phase.* In the challenge phase,  $\mathcal{A}$  is required to submit two tags  $\mathcal{T}_{c1}, \mathcal{T}_{c2}$  which have not been queried with  $O_5$ . If  $\mathcal{T}_{c1}$  and  $\mathcal{T}_{c2}$  are not the same tags as  $\mathcal{T}_i$  and  $\mathcal{T}_j$ , then  $\mathcal{B}$  aborts the simulation.  $\mathcal{B}$  will also submit  $\mathcal{T}_i$  and  $\mathcal{T}_j$  to the challenger in the ind\*-privacy game, obtain the result: the challenge tag  $\mathcal{T}_c \in \{\mathcal{T}_i, \mathcal{T}_j\}$ , and send  $\mathcal{T}_c$  as the challenge tag to  $\mathcal{A}$ . Next,  $\mathcal{B}$  enquires  $O_5$  on all the tags except  $\mathcal{T}_i$  and  $\mathcal{T}_j$ , and records these results in **TagKey-List**.

*Simulate the guess phase.* To simulate the guess phase, upon  $\mathcal{A}$  enquiring  $O_1 \sim O_3$  and  $O_5$  oracles on  $\mathcal{T}_c$ ,  $\mathcal{B}$  queries the oracles  $O_1 \sim O_3$  in the ind\*-privacy game, and combines the list **TagKey-List** to respond  $\mathcal{A}$ . If  $\mathcal{A}$  queries  $O_5$  on  $\mathcal{T}_c$ , then  $\mathcal{B}$  aborts the simulation.

*Output.* Finally,  $\mathcal{A}$  submits a bit  $b'$  as its output, and meantime  $\mathcal{B}$  also sets  $b'$  as its output.

According to the above description, if the simulation is not aborted by  $\mathcal{B}$  specifically, then it is a perfect one. Note that the simulation will be aborted only if  $\mathcal{A}$  queries  $O_5$  on the candidate challenge tags or submits wrong candidate challenge tags. Thus the probability that the simulation is not aborted can be calculated by  $(1 - \frac{2w}{q+s+u+v+w}) \cdot \frac{2}{n(n-1)}$ . This indicates that if  $\mathcal{A}$  can win the ind-privacy game with the advantage of more than  $\epsilon$ , then  $\mathcal{B}$  can win the ind\*-privacy game with the advantage of more than  $(1 - \frac{2w}{q+s+u+v+w}) \cdot \frac{2\epsilon}{n(n-1)}$ . Moreover, the running time of  $\mathcal{B}$  is approximate to that of  $\mathcal{A}$ . This contradicts the condition that *RAS* is ind\*-private and thus the proof is completed.  $\square$

#### 4.1.3. Unpr-privacy $\Rightarrow$ Ind\*-privacy

**Theorem 3.** *Given an RFID authentication system RAS, if RAS is unpr-private, then it is ind\*-private.*

**Proof.** We first assume that *RAS* is not secure under the ind\*-privacy model. Namely, a PPT adversary  $\mathcal{A}$  has the ability to pass the ind\*-privacy game with an advantage more than  $\epsilon$  within time  $t$ . Then we try to build an algorithm  $\mathcal{B}$  which invokes  $\mathcal{A}$  as a subroutine in order to win the unpr-privacy game. Due to the condition that *RAS* is unpr-private, there is supposed to be no PPT adversary that can pass the unpr-privacy game. Therefore, as long as we can reduce the problem of  $\mathcal{A}$  in the ind\*-privacy game to the problem of  $\mathcal{B}$  in the unpr-privacy game, then the proof is

completed. In the following, we depict how  $\mathcal{B}$  simulates the ind\*-privacy game with  $\mathcal{A}$ .

**Simulate the initialization phase** The same as the proof in [Theorem 2](#).

**Simulate the learning phase.** To simulate the answers of queries  $O_1 \sim O_5$  by  $\mathcal{A}$ ,  $\mathcal{B}$  enquires these oracles in the  $\text{unp}^\tau$ -privacy game and returns the received responses to  $\mathcal{A}$ . If  $\mathcal{A}$  queries  $O_5$  on  $\mathcal{T}_i$  or  $\mathcal{T}_j$ , then  $\mathcal{B}$  aborts the simulation.

**Simulate the challenge phase.** In the challenge phase,  $\mathcal{A}$  is required to submit two tags  $\mathcal{T}_{c1}, \mathcal{T}_{c2}$  which have not been queried with  $O_5$ . If  $\mathcal{T}_{c1}$  and  $\mathcal{T}_{c2}$  are not the same tags as  $\mathcal{T}_i$  and  $\mathcal{T}_j$ , then  $\mathcal{B}$  aborts the simulation.  $\mathcal{B}$  selects a random bit  $b$  to determine the challenge tag  $\mathcal{T}_c = \mathcal{T}_i$  if  $b = 0$  and  $\mathcal{T}_c = \mathcal{T}_j$  otherwise. Next,  $\mathcal{B}$  transmits the challenge tag  $\mathcal{T}_c$  to  $\mathcal{A}$  and also sets  $\mathcal{T}_c$  as its own challenge tag in the  $\text{unp}^\tau$ -privacy game.

**Simulate the guess phase.** Upon  $\mathcal{A}$  enquiring  $O_1 \sim O_4$  oracles on  $\mathcal{T}_c$ ,  $\mathcal{B}$  queries these oracles on  $\mathcal{T}_c$  in the  $\text{unp}^\tau$ -privacy experiment and forwards the received responses to  $\mathcal{A}$ .

**Output.** Finally,  $\mathcal{A}$  submits a bit  $b'$  as its output and meantime  $\mathcal{B}$  outputs 1 if  $b' = b$ , otherwise  $\mathcal{B}$  outputs 0.

According to the above description, if the simulation is not aborted by  $\mathcal{B}$  specifically, then it is a perfect one. The probability that the simulation is not aborted can be calculated by  $(1 - \frac{2w}{q+s+u+v+w}) \cdot \frac{2}{n(n-1)}$ . We will explain why it is a perfect simulation if there is no abortion. Suppose the challenger in the  $\text{unp}^\tau$ -privacy experiment selects a random bit  $b_0$  in the challenge phase. If  $b_0$  is 0,  $\mathcal{T}_c$  is essentially a virtual tag in the perspective of  $\mathcal{A}$  because in this case  $\mathcal{A}$  will always receive random responses upon enquiring  $O_1 \sim O_3$  during the guess phase. Therefore, the probability that  $b' = b$  is  $\frac{1}{2}$ . On the other hand, if  $b_0$  equals 1, the probability that  $b' = b$  becomes  $\frac{1}{2} + \epsilon$ . This indicates that the advantage that  $\mathcal{B}$  wins the  $\text{unp}^\tau$ -privacy experiment is  $|\frac{1}{2} - (\frac{1}{2} + \epsilon)| = \epsilon$ . This is exactly the same advantage as that of  $\mathcal{A}$ . Above all, if  $\mathcal{A}$  can win the ind\*-privacy game with the advantage of more than  $\epsilon$ , then  $\mathcal{B}$  can win the  $\text{unp}^\tau$ -privacy game with the advantage of more than  $(1 - \frac{2w}{q+s+u+v+w}) \cdot \frac{2\epsilon}{n(n-1)}$ . Moreover, the running time of  $\mathcal{B}$  is approximate to that of  $\mathcal{A}$ . This contradicts the condition that RAS is  $\text{unp}^\tau$ -private and thus the proof is completed.  $\square$

#### 4.1.4. $\text{Unp}^\tau$ -privacy $\implies$ Ind-privacy

According to [Theorem 2](#) and [Theorem 3](#), we can directly derive [Theorem 4](#):

**Theorem 4.** Given an RFID authentication system RAS, if RAS is  $\text{unp}^\tau$ -private, then it is ind-private.

#### 4.1.5. $\text{Unp}^\tau$ -privacy $\not\Leftarrow$ Ind-privacy

Intuitively, ind-privacy requires it is hard for the adversary to distinguish two tags according to their transcripts in spite of the distribution of the transcripts, while  $\text{unp}^\tau$ -privacy stipulates that the transcripts should be randomly distributed.

**Theorem 5.** An RFID authentication system RAS with ind-privacy does not imply that it is  $\text{unp}^\tau$ -private.

**Proof.** (sketch). We employ the similar technique with Li et al. [24] and build an RFID authentication system in which the protocol transcripts have format of  $(c, r||r, f)$ . On one hand, in the ind-privacy game, two tags with two different transcripts  $r_1||r_1$  and  $r_2||r_2$  are indistinguishable since  $r_1$  and  $r_2$  are randomly chosen. Thus, the designed RAS is ind-private. On the other hand, in the  $\text{unp}^\tau$ -privacy game, the adversary is required to distinguish whether  $r_1||r_2$  is from a real protocol transcript or randomly selected by the challenger. If they are randomly selected by the challenger, then  $r_1 \neq r_2$  with overwhelming probability; otherwise,

$r_1$  is equivalent to  $r_2$  since this is how the real protocol works. This means that RAS is not secure under the  $\text{unp}^\tau$ -privacy model. Above all, the proof is completed.  $\square$

#### 4.2. Relation between $\text{unp}^\tau$ -privacy and $\text{unp}^*$ -privacy

In [Section 3.3.1](#) we have shown that the counterexample protocol in [Fig. 5](#) is provably secure under the  $\text{unp}^*$ -privacy model but not in the  $\text{unp}^\tau$ -privacy model. This means  $\text{unp}^*$ -privacy does not imply  $\text{unp}^\tau$ -privacy. In the following, we will prove that  $\text{unp}^\tau$ -privacy implies  $\text{unp}^*$ -privacy, which indicates that  $\text{unp}^\tau$ -privacy is stronger than  $\text{unp}^*$ -privacy.

**Theorem 6.** Given an RFID authentication system RAS, if RAS is  $\text{unp}^\tau$ -private, then it is  $\text{unp}^*$ -private.

**Proof.** We first assume that RAS is not secure under the  $\text{unp}^*$ -privacy model. Namely, a PPT adversary  $\mathcal{A}$  has the ability to pass the  $\text{unp}^*$ -privacy game with an advantage of more than  $\epsilon$  within time  $t$ . Then we try to build an algorithm  $\mathcal{B}$  which invokes  $\mathcal{A}$  as a subroutine in order to win the  $\text{unp}^\tau$ -private game. Due to the condition that RAS is  $\text{unp}^\tau$ -private, there is supposed to be no PPT adversary that can pass the  $\text{unp}^\tau$ -privacy game. Therefore, as long as we can reduce the problem of  $\mathcal{A}$  in the  $\text{unp}^*$ -privacy experiment to the problem of  $\mathcal{B}$  in the  $\text{unp}^\tau$ -privacy experiment, then the proof is completed. In the following, we illustrate how  $\mathcal{B}$  simulates the  $\text{unp}^*$ -privacy game with  $\mathcal{A}$ .

**Simulate the initialization phase.** The same as that in [Theorem 1](#).

**Simulate the learning phase.** To simulate the answers of queries  $O_1 \sim O_3$  and  $O_5$  by  $\mathcal{A}$ ,  $\mathcal{B}$  enquires these oracles in the  $\text{unp}^\tau$ -privacy game and returns the received responses to  $\mathcal{A}$ . If  $\mathcal{A}$  enquires  $O_5$  on the tag  $\mathcal{T}_i$ , then  $\mathcal{B}$  aborts the simulation.

**Simulate the challenge phase.** In this phase,  $\mathcal{A}$  is required to submit a challenge tag  $\mathcal{T}_c$  that has not been queried with  $O_5$ .  $\mathcal{B}$  sets  $\mathcal{T}_c$  as the challenge tag in the  $\text{unp}^\tau$ -privacy game, too. If  $\mathcal{T}_c \neq \mathcal{T}_i$ , then  $\mathcal{B}$  aborts the simulation.

**Simulate the guess phase.** Upon  $\mathcal{A}$  enquiring  $O_1 \sim O_3$  oracles on  $\mathcal{T}_c$ ,  $\mathcal{B}$  queries these oracles on  $\mathcal{T}_c$  in the  $\text{unp}^\tau$ -privacy game and returns the received responses to  $\mathcal{A}$ .

**Output.** Finally,  $\mathcal{A}$  submits a bit  $b'$  as its output, and meantime  $\mathcal{B}$  also sets  $b'$  as its output.

If the simulation is not aborted by  $\mathcal{B}$  specifically, then it is a perfect one. The probability that the simulation is not aborted can be calculated by  $(1 - \frac{w}{q+s+u+v+w}) \cdot \frac{1}{n}$ . This indicates that if  $\mathcal{A}$  can win the  $\text{unp}^*$ -privacy game with the advantage of more than  $\epsilon$ , then  $\mathcal{B}$  can win the  $\text{unp}^\tau$ -privacy game with the advantage of more than  $(1 - \frac{w}{q+s+u+v+w}) \cdot \frac{\epsilon}{n}$ . Moreover, the running time of  $\mathcal{B}$  is approximate to that of  $\mathcal{A}$ . This contradicts the condition that RAS is  $\text{unp}^\tau$ -private. And thus the proof is completed.  $\square$

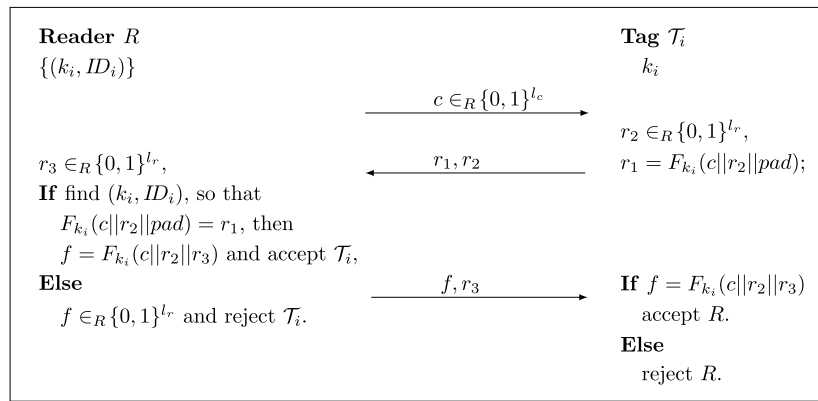
By far, we have studied the relationship among all ind-privacy,  $\text{unp}^*$ -privacy and  $\text{unp}^\tau$ -privacy. According to these work, we can get the claim:

**Claim 2.**  $\text{Unp}^\tau$ -privacy is stronger than both  $\text{unp}^*$ -privacy and ind-privacy.

### 5. Our new RFID authentication protocol

Now we design a new RFID mutual authentication protocol with  $\text{unp}^\tau$ -privacy as shown in [Fig. 8](#).  $F$  is the same PRF family as in the counterexample and  $pad \in \{0, 1\}^{l_{pad}}$  is a padding so that  $l_c + l_r + l_{pad} = l_d$ . The protocol works as follows depicted in [Fig. 8](#).

- (1) The reader  $R$  randomly produces a challenge  $c$  and sends it to the tag  $\mathcal{T}_i$ .



**Fig. 8.** Our new RFID mutual authentication protocol with  $\text{unp}^\tau$ -privacy.

- (2) The tag randomly generates a string  $r_2 \in \{0, 1\}^{l_r}$ , calculates  $r_1$ , and returns  $r_1, r_2$  to the reader.
- (3) Upon receiving the response from the tag, the reader calculates and compares to find the matching tag according to the information stored in the database.
- (4) The final message from the reader will be verified by the tag. If the message is valid, the tag will accept the reader; otherwise, the reader will be rejected.

**Theorem 7.** *The mutual authentication protocol in Fig. 8 is  $\text{unp}^\tau$ -private, given that the function family  $F : \{0, 1\}^k \times \{0, 1\}^{ld} \rightarrow \{0, 1\}^{l_r}$  is a PRF family.*

**Proof.** The proof is similar with that in Theorem 1. We first assume that the authentication protocol in Fig. 8 is not  $\text{unp}^\tau$ -private. Namely, a PPT adversary  $\mathcal{A}$  has the ability to pass the  $\text{unp}^\tau$ -privacy game with an advantage of more than  $\epsilon$  within time  $t$ . Then we try to build an algorithm  $\mathcal{B}$  which invokes  $\mathcal{A}$  in order to win the PTT game. Due to the condition that  $F$  is a secure PRF family, there is supposed to be no PPT adversary that can pass the PTT game. Therefore, as long as we can reduce the problem of  $\mathcal{A}$  in the  $\text{unp}^\tau$ -privacy experiment to the problem of  $\mathcal{B}$  in PTT experiment, then the proof is completed. In the following, we depict how  $\mathcal{B}$  simulates the  $\text{unp}^\tau$ -privacy game with  $\mathcal{A}$ .

*Simulate the initialization phase.* The same as the proof in Theorem 1, except for that in this simulation there is no  $\text{ctr}_i$  and  $s_i$ .

*Simulate the learning phase.* To simulate answers of queries  $O_1 \sim O_5$  by  $\mathcal{A}$ ,  $\mathcal{B}$  enquires  $O_f$  in PTT experiment game and utilizes the keys  $\{k_j\}_{1 \leq j \leq n, j \neq i}$  to respond. If  $\mathcal{A}$  enquires  $O_5$  on  $\mathcal{T}_i$ , then  $\mathcal{B}$  aborts the simulation.

*Simulate the challenge phase.*  $\mathcal{A}$  is required to submit a challenge tag  $\mathcal{T}_c$  that has not been queried with  $O_5$ . If  $\mathcal{T}_c \neq \mathcal{T}_i$ , then  $\mathcal{B}$  aborts the simulation.

*Simulate the guess phase.* To simulate the guess phase,  $\mathcal{B}$  utilizes  $O_f$  query in the PTT game and the secret keys  $\{k_j\}_{1 \leq j \leq n, j \neq i}$  to respond the queries of  $O_1 \sim O_4$  on  $\mathcal{T}_c$  by  $\mathcal{A}$  as shown in the following steps.

- ① Upon  $\mathcal{A}$  enquiring  $O_1$ ,  $\mathcal{B}$  randomly generates a session identifier  $sid$  and a challenge  $c$  and returns  $(sid, c)$ .
- ② Upon  $\mathcal{A}$  enquiring  $O_2$ ,  $\mathcal{B}$  randomly generates  $r_2 \in_R \{0, 1\}^{l_r}$ , and queries  $O_f$  with the input of  $x = c||r_2||pad$ , obtaining the result  $y$  which is assigning to  $r_1$ . Finally,  $\mathcal{B}$  sends  $(r_1, r_2)$  to  $\mathcal{A}$ .
- ③ Upon  $\mathcal{A}$  enquiring  $O_3$ ,  $\mathcal{B}$  selects a random string  $r_3 \in_R \{0, 1\}^{l_r}$ , queries  $O_f$  with input of  $c||r_2||r_3$ , and obtains the result  $f$ . Then it sends  $f$  and  $r_3$ , as well as the reaction of the reader  $R$  to  $\mathcal{A}$ . Note that in order to obtain the reaction of  $R$ ,  $\mathcal{B}$  also queries  $O_f$  with input of  $x = c||r_2||pad$ , and compares the answer returned by  $O_f$  with the value provided by the adversary  $\mathcal{A}$

in the query. If they are equal, then  $\mathcal{B}$  returns the reaction of  $R$  as ‘accept’, else, it returns ‘reject’.

- ④ Upon  $\mathcal{A}$  enquiring  $O_4$ ,  $\mathcal{B}$  queries  $O_f$  with input of  $c||r_2||r_3$  and compares the answer returned by  $O_f$  with the value provided by the adversary  $\mathcal{A}$  in the query, and whether the reaction of  $R$  is ‘accept’ for this session. If both of the checking results are yes, then it returns ‘accept’ as the reaction of  $\mathcal{T}_i$ , else it returns ‘reject’.

*Output.* Finally,  $\mathcal{A}$  submits a bit  $b'$  as its output, and meantime  $\mathcal{B}$  also sets  $b'$  as its output.

We can see that when  $O_f = RF$ , then the simulation is identical to the experiment with  $b = 0$ ; otherwise, if  $O_f = F_{k_i}$ , then the simulation is identical to the experiment with  $b = 1$  except for a little difference that in the experiment the challenger will not check the reaction of  $R$  when answering the query of  $O_4$  from  $\mathcal{A}$ . Nevertheless, we can show that this difference is negligible. The only difference that the adversary  $\mathcal{A}$  may observe is: upon receiving  $O_4$  from  $\mathcal{A}$ , in the simulated game, if  $O_3$  outputs ‘reject’, then  $O_4$  will always output ‘reject’; while in the real experiment, if  $O_3$  outputs ‘reject’, then  $O_4$  may output ‘accept’ if and only if  $\mathcal{A}$  is able to forge a valid input for  $O_4$ . It is obvious that the difference between the real game and the simulated game is negligible since the probability for the adversary to forge a valid reply  $f$  is negligible.

Therefore, if the simulation is not aborted by  $\mathcal{B}$  specifically, then it is a perfect one. The probability that the simulation is not aborted can be calculated by  $(1 - \frac{w}{q+s+u+v+w}) \cdot \frac{1}{n}$ . This indicates that if  $\mathcal{A}$  can win the  $\text{unp}^\tau$ -privacy game with the advantage of more than  $\epsilon$ , then  $\mathcal{B}$  can win the PTT game with the advantage of more than  $(1 - \frac{w}{q+s+u+v+w}) \cdot \frac{\epsilon}{n}$ . Moreover, the running time of  $\mathcal{B}$  is approximate to that of  $\mathcal{A}$ . This contradicts the condition that  $F$  is a PRF family and thus the proof is completed.  $\square$

## 6. Relation between $\text{unp}^\tau$ -privacy and MA model

By far, when we talk about an RFID authentication system RAS, we assume that RAS is sound, which means given a three round protocol  $\mathcal{P}$ , we presume  $\mathcal{P}$  provides mutual authentication. Now, we want to eliminate these preconditions. Intuitively, we expect that given any protocol  $\mathcal{P}$ , if it satisfies our proposed  $\text{unp}^\tau$ -privacy model, then it must provide mutual authentication. This offers us a reference to design a mutual authentication protocol with tag privacy. In order to achieve this, we first construct a general model for mutual authentication and then we will explore the relationship between the  $\text{unp}^\tau$ -privacy model and the mutual authentication model.

Experiment  $\text{Exp}_{\mathcal{A}}^{MA}[\kappa, n, q, s, u, v, w]$

1. Initialize the RFID system with a reader  $R$  and a set of tags  $\mathcal{T}$  with  $|\mathcal{T}| = n$ ;
2.  $\{\mathcal{T}_c, st\} \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_4, O_5}(R, \mathcal{T})$ ;
3.  $\{(c_{sid}, r_{sid}, f_{sid})\} \leftarrow \mathcal{A}^{O_1, O_2, O_3, O_4}(R, st, \mathcal{T}_c)$ ;
4. The experiment outputs 1 if the reader  $R$  accepts  $\mathcal{T}_c$  in a session  $sid$  whose transcript is  $(c_{sid}, r_{sid}, f_{sid})$  and  $r_{sid}$  is not in the returned values of  $O_2$  in session  $sid$ , or if  $\mathcal{T}_c$  accepts  $R$  in a session  $sid$  whose transcript is  $(c_{sid}, r_{sid}, f_{sid})$  and  $f_{sid}$  is not in the returned values of  $O_3$  in session  $sid$ ; otherwise, the experiment outputs 0.

Fig. 9. Mutual authentication model.

### 6.1. Mutual authentication model: MA

The MA experiment is briefly depicted in Fig. 9. At the beginning, a reader and  $n$  tags are set up with the system parameters. During the learning phase, the adversary  $\mathcal{A}$  is allowed to query  $O_1 \sim O_5$  oracles within  $q, s, u, v$  and  $w$  times in total, respectively. Then  $\mathcal{A}$  is required to choose a challenge tag  $\mathcal{T}_c$  that has not been queried with  $O_5$ . Then in the challenge phase,  $\mathcal{A}$  is required to generate a new transcript tuple  $(c_{sid}, r_{sid}, f_{sid})$ . Meantime,  $\mathcal{A}$  can issue  $O_1 \sim O_4$  oracle queries within  $q, s, u, v$  times in total, respectively. The experiment outputs 1 if the reader  $R$  accepts  $\mathcal{T}_c$  in a session  $sid$  whose transcript is  $(c_{sid}, r_{sid}, f_{sid})$  and  $r_{sid}$  is not in the returned values of  $O_2$  in session  $sid$ , or if  $\mathcal{T}_c$  accepts  $R$  in a session  $sid$  whose transcript is  $(c_{sid}, r_{sid}, f_{sid})$  and  $f_{sid}$  is not in the returned values of  $O_3$  in session  $sid$ ; otherwise, the experiment outputs 0. We use  $\text{Exp}_{\mathcal{A}}^{MA}$  to represent the MA experiment. Let

$$\text{Adv}_{\mathcal{A}}^{MA}[\kappa, n, q, s, u, v, w] = \Pr[\text{Exp}_{\mathcal{A}}^{MA} = 1]$$

**Definition 9.** Given any mutual authentication protocol  $\mathcal{P}$ ,  $\mathcal{P}$  is said to be MA-secure if for any PPT adversary  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}^{MA}[\kappa, n, q, s, u, v, w]$  for  $\mathcal{P}$  is negligible.

### 6.2. $\text{Unp}^{\tau}$ -privacy $\implies$ MA

In the MA experiment, if any adversary  $\mathcal{A}$  can forge a valid response  $r$  or  $f$  without querying for them from the oracles  $O_2$  or  $O_3$  respectively, then  $\mathcal{A}$  can win the game. While if  $\mathcal{A}$  can win the MA game, then it can also win the  $\text{unp}^{\tau}$ -privacy game. This is because  $\mathcal{A}$  can forge a valid  $r$  or  $f$ , and observe the reactions of the reader and the tag. Take the reader's reaction for example,  $\mathcal{A}$  first forges a valid  $r$ , and then queries  $O_3$  to get the reaction of the reader. If the reader outputs 'accept' then it indicates the random bit  $b$  selected by the challenger in the  $\text{unp}^{\tau}$ -privacy game is 1; otherwise, it means  $b = 0$ , since when  $b = 0$ , the challenger compares whether  $r$  is equal to the output of  $O_2$  according to the  $\text{unp}^{\tau}$ -privacy experiment. Since  $\mathcal{A}$  has never queried  $O_2$  for  $r$ , the forged  $r$  is different from any outputs of  $O_2$  with an overwhelming probability, which means the reader will reject the tag with an overwhelming probability. Therefore, the adversary  $\mathcal{A}$  can distinguish  $b = 0$  or  $b = 1$ , which means  $\mathcal{A}$  can also win the  $\text{unp}^{\tau}$ -privacy game. In the following, we will give a theorem and prove it formally.

**Theorem 8.** Given any mutual authentication protocol  $\mathcal{P}$ , if  $\mathcal{P}$  satisfies the  $\text{unp}^{\tau}$ -privacy model, then it satisfies the MA-model, too.

**Proof.** We first assume that  $\mathcal{P}$  is not MA-secure. Namely, a PPT adversary  $\mathcal{A}$  has the ability to pass the MA game with an advantage of more than  $\epsilon$  within time  $t$ . Then we try to build an algorithm

$\mathcal{B}$  which invokes  $\mathcal{A}$  in order to win the  $\text{unp}^{\tau}$ -privacy game. Due to the condition that  $\mathcal{P}$  is  $\text{unp}^{\tau}$ -private, there is supposed to be no PPT adversary that can pass the  $\text{unp}^{\tau}$ -privacy game. Therefore, as long as we can reduce the problem of  $\mathcal{A}$  in the MA game to the problem of  $\mathcal{B}$  in the  $\text{unp}^{\tau}$ -privacy game, then the proof is completed. In the following, we depict how  $\mathcal{B}$  simulates the MA game with  $\mathcal{A}$ .

*Simulate the initialization phase.* To simulate the setup phase,  $\mathcal{B}$  randomly chooses an index  $i \in [1, n]$  that will be considered as the index of the challenge tag. Note that tag  $\mathcal{T}_i$ 's secret key  $k_i$  is set up implicitly, i.e.,  $\mathcal{B}$  has no idea of  $k_i$ . For the secret keys of the rest  $n - 1$  tags in  $\{\mathcal{T} - \mathcal{T}_i\}$ , they are randomly generated by  $\mathcal{B}$  according to the secret key space.

*Simulate the learning phase.* Upon  $\mathcal{A}$  enquiring  $O_1 \sim O_5$  oracles,  $\mathcal{B}$  queries these oracles in the  $\text{unp}^{\tau}$ -privacy game and forwards the received responses to  $\mathcal{A}$ . If  $\mathcal{A}$  queries  $O_5$  on  $\mathcal{T}_i$ , then  $\mathcal{B}$  aborts the simulation. After learning,  $\mathcal{A}$  outputs the challenge tag  $\mathcal{T}_c$  which has not been queried with  $O_5$ ,  $\mathcal{B}$  also sets  $\mathcal{T}_c$  as its own challenge tag in the  $\text{unp}^{\tau}$ -privacy experiment. If  $\mathcal{T}_c$  is not  $\mathcal{T}_i$ ,  $\mathcal{B}$  aborts the simulation.

*Simulate the challenge phase.* Upon  $\mathcal{A}$  enquiring  $O_1 \sim O_4$  on  $\mathcal{T}_c$ ,  $\mathcal{B}$  queries these oracles on  $\mathcal{T}_c$  in the  $\text{unp}^{\tau}$ -privacy game and forwards the received responses to  $\mathcal{A}$ .

*Output.* Finally,  $\mathcal{A}$  outputs a tuple  $(c_{sid}, r_{sid}, f_{sid})$ .  $\mathcal{B}$  checks whether  $R$  accepts  $\mathcal{T}_c$  and  $r_{sid}$  is not in the returned values of  $O_2$  in session  $sid$ , or  $\mathcal{T}_c$  accepts  $R$  and  $f_{sid}$  is not in the returned values of  $O_3$ . If yes,  $\mathcal{B}$  outputs 1; otherwise it outputs 0.

We can see that if the simulation is not aborted by  $\mathcal{B}$  specifically, then it is a perfect one. Now we will explain why  $\mathcal{B}$  can win the  $\text{unp}^{\tau}$ -privacy game if  $\mathcal{A}$  can win the MA game. Let  $b_0$  be the random bit selected in the  $\text{unp}^{\tau}$ -privacy experiment. Let  $\text{Adv}_{\mathcal{B}}$  be the advantage of  $\mathcal{B}$  in the  $\text{unp}^{\tau}$ -privacy experiment in the case that the simulation is not aborted. According to the definition of  $\text{unp}^{\tau}$ -privacy, we have

$$\begin{aligned} \text{Adv}_{\mathcal{B}} &= P_r[\mathcal{B} \text{ wins the } \text{unp}^{\tau}\text{-privacy game}] - \frac{1}{2} \\ &= P_r[\mathcal{B} \text{ outputs } 1 | b_0 = 1] P_r[b_0 = 1] \\ &\quad + P_r[\mathcal{B} \text{ outputs } 0 | b_0 = 0] P_r[b_0 = 0] - \frac{1}{2} \\ &= \frac{1}{2} P_r[\mathcal{B} \text{ outputs } 1 | b_0 = 1] \\ &\quad + \frac{1}{2} (1 - P_r[\mathcal{B} \text{ outputs } 1 | b_0 = 0]) - \frac{1}{2} \\ &= \frac{1}{2} (P_r[\mathcal{B} \text{ outputs } 1 | b_0 = 1] - P_r[\mathcal{B} \text{ outputs } 1 | b_0 = 0]) \\ &= \frac{1}{2} (\epsilon - P_r[\mathcal{B} \text{ outputs } 1 | b_0 = 0]) \end{aligned}$$

When  $b_0 = 0$ , the outputs of  $O_2$  are random strings, and  $O_3$  will output 'accept' only when  $r_{sid}$  is equal to the output of  $O_2$  in session  $sid$  according to the  $\text{unp}^{\tau}$ -privacy experiment for  $b_0 = 0$ . Then the probability that " $O_2$  has never been queried in session  $sid$  (that is,  $r_{sid}$  is not in the returned values of  $O_2$  in session  $sid$ ), but  $r_{sid}$  provided by  $\mathcal{A}$  is equal to the output of  $O_2$ " is  $(\frac{1}{2})^{l_r}$  (assume the length of  $r_{sid}$  is  $l_r$ ). By a union bound, the probability that such an event happens in any session is at most  $\frac{s}{2^{l_r}}$ , where  $s$  is the number of  $O_2$  queries allowed in the MA experiment.

Similarly, the probability that " $O_3$  has never been queried in session  $sid$  but  $f_{sid}$  provided by  $\mathcal{A}$  is equal to the output of  $O_3$ " is  $(\frac{1}{2})^{l_f}$  (assume the length of  $f_{sid}$  is  $l_f$ ) and by a union bound, the probability that such an event happens in any session is at most  $\frac{u}{2^{l_f}}$ , where  $u$  is the number of  $O_3$  queries allowed in the MA experiment.

Now, we can obtain  $P_r[\mathcal{B} \text{ outputs } 1 | b_0 = 0] = \frac{s}{2^{l_r}} + \frac{u}{2^{l_f}}$ . Since  $s, u, l_r, l_f$  are polynomial in the secret key  $k$  (in general,  $l_r$  and  $l_f$  are several times longer than  $k$  in bit string form),  $P_r[\mathcal{B} \text{ outputs } 1 | b_0 = 0]$  is negligible. Therefore, if  $\epsilon$  is non-negligible, then the advantage

of  $\mathcal{B}$ , i.e.  $\mathbf{Adv}_{\mathcal{B}} = \frac{1}{2}(\epsilon - (\frac{s}{2f_r} + \frac{u}{2f_f}))$ , is also non-negligible. Above all, if we consider the case that the simulation could be aborted, then the final advantage of  $\mathcal{B}$  become  $(1 - \frac{w}{q+s+u+v+w}) \cdot \frac{1}{n} \cdot \mathbf{Adv}_{\mathcal{B}}$ , which is also non-negligible. Moreover, the running time of  $\mathcal{B}$  is approximate to that of  $\mathcal{A}$ . Thus the proof is completed.  $\square$

## 7. Conclusion

In this paper, we reviewed un $p^*$ -privacy and showed that it cannot capture a new practical attack. At the meantime, we re-investigated the relationship between un $p^*$ -privacy and ind-privacy and proved that un $p^*$ -privacy is not comparable with ind-privacy. Then we presented a new unpredictability-based privacy model: un $p^r$ -privacy which can handle the above mentioned practical attacks and we revisited the relations among ind-privacy, un $p^*$ -privacy and un $p^r$ -privacy. Then we proposed a mutual authentication protocol and proved its security under the un $p^r$ -privacy model. Finally, we constructed a new mutual authentication model  $MA$  and proved that un $p^r$ -privacy implies  $MA$ . This gives us a reference to design a secure RFID mutual authentication protocol with tag privacy.

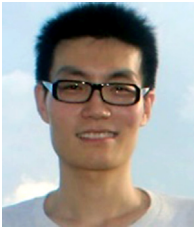
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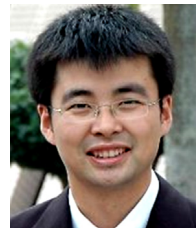


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