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#### Citation

Li, Li and SUN, Jun. Automated verification of timed security protocols with clock drift. (2016). *Proceedings of the 21st International Symposium Limassol, Cyprus, 2016 November 9–11*. 9995, 513-530.

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# Automated Verification of Timed Security Protocols with Clock Drift

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**Abstract.** Time is frequently used in security protocols to provide better security. For instance, critical credentials often have limited lifetime which improves the security against brute-force attacks. However, it is challenging to correctly use time in protocol design, due to the existence of clock drift in practice. In this work, we develop a systematic method to formally specify as well as automatically verify timed security protocols with clock drift. We first extend the previously proposed *timed applied  $\pi$ -calculus* as a formal specification language for timed protocols with clock drift. Then, we define its formal semantics based on *timed logic rules*, which facilitates efficient verification against various security properties. Clock drift is encoded as parameters in the rules. The verification result shows the constraints associated with clock drift that are required for the security of the protocol, e.g., the maximum drift should be less than some constant. We evaluate our method with multiple timed security protocols. We find a time-related security threat in the TESLA protocol, a complex time-related broadcast protocol for lossy channels, when the clocks used by different protocol participants do not share the same clock rate.

## 1 Introduction

Time is essential in cyber-security, e.g., message transmissions and user authentications are often required to be finished in a timely manner. In order to check the relevant timing requirements, *timestamps* are constructed from *clocks*, sent through networks and checked by participants in security protocols. For example, in order to deliver a message  $m$  timely, the sender first attaches its current clock reading  $t_s$  to  $m$  and sends them in a secure way. Then, when the receiver obtains  $t_s$  and  $m$ , it checks  $t_s$  against its own clock reading  $t_r$  with  $t_r - t_s \leq p$  to ensure that  $m$  is received within a certain timing threshold  $p$ . In the above example, the untimed security ( $m$  is not tampered, replayed nor disclosed) and the timed security ( $m$  is delivered in time) are equally important. Given a timed protocol, existing literatures [12, 16] focus on checking its security when the clocks of different protocol participants are fully synchronized. However, in practice,

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J. Sun—The project is supported by the NRF Project IGDSi1305012 in SUTD.

timestamps are often generated and checked based on different local clocks without perfect synchronization, which could compromise the security proved based on the assumption of perfect clock synchronization. Hence, this work studies the security of timed protocols with the present of the clock drift.

Clock drift commonly exists in practice. For instance, in sensor networks, cheap sensors usually do not have enough resources to maintain accurate clock rate and precise clock reading. Hence, small clock drift should be expected and considered in their applications. Even though the local clocks can be synchronized at runtime over the network, various unavoidable factors, e.g., network delay, traffic congestion, can lead to a certain level of inaccuracy. Furthermore, when attackers are present in the network, they may attack the clock synchronization protocol [23]. In such a case, the local clocks under the attack may have large clock drift. As a result, when the security depends on the clock reading, the protocol should provide counter-measures for the clock drift.

Clock drift can cause insecurity of timed protocols because the protocol participants rely on local clocks in practice, whereas the security protocol is designed based on the global clock. For instance, in the above message transmission example, let  $t'_s$  and  $t'_r$  be the readings of the global clock when  $t_s$  and  $t_r$  are read from the local clocks respectively. The receiver deems the message as timely by checking  $t_r - t_s \leq p$ . However, the security property requires  $t'_r - t'_s \leq p$  to ensure a timely message transmission. In order to capture the inconsistency between local clocks and the (fictional) global clock, we first extend *timed applied  $\pi$ -calculus* [16] to formally specify clock drift in protocol models. Then, we define the semantics of the local clocks in Sect. 4, which captures their relationship to the global clock. By using this semantics, we can answer the following two security questions. First, our work can check whether a protocol is secure with the presence of clock drift. More importantly, our work can find out how much clock drift can be tolerated in a timed security protocol. We extend SPA, a verification tool we developed in [15, 16], with the new calculus and semantics for clock drift. In this work, we use a corrected version [12] of Wide Mouthed Frog [7] as a running example to illustrate our specification and verification method. We apply our method to a number of timed security protocols and successfully find a security threat in TESLA [21, 22] in Sect. 5.2, a complex time-related broadcast protocol for lossy channels, when the clocks used by different protocol participants do not share the same clock rate.

## 2 Specification

In this section, we first introduce CWMF [12], a *corrected* version of Wide Mouthed Frog [7] protocol, as a running example. When the local clocks of the protocol participants in CWMF are assumed to be perfectly synchronized, CWMF can be verified as secure [12, 14]. The verification proves that a secret session key can be established among its participants within a certain time. However, it is unclear whether clock drift, which is unavoidable in practice, would compromise the security of CWMF. In the following, we first present CWMF in details and then demonstrate how *timed applied  $\pi$ -calculus*, extended with local clocks, can be used to model such protocols.

## 2.1 Corrected Wide Mouthed Frog

CWMF is designed to establish a timely fresh session key  $k$  from an initiator  $A$  to a responder  $B$  through a server  $S$ . In CWMF, whenever a message is received, the receiver checks the message freshness before accepting it. To be general, we use a parameter  $p_m$  to represent the maximum message lifetime. Additionally, we consider the minimal network delay as a parameter  $p_n$ . Since  $p_n$  is a timing parameter related to the network environment, it is not directly used in the protocol specification. Instead, it is a compulsory delay that applies to all of the network transmissions.

CWMF is a key exchange protocol that involves three participants: an initiator  $A$ , a responder  $B$  and a server  $S$ . By assumption,  $A$  and  $B$  have registered their secret long-term keys at the server respectively. The registered key of a user  $u$  is written as  $key(u)$ , which is used to encrypt all network communications between the user and the server. Whenever a message  $m$  is transmitted between a user  $u$  and the server  $S$ , the message  $m$  is encrypted by the symmetric encryption function  $enc_s$  written as  $enc_s(m, key(u))$ . CWMF then can be described as the following three steps.

- (1)  $A$  generates a random session key  $k$  at its local time  $t_a$   
 $A \rightarrow S : \langle A, enc_s(\langle t_a, B, k, tag_1 \rangle, key(A)) \rangle$
- (2)  $S$  receives the request from  $A$  at its local time  $t_s$   
 $S$  checks :  $t_s - t_a \leq p_m$   
 $S \rightarrow B : enc_s(\langle t_s, A, k, tag_2 \rangle, key(B))$
- (3)  $B$  receives the message from  $S$  at its local time  $t_b$   
 $B$  checks :  $t_b - t_s \leq p_m$   
 $B$  accepts the session key  $k$

First,  $A$  generates a fresh key  $k$  at its local time  $t_a$  and initiates the CWMF protocol with  $B$  by sending its name  $A$  and the request  $\langle t_a, B, k, tag_1 \rangle$  encrypted by  $key(A)$  to  $S$ . Second, after receiving the request from  $A$  at  $S$ 's local time  $t_s$ ,  $S$  ensures the message freshness by checking  $t_s - t_a \leq p_m$ . Then,  $S$  accepts  $A$ 's request by forwarding the request  $\langle t_s, A, k, tag_2 \rangle$  encrypted by  $key(B)$  to  $B$ . It informs  $B$  that  $S$  receives a request from  $A$  at its local time  $t_s$  to communicate with  $B$  using the key  $k$ .  $tag_1$  and  $tag_2$  are two constants that are used to distinguish these two messages. CWMF uses them to prevent the reflection attack [18] in the original Wide Mouthed Frog protocol [7]. Third,  $B$  checks the message freshness again and accepts the request from  $A$  if the message is received in a timely fashion. All of the transmitted messages are encrypted under the users' long-term keys that are pre-registered at  $S$ .

## 2.2 Timed Applied $\pi$ -calculus

*Timed applied  $\pi$ -calculus* works as a specification language for timed protocols. It is essentially the calculus proposed in [2, 16] with the extensions of local clocks and clock drift. Table 1 presents its syntax with the extensions highlighted in the **bold** font.

**Table 1.** Syntax of timed applied  $\pi$ -calculus

Type	Expression	
Message ( $m$ )	$f(m_1, m_2, \dots, m_n)$ $A, B, C$ $n, k$ $t, t_1, t_i, t_n$ $x, y, z$	(function) (name) (nonce) (timestamp) (variable)
Parameter ( $p$ )	$p, p_1, p_j, p_m$	(parameter)
Clock ( $c$ )	$c, c_1, c_k, c_s$	<b>(clock)</b>
Constraint ( $B$ )	$\mathcal{CS}(t_1, t_2, \dots, t_n, p_1, p_2, \dots, p_m)$	(timing constraint)
Configuration ( $L$ )	$\mathcal{CS}(p_1, p_2, \dots, p_m)$	(parameter relation)
Process ( $P, Q$ )	$0$ $P Q$ $!P$ $\nu n.P$ $\mu t.P$ $\mu t : c.P$ if $m_1 = m_2$ then $P$ [else $Q$ ] <sup>a</sup> if $B$ then $P$ [else $Q$ ] wait $\mu t$ until $B$ then $P$ wait $\mu t : c$ until $B$ then $P$ let $x = f(m_1, \dots)$ then $P$ $\overline{in}(x).P$ $\overline{out}(m).P$ check $m$ in $db$ as unique then $P$ $init(m)@t.P$ $join(m)@t.P$ $accept(m)@t.P$	(null process) (parallel) (replication) (nonce generation) (global clock reading) <b>(local clock reading)</b> (untimed condition) (timed condition) (global timing delay) <b>(local timing delay)</b> (function application) (channel input) (channel output) (replay checking) (initialization claim) (participation claim) (acceptance claim)

<sup>a</sup>The expression with the brackets ‘ $[E]$ ’ means that  $E$  can be omitted.

In *timed applied  $\pi$ -calculus*, we compose *messages* using *functions*, *names*, *nonces*, *variables* and *timestamps*. Functions are generally defined as  $f(m_1, m_2, \dots, m_n) \Rightarrow m @ D$ , where  $f$  is the function name,  $m_1, m_2, \dots, m_n$  are the input messages,  $m$  is the output message and  $D$  is the consumed timing range. When  $m$  is exactly the same as  $f(m_1, m_2, \dots, m_n)$ , we call the function a *constructor*; otherwise, it is a *destructor*. For simplicity, we add some syntactic sugar as follows: (1) when  $D = [0, \infty)$  which is the largest timing range of functions, we omit ‘ $@ D$ ’ in the function definition; (2) for constructors, we omit ‘ $\Rightarrow m$ ’ in the definition. For instance, the symmetric encryption function is defined as  $enc_s(m, k)$ , and its decryption function is defined as  $dec_s(enc_s(m, k), k) \Rightarrow m$ . Names are globally shared strings. Nonces are fresh random numbers. Variables are memory locations for holding messages. Timestamps are clock readings. Additionally, *parameters* are configurable constants (e.g., the maximum message lifetime  $p_m$ ) and persistent settings (e.g., the minimal network latency  $p_n$ ).

In this work, we extend [16] with local clocks. That is, timestamps can be read from these local clocks rather than the shared global clock. For instance, in CWMF, the local clocks of  $A$ ,  $S$  and  $B$  can be declared as  $c_a$ ,  $c_s$  and  $c_b$  respectively. The constraint set  $B = \mathcal{CS}(t_1, \dots, t_n, p_1, \dots, p_m)$  represents a set of linear constraints over timestamps and parameters, which can acts as protocol checking conditions and environment assumptions in the protocol. For instance, given the minimal network latency  $p_n$ , when a message sent at  $t$  is received at  $t'$ , we have  $t' - t \geq p_n$ . Additionally, the configuration  $L = \mathcal{CS}(p_1, \dots, p_m)$  is a set of linear constraints over only parameters that should be satisfied globally. For example, the configuration  $p_n > 0$  should be satisfied because the message transmission delay should stay positive.

As shown in Table 1, processes are defined as follows. ‘0’ is a null process that does nothing. ‘ $P|Q$ ’ is a parallel composition of processes  $P$  and  $Q$ . The replication ‘ $!P$ ’ stands for an infinite parallel composition of process  $P$ , which captures an unbounded number of protocol sessions running in parallel. The nonce generation process ‘ $\nu n.P$ ’ represents that a fresh nonce  $n$  is generated and bound to process  $P$ . The global clock reading process ‘ $\mu t.P$ ’ means that a timestamp  $t$  is read from the global clock and bound to process  $P$ . The local clock reading process ‘ $\mu t : c.P$ ’ similarly means that a timestamp  $t$  is read from a local clock  $c$  and bound to process  $P$ . The checking condition  $cond$  in the ‘if  $cond$  then  $P$  else  $Q$ ’ process has two forms: (1) the untimed condition  $m_1 = m_2$  is a symbolic equivalence checking between two messages; (2) the timed condition  $\mathcal{CS}(t_1, t_2, \dots, t_n, p_1, p_2, \dots, p_m)$  is a constraint over timestamps and parameters. When  $cond$  evaluates to true, process  $P$  is executed; otherwise,  $Q$  is executed. The global timing delay process ‘wait  $\mu t$  until  $B$  then  $P$ ’ means that  $P$  is executed until the reading  $t$  from the global clock satisfies the timing condition  $B$ . Similarly, the local timing delay process ‘wait  $\mu t : c$  until  $B$  then  $P$ ’ means that  $P$  is executed until the reading  $t$  from a local clock  $c$  satisfies the timing condition  $B$ . The function application ‘let  $x = f(m_1, \dots, m_n)$  then  $P$ ’ means if the function  $f$  is applicable to a sequence of messages  $m_1, \dots, m_n$ , its result is bound to the variable  $x$  in process  $P$ . The channel input ‘ $in(x).P$ ’ means that a message, bound to the variable  $x$ , should be received before executing  $P$ . The channel output ‘ $\overline{out}(m).P$ ’ describes that the message  $m$  shall be sent out before executing process  $P$ . The uniqueness checking expression ‘check  $m$  in  $db$  as unique then  $P$ ’ ensures that (1) the value of  $m$  does not exist in a database  $db$  before this expression, and (2)  $m$  is inserted into  $db$  after this expression. The uniqueness checking is particularly useful for preventing replay attacks in practice.

Additionally, the *init*, *join* and *accept* events are introduced to specify the security properties. They represent the initialization, participation and acceptance of the protocol participants respectively according to their roles, which are elaborated in Sect. 3.

**Notations and Definitions.** For simplicity,  $tuple_n(m_1, m_2, \dots, m_n)$  is simply written as  $\langle m_1, m_2, \dots, m_n \rangle$ . A variable  $x$  is bound to a process  $P$  when  $x$  is constructed by the function application process ‘let  $x = f(m_1, \dots)$  then  $P$  else  $Q$ ’ or

the channel input process ‘ $c(x).P$ ’ as shown in Table 1. When a variable  $x$  appears in a process  $P$  while it is not bound to  $P$ , it is a free variable in  $P$ . A process is *closed* when it does not have any free variable. Notice that all of the processes considered in this work are closed. When  $x$  is a tuple in the function application process or the channel input process above, we simply write  $x$  as  $\langle x_1, x_2, \dots, x_n \rangle$ . When we only want to check that a variable  $x_i$  equals to a constant  $C$ , we can replace ‘ $x_i$ ’ with ‘ $=C$ ’ in the above tuple.

**Remarks.** We do not need special syntax to specify private channels in *timed applied  $\pi$ -calculus*. Private channels can be constructed with public channels and unbreakable encryptions. For instance, in order to model a message  $m$  transmitted in a private channel, we first introduce a secret key  $k_s$ . Then, we can model a private channel as  $\overline{out}(enc_s(m, k_s)).P \mid in(x).let m' = dec_s(x, k_s) then Q$ .

### 2.3 CWMF Model

In order to verify CWMF in a hostile environment, we make the following assumptions. (1) The adversary can ask any protocol participant to join the protocol, including  $A$ ,  $S$  and  $B$ . (2) The adversary controls the protocol participation time, e.g., the initialization time of  $A$  in CWMF. (3)  $S$  provides its session key exchange service to all of its registered users. (4) The adversary can register as any user at the server, except for  $A$  and  $B$ . The precise attacker model employed in our work is discussed in Sect. 3. In CWMF, because we are interested in the protocol acceptance between legitimate users, we assume that  $B$  only accepts requests from  $A$ . Additionally, a public channel controlled by the adversary is used in CWMF for network communication.

Before the protocol starts, all of its participants need to register a secret long-term key at the server. We assume that  $A$  and  $B$  have already registered at the server using their names. Hence, the server can generate new keys for any other user (possibly personated by the adversary), which can be modeled as the process  $P_r$  below.

$$P_r \triangleq in(u).if u \neq A \wedge u \neq B then \overline{out}(key(u)).0$$

In CWMF,  $A$  takes a role of the initiator as specified by  $P_a$  below. It first starts the protocol by receiving a responder’s name  $r$  from  $c$ , assuming that  $r$  is specified by the adversary. Then,  $A$  generates a session key  $k$  and reads  $t_a$  from its local clock  $c_a$ . Then,  $A$  emits an *init* event to indicate the protocol initialization with the arguments  $A, r, k$  at  $t_a$ . Finally, the message  $\langle A, enc_s(\langle t_a, r, k, tag_1 \rangle, key(A)) \rangle$  is sent from  $A$  to  $S$ .

$$P_a \triangleq in(r).vk.\mu t_a : c_a.init(A, r, k)@t_a.\overline{out}(\langle A, enc_s(\langle t_a, r, k, tag_1 \rangle, key(A)) \rangle).0$$

As specified by the process  $P_s$ , after  $S$  receives a user’s request as a tuple  $\langle i, x \rangle$ , it records its local time from  $c_s$  as  $t_s$  and decrypts  $x$  using  $key(i)$ . If the decryption is successful, it obtains the initialization time  $t_i$ , the responder’s name  $r$  and the session key  $k$ . When the freshness checking  $t_s - t_i \leq p_m$  is passed,  $S$

then believes that it is participating in a protocol run at time  $t_s$  and engages the *join* event. Later, a new message encrypted by the responder's key, written as  $enc_s(\langle t_s, i, k, tag_2 \rangle, key(r))$ , is sent to the responder over the public channel.

$$P_s \triangleq in(\langle i, x \rangle). \mu t_s : c_s. let \langle t_i, r, k, =tag_1 \rangle = dec_s(x, key(i)) \text{ then} \\ \text{if } t_s - t_i \leq p_m \text{ then } join(i, r, k) @ t_s. \overline{out}(enc_s(\langle t_s, i, k, tag_2 \rangle, key(r))). 0$$

Additionally, as shown in the process  $P_b$ , when  $B$  receives the message from  $S$ ,  $B$  records its local time as  $t_b$  and tries to decrypt request as a tuple of the server's processing time  $t_s$ , the initiator's id  $i$  and the session key  $k$ . If  $i = A$  and the freshness checking  $t_b - t_s \leq p_m$  is passed,  $B$  then believes that the request is sent from  $A$  within  $2 * p_m$  and engages the accept event at time  $t_b$ .

$$P_b \triangleq c(x). \mu t_b : c_b. let \langle t_s, =A, k, =tag_2 \rangle = dec_s(x, key(B)) \text{ then} \\ \text{if } t_b - t_s \leq p_m \text{ then } check \ k \ \text{in} \ db \ \text{as} \ unique \ \text{then} \ accept(A, B, k) @ t_b. 0$$

Finally, we have a process  $P_p \triangleq \bar{c}(A). \bar{c}(B). 0$  that broadcasts the names  $A$  and  $B$ . The overall process  $P \triangleq (!P_r) | (!P_a) | (!P_s) | (!P_b) | (!P_p)$  is a parallel composition of the infinite replications of the five processes described above.

### 3 Timed Security Properties

In this section, we define the timed security properties. Notice that the properties are defined based on the global clocks, whereas the participants in the protocols rely on local clocks in practice. In this work, we focus on the authentication properties, as they can be largely affected by clock drift. We first introduce the adversary model as follows.

**Adversary Model.** We assume that an active attacker exists in the network, whose capabilities are extended from the Dolev-Yao model [13]. The attacker can intercept all communications, compute new messages, generate new nonces and send the messages he obtained. Additionally, he can use all the publicly available functions, e.g., encryption, decryption, concatenation. He can also ask the genuine protocol participants to take part in the protocol at any time. Comparing our attack model with the Dolev-Yao model, reading timestamps from various clocks, attacking weak cryptographic functions and compromising legitimate protocol participants are allowed additionally. A formal definition of the adversary model is defined as follows.

**Definition 1 Adversary Process.** *The adversary is defined as an arbitrary closed timed applied  $\pi$ -calculus process  $K$  which does not emit the init, join and accept events.*

**Timed Authentication.** In a protocol, we often have an initiator who starts the protocol and a responder who accepts the protocol. For instance, in CWMF,  $A$  is the initiator and  $B$  is the responder. Additionally, other entities called partners,



e.g.,  $S$  in CWMF, can be involved during the protocol execution. In general, the protocol authentication aims at establishing common knowledge among the protocol participants when the protocol successfully ends. Specifically, for timed protocols, the common knowledge contains the information on the participants' time.

Since different participants take different roles in the protocol, we introduce the *init*, *accept* and *join* events for the initiator, the responder and the partners respectively. Whenever a protocol participant believes that it is participating in a protocol as a certain role, it engages the corresponding event with the protocol parameters and the correct time. For instance, in CWMF,  $A$  engages *init*( $A, r, k$ )@ $t_a$ ;  $S$  engages *join*( $i, r, k$ )@ $t_s$ ; and  $B$  engages *accept*( $i, B, k$ )@ $t_b$ . We remark that  $t_a$ ,  $t_s$  and  $t_b$  in above events should be the correct readings from the global clock, which could be different from the values used for constructing messages in the protocol.

Based on the *init*, *join* and *accept* events, the protocol authentication properties then can be formally specified as event correspondences. The timed non-injective authentication is satisfied if and only if for every acceptance of the protocol responder, the protocol initiator indeed initiates the protocol and the protocol partners indeed join in the protocol, agreeing on the protocol arguments and timing requirements. We formally define the non-injective timed authentication as follows.

**Definition 2 Non-injective Timed Authentication.** *The non-injective timed authentication, denoted as  $Q_n = \text{accept} \leftarrow [B] \vdash \text{init}, \text{join}_1, \dots, \text{join}_n$ , is satisfied by a closed process  $P$ , if and only if, given the adversary process  $K$ , for every occurrence of an accept event in  $P|K$ , the corresponding init event and join events in  $Q_n$  have occurred before in  $P|K$ , agreeing on the arguments and the timing constraints  $B$ .*

In CWMF, the non-injective timed authentication can be written as

$$Q_n = \text{accept}(i, r, k)@t_r \leftarrow [t_s - t_i \leq \S p_m \\ \wedge t_r - t_s \leq \S p_m] \vdash \text{init}(i, r, k)@t_i, \text{join}(i, r, k)@t_s.$$

The injective timed authentication additionally requires an injective correspondence between the protocol initialization and acceptance comparing with the non-injective timed authentication. Hence, the injective timed authentication, which ensures the infeasibility of replay attack, is strictly stronger than the non-injective one.

**Definition 3 Injective Timed Authentication.** *The injective timed authentication, denoted as  $Q_i = \text{accept} \leftarrow [B] \vdash \text{init}, \text{join}_1, \dots, \text{join}_n$ , is satisfied by a closed process  $P$ , if and only if, (1) the non-injective timed authentication  $Q_n = \text{accept} \leftarrow [B] \vdash \text{init}, \text{join}_1, \dots, \text{join}_n$ , is satisfied by  $P$ ; (2) given the adversary process  $K$ , for every *init* event of  $Q_i$  occurred in  $P|K$ , at most one *accept* event can occur in  $P|K$ , agreeing on the arguments in the events and the constraints  $B$  in global time.*

For simplicity, given a non-injective authentication property  $Q_n = \text{accept} \leftarrow [B] \vdash H$  and its injective version  $Q_i = \text{accept} \leftarrow [B] \rightarrow H$ , we define two functions such that  $\text{inj}(Q_n) = Q_i$  and  $\text{non\_inj}(Q_i) = Q_n$ . Hence, we can write injective timed authentication of CWMF as  $Q_i = \text{inj}(Q_n)$ .

## 4 Semantics of Clock Drift

In this section, we first briefly introduce the *timed logic rules* [16] which are used to capture the semantics of the *timed applied  $\pi$ -calculus*. We use CWMF to demonstrate how *timed logic rules* can be used to capture the semantics of *timed applied  $\pi$ -calculus*. Particularly, we capture the semantics of reading timestamps from local clocks based on two different ways of modeling clock drift. We use these two different semantics to show that our method can be adopted to handle different scenarios in practice. We have implemented these two different clock drift semantics in SPA [16].

**Table 2.** Syntax of Timed Logic Rules

Type	Expression	
Message ( $m$ )	$f(m_1, m_2, \dots, m_n)$ $a[], b[], c[], A[], B[], C[]$ $[n], [k], [N], [K]$ $\mathbb{t}, \mathbb{t}_1, \mathbb{t}_i, \mathbb{t}_n$ $x, y, z, X, Y, Z$	(function) (name) (nonce) (timestamp) (variable)
Parameter ( $p$ )	$\S p$	(parameter)
Constraint ( $B$ )	$\mathcal{C}(\mathbb{t}_1, \mathbb{t}_2, \dots, \mathbb{t}_n, \S p_1, \S p_2, \dots, \S p_m)$	(timing relation)
Configuration ( $L$ )	$\mathcal{C}(\S p_1, \S p_2, \dots, \S p_m)$	(parameter config)
Event ( $e$ )	$\text{init}(\star[d], m, \mathbb{t})$ $\text{join}(\star[d], m, \mathbb{t})$ $\text{accept}(\star[d], m, \mathbb{t})$ $\text{know}(\star m, \mathbb{t})$ $\text{new}(\star[n], l[])$ $\text{unique}(\star u, \star l[], m)$	(initialization) (participation) (acceptance) (knowledge) (generation) (uniqueness)
Rule ( $R$ )	$[G] e_1, \dots, e_n \dashv [B] \rightarrow e$	(rule)

### 4.1 Timed Logic Rules

In [16], we proposed the *timed logic rules* to define the semantics of the *timed applied  $\pi$ -calculus* in terms of the adversary capabilities, so timed security protocols can be verified efficiently. In this work, we show how to use them to capture clock drift. When the semantics of calculus processes are represented by logic rules, we need additional notations to differentiate the data types of names, nonces, timestamps, variables and parameters as shown in Table 2.

(1) The syntax of variables and functions are unchanged. (2) Names are appended with a pair of square brackets from  $A$  to  $A[]$ . (3) Nonces are put inside of a pair of square brackets from  $n$  to  $[n]$ . (4) Timestamps are written with a blackboard bold font from  $t$  to  $\mathbb{t}$ . (5) Parameters are prefixed from  $p$  to  $\S p$ .

Generally, each timed logic rule specifies a capability of the adversary in the form of  $[G] e_1, e_2, \dots, e_n \dashv [B] \rightarrow e$ .  $G$  is a set of untimed guards,  $\{e_1, e_2, \dots, e_n\}$  is a set of premise events,  $B$  is a set of timing constraints and  $e$  is a conclusion event. It means that if the untimed guard condition  $G$ , the premise events  $\{e_1, e_2, \dots, e_n\}$  and the timing constraints  $B$  are satisfied, the conclusion event  $e$  is ready to occur. When  $G$  is empty, we simply omit ' $[G]$ ' in the rule.

The events represent the things that can occur in the protocol. In this work, six types of events are essential to the timed protocols with clock drift. Similar to the *timed applied  $\pi$ -calculus*, we have event *init*, *join* and *accept* that signal the authentication claims made by the legitimate protocol participants. In particular, the *init*, *join* events appear in the premise part whereas the *accept* events appear in the conclusion part. We amend the events from  $init(m)@t$ ,  $join(m)@t$  and  $accept(m)@t$  to  $init([d], m, \mathbb{t})$ ,  $join([d], m, \mathbb{t})$  and  $accept([d], m, \mathbb{t})$  respectively. The additional nonce  $[d]$  represents the session id, which is specifically introduced to check the authentication properties.

Additionally,  $know(m, \mathbb{t})$  means that the adversary obtains message  $m$  at time  $\mathbb{t}$ . Because the adversary intercepts all communications over the public channel, for every network input  $in(x)$  at time  $t$ , we add  $know(x, \mathbb{t}')$  satisfying  $\mathbb{t}' \leq \mathbb{t}$  to the rule premises, meaning that the adversary need to know  $x$  before time  $t$  so as to send it at  $t$ ; for every network output  $out(m)$  at time  $t$ , we construct a rule that concludes  $know(m, \mathbb{t}')$  and satisfies  $\mathbb{t}' - \mathbb{t} \geq \S p_n$ , representing  $m$  can be intercepted by the adversary after the network delay  $\S p_n$ . Furthermore, given a nonce generated in  $\nu n.P$ , we add  $new([n], l[])$  to the rule premises, denoting the generation of nonce  $[n]$  at the process location  $l[]$  (we use unique labels to represent different locations in the process). Lastly,  $unique(u, db[], m)$  means that the message  $u$  should have a unique value in a database  $db[]$  (any constant can be a database name). Given the above unique event constructed in a process,  $m$  is an ordered tuple of messages that can be identified by  $\langle u, db[] \rangle$ , consisting of the network inputs, generated nonces and read timestamps in the chronological order until the process ends or its sub-process is an infinite replication process. Unique events and new events are constructed in the following two cases: (1) when 'check  $u$  in  $db$  as unique then  $P$ ' is present in the process,  $unique(u, db[], m)$  is added; (2) given ' $\nu n.P$ ' in the process at the location  $l$ ,  $new(n, l[])$  and  $unique(n, l[], m)$  are added. The location names are generated by a special function  $loc()$ , which returns a unique name to represent the current process location. The semantics of *timed applied  $\pi$ -calculus* is presented in the full paper version [1].

Since we assume that different nonces must have different values, every rule can have at most one *new* event for every single nonce. When two *new* events have the same nonce in a rule, we merge them into a single event. Similarly, we need to merge other events in the following scenarios: *know* events of the same

message; *unique* events with the same unique value and database; *init*, *join* or *accept* events with the same session id. In general, each event is associated with a signature and premise events with the same signatures in a rule should be merged. As shown in Table 2, event signature can be constructed by concatenating its event name with a sequence of messages prefixed by ‘ $\star$ ’. For instance, in the event  $unique(\star u, \star l[], m)$ , the unique value  $u$  and the location  $l[]$  is prefixed by  $\star$ , so its signature is ‘ $unique.u.l[]$ ’, where ‘.’ concatenates the strings.

To provide a better understanding of the timed logic rules, we show three examples without clock drift. Later, we compare them with those rules with clock drift.

*Example 1.* Given that the symmetric encryption function  $enc_s$  is public, the adversary can use it to encrypt messages. In order to use this function, the adversary first needs to know a message  $m$  and a key  $k$ . Then, the encryption function returns the encrypted message  $enc_s(m, k)$ . Hence, the encryption can be represented as the following rule.

$$know(m, \mathbb{t}_1), know(k, \mathbb{t}_2) \text{ -- } [\mathbb{t}_1 \leq \mathbb{t} \wedge \mathbb{t}_2 \leq \mathbb{t}] \text{ -- } know(enc_s(m, k), \mathbb{t}) \quad (1)$$

Notice that the timing constraints means that  $enc_s(m, k)$  can only be known to the adversary after  $m$  and  $k$  are known, following the chronological order.  $\square$

*Example 2.* In CWMF, the server provides its key registration service to the public as  $P_s$ . This service can be captured as follows.

$$[u \neq A[] \wedge u \neq B[]] know(u, \mathbb{t}_1) \text{ -- } [\mathbb{t} - \mathbb{t}_1 \geq \S p_n] \text{ -- } know(key(u), \mathbb{t})$$

It means that anyone can register at the server using any name except  $A$  and  $B$ .  $\square$

*Example 3.* In this example, we demonstrate the *timed logic rule* for  $P_b$  in CWMF, when  $B$  reads the timestamps from the global clock rather than its local clock.  $B$  receives a message  $enc_s(\langle t_s, A, k, tag_2 \rangle, key(B))$  from  $S$ , records its current time as  $t_b$  and claims acceptance if  $t_b - t_s \leq p_m$ . Since the adversary can start the protocol at anytime, we assume that  $t_b$  is specified by the adversary. Then, the *timed logic rule* of  $P_b$  is written as the following rule, where  $m_b = \langle enc_s(\langle t_s, A[], k, tag_2[] \rangle, key(B[])), t_b \rangle$ .

$$\begin{aligned} & unique(k, db[], m_b), new([n_b], l_b[]), unique([n_b], l_b[], m_b), \\ & know(t_b, t_b), know(enc_s(\langle t_s, A[], k, tag_2[] \rangle, key(B[])), t_1) \\ & \text{-- } [\mathbb{t}_1 \leq t_b \wedge t_b - t_s \leq \S p_m] \text{ -- } accept([n_b], \langle A[], B[], k \rangle, t_b) \end{aligned} \quad (2)$$

In Sect. 4.2, we will compare it with the rules explicitly modeling the clock drift.  $\square$

## 4.2 Semantics of Local Clocks

In this work, we additionally introduce the operation  $\mu t : c$  that reads a timestamp  $t$  from a local clock  $c$ . This operation is applicable to the local clock

reading process and the local timing delay process shown in Table 1. In order to capture the semantics of timestamps constructed with  $\mu t : c$  in the calculus, we need to record two timestamps  $\mathbb{t}$  and  $\mathbb{t}_g$  from the local clock  $c$  and the global clock respectively. The semantics of regular operations in protocol execution, e.g., message constructions and guard conditions, is defined based on the local time  $\mathbb{t}$  because they use the real values read from local clocks. However, the semantics of the security claims, i.e., *init*, *join* and *accept* events, should be defined based on the global time  $\mathbb{t}_g$  to indicate the correct timing of event engagement. In this way, we can correctly specify and distinguish two different types of timestamps that are (1) used in the protocol execution and (2) captured by the security properties. Hence, the remaining task is to establish the relation between  $\mathbb{t}$  and  $\mathbb{t}_g$  based on the assumptions of the clock drift. In the following, we show two different ways of modeling clock drift. Notice that, when all of the timestamps are read from the global clock, the *timed logic rules* remain the same as those in [16]. For instance, the *timed logic rules* in Examples 1 and 2 remain the same, while the *timed logic rule* in Example 3 shall be updated to take clock drift into account. In this work, we consider two different scenarios of clock drift: (**VR**) different clocks have different clock rates but concern their maximum drift bounds; (**SR**) different clocks share the same clock rate but have different readings. The differences between VR and SR in the following *time logic rules* are highlighted in the red font.

**Variable Clock Rate (VR).** In VR, we assume that the local clock rate can vary during the protocol execution. That is, local clocks can run faster or slower than the global clock from time to time. Additionally, we assume that their maximum clock drift are bounded, resulting in the following two properties. First, the timestamps read from the same local clock should always be monotonic. For example, given a process  $\mu t_1 : c. \mu t_2 : c. 0$ , we have  $t_1 \leq t_2$ . However, if  $t_1$  and  $t_2$  are read from two different local clocks, e.g.,  $\mu t_1 : c_1. \mu t_2 : c_2. 0$ ,  $t_2$  could be smaller than  $t_1$ . Second, the differences between a local clock and the global clock are always bounded by a maximum drift parameter associated with that local clock. For instance, given a timestamp  $t$  read from  $c$  at global time  $t'$ , we have  $|t - t'| \leq p_c$ , where  $p_c$  is the maximum drift of  $c$ , satisfying  $p_c > 0$ . If VR is assumed, the *timed logic rule* of  $P_b$  can be written as the following rule, where  $m'_b = \langle enc_s(\langle \mathbb{t}_s, A \rangle, k, tag_2 \rangle), key(B) \rangle, \langle \mathbb{t}_b, \mathbb{t}'_b \rangle$ .

$$\begin{aligned} & unique(k, db \square, m'_b), new([n_b], l_b \square), unique([n_b], l_b \square, m'_b), \\ & know(\mathbb{t}_b, \mathbb{t}'_b), know(enc_s(\langle \mathbb{t}_s, A \rangle, k, tag_2 \rangle), key(B \square)), \mathbb{t}_1 \\ & \neg [\mathbb{t}_1 \leq \mathbb{t}'_b \wedge \mathbb{t}_b - \mathbb{t}_s \leq \S p_m \wedge |\mathbb{t}'_b - \mathbb{t}_b| \leq \S p_b] \rightarrow accept([n_b], \langle A \square, B \square, k \rangle, \mathbb{t}'_b) \end{aligned}$$

**Shared Clock Rate (SR).** When the local clocks share the same clock rate of the (correct) global clock, the differences of the readings from different clocks are always the same. In this case, we introduce a clock drift parameter  $d_c$  for each clock  $c$ . Whenever a timestamp  $t$  is read from  $c$  at the global time  $t'$ , we have  $t = t' + d_c$ . Hence, in this case, given the two timestamps extracted from the same local clock, their difference reflects the exact duration of that time period.

For instance, the *timed logic rule* of  $P_b$  can be written the following rule, where  $d_b$  is the clock drift of  $c_b$  and  $m'_b$  is the same as above.

$$\begin{aligned} & \text{unique}(k, db[], m'_b), \text{new}([n_b], l_b[]), \text{unique}([n_b], l_b[], m'_b), \\ & \text{know}(\mathbb{t}_b, \mathbb{t}'_b), \text{know}(\langle \mathbb{t}_s, A[], k, \text{tag}_2[] \rangle, \text{key}(B[])), \mathbb{t}_1) \\ & \neg [\mathbb{t}_1 \leq \mathbb{t}'_b \wedge \mathbb{t}_b - \mathbb{t}_s \leq \S p_m \wedge \mathbb{t}_b - \mathbb{t}'_b = \S d_b] \rightarrow \text{accept}([n_b], \langle A[], B[], k \rangle, \mathbb{t}'_b) \end{aligned}$$

**Comparing VR and SR.** The difference between VR and SR can be illustrated with the calculation of the round-trip delay (RTD) in the Network Time Protocol (NTP). NTP is designed to synchronize the clocks between a client  $A$  and a server  $B$ . In NTP,  $A$  first reads its clock  $c_a$  as  $t_a$  and then sends an authenticated signal to  $B$ . Once  $B$  receives the signal, it reads its clock  $c_b$  as  $t_b$ . After  $B$  verifies the signal successfully,  $B$  reads its clock  $c_b$  as  $t'_b$  and replies another authenticated signal back to  $A$ . Once  $A$  receives the reply signal, it reads its clock  $c_a$  as  $t'_a$ . If the reply signal is correctly verified,  $A$  calculates the RTD as  $\delta = (t'_a - t_a) - (t'_b - t_b)$ . When SR is assumed, the calculation of  $\delta$  is accurate even if clock drift exists. However, when VR is assumed,  $\delta$  is *not* accurate because the distance of clock drift can vary during the protocol execution.

### 4.3 Verification Overview

After obtaining the initial *timed logic rules* from the *timed applied  $\pi$ -calculus* as shown above, the security properties then can be verified using the method proposed in [16]. We briefly introduce the method in the following and refer the readers to [16] for details.

In general, the verification method works by composing all of the existing timed logic rules into new rules, by unifying the conclusion of one rule with the premises of other rules. For instance, we can compose Rule (1) to Rule (2) as the following rule.

$$\begin{aligned} & \text{unique}(k, db[], m'_b), \text{new}([n_b], l_b[]), \text{unique}([n_b], l_b[], m'_b), \\ & \text{know}(\mathbb{t}_b, \mathbb{t}_b), \text{know}(\langle \mathbb{t}_s, A[], k, \text{tag}_2[] \rangle, \mathbb{t}_1), \text{know}(\text{key}(B[]), \mathbb{t}_2) \\ & \neg [\mathbb{t}_1 \leq \mathbb{t}_b \wedge \mathbb{t}_2 \leq \mathbb{t}_b \wedge \mathbb{t}_b - \mathbb{t}_s \leq \S p_m] \rightarrow \text{accept}([n_b], \langle A[], B[], k \rangle, \mathbb{t}_b) \end{aligned}$$

We repeatedly generate new rules until no new rule can be generated. Then, we use the set of all rules to check the authentication properties, ensuring that no violating rule exists and every authentication property is satisfied. When the above two criteria can be met, the result of the verification is a set of configurations (each configuration is a set of constraints over the parameters). We prove that the protocol is guaranteed to satisfy the security property if its parameters choose values from the configurations. Due to the limitation of space, we demonstrate the full verification process of CWMF in the full paper version [1]. Notice that the verification process is not guaranteed to terminate in general. However, it has been shown that it often terminates for practical protocols [5, 14, 15]. After obtaining the secure configurations, we need to additionally ensure that clock

**Table 3.** Experiment results

Protocol	# $\mathcal{R}$	No clock drift		Shared clock rate		Variable clock rate	
		Result	Time	Result	Time	Result	Time
Corrected WMF [7, 16, 18]	80	Secure	47.51 ms	Threat	112.75 ms	Attack	150.09 ms
TESLA [21, 22]	343	Secure	3.17 s	Threat	3.55 s	Threat	4.37 s
Auth Range [6, 8]	53	Secure	38.58 ms	Secure	60.73 ms	Attack	46.47 ms
CCITT X.509 (1c) [3]	135	Secure	162.69 ms	Secure	231.86 ms	Secure	224.00 ms
CCITT X.509 (3) BAN [7]	198	Secure	791.00 ms	Secure	1058.05 ms	Secure	969.97 ms
NS PK Time [10, 17, 20]	173	Secure	170.00 ms	Threat	205.93 ms	Threat	353.20 ms

drift parameters are not constrained by other protocol parameters. If any clock drift parameter is constrained by other protocol parameters, we believe that the protocol has security **threat** under the clock drift as those constraints must be checked at runtime in the real application. For instance, given the network latency  $p_n$  and the maximum drift  $p_c$  for a local clock  $c$ , if  $p_c < p_n$  is required for security but it cannot be satisfied in the real application scenario, the protocol is vulnerable.

## 5 Evaluations

Our method has been integrated into the tool named Security Protocol Analyzer (SPA). SPA relies on PPL [4] to check the satisfaction of timing constraints, i.e., to tell whether a set of timing constraints is empty or not. We use SPA to check multiple timed protocols as shown in Table 3. All the experiments are conducted using a Mac OS X 10.10.5 with 2.3 GHz Intel Core i5 and 16G 1333 MHz DDR3. In order to clearly demonstrate how clock drift can affect the security of protocols, all of the protocols evaluated in this section are correct under perfect synchronization. The evaluated protocols are *corrected* WMF [7, 12], TESLA [21, 22], a distance bounding protocol [6, 8], *corrected* CCITT [3, 7, 9], and a timing commitment version [10, 15] of Needham-Schroeder [17, 20]. All of the protocols can be verified or falsified for an unbounded number of protocol sessions. SPA and the protocol models are available at [1]. Notice that the security (secure constraints over parameters) is proved based on the satisfaction of all of the queries, so we do not show the results for different queries separately in the table. Particularly, we have found a new clock drift related security threat in TESLA. In the following, we illustrate how SPA works with our running example first and then other protocols.

### 5.1 CWMF Protocol

Based on the specification of CWMF in Sect. 2.3, WMF is checked in three different scenarios of clock drift. Let  $d_a$ ,  $d_s$  and  $d_b$  be the drift distances of  $c_a$ ,  $c_s$  and  $c_b$  respectively.

- When all clocks are perfectly synchronized, in order to finish CWMF, SPA returns that the minimum network latency  $p_n$  should be smaller than the maximum message lifetime  $p_m$ .
- (SR) When the local clocks share the same clock rate, CWMF is correct if and only if the following constraints are met: (1)  $0 \leq d_s - d_a$ ; (2)  $0 \leq d_b - d_s$ ; (3)  $d_s - d_a \leq p_m - p_n$ ; (4)  $d_b - d_s \leq p_m - p_n$ . Constraint (1) and (2) ensure that the injective authentication is finished within  $p_m$ . Constraint (3) and (4) are required to finish the protocol. Since  $d_a$ ,  $d_s$  and  $d_b$  exist in the constraints, which might not be satisfied in practice, the verification result presents a security threat of CWMF.
- (VR) When different local clocks have different clock rates, the constraint returned by SPA is *false*. It means that SPA cannot find the right parameter values to make CWMF secure in the case of VR. Intuitively, the authentication property requires CWMF to be finished within  $2 \times p_m$ , whereas the protocol itself can only achieve the timing threshold  $2 \times p_m + p_a + p_b$ . In order to ensure  $2 \times p_m + p_a + p_b \leq 2 \times p_m$ , we have  $p_a + p_b \leq 0$ . Since  $p_a$  and  $p_b$  are positives, SPA cannot find any suitable constraint for these parameters.

## 5.2 TESLA Protocol

TESLA [21, 22] is short for Timed, Efficient, Streaming, Loss-tolerant Authentication protocol. It can provide efficient authenticated broadcast over lossy channels. Generally, it consists of many resource constrained receivers and a relatively powerful sender.

**Protocol Description.** The security goal of TESLA is to transfer a set of messages  $\{M_j \mid j \in [0 \dots n]\}$  from a sender  $S$  to a receiver  $R$  in an authenticated manner, i.e., every message  $M_j$  accepted by  $R$  is sent by  $S$  previously. Since  $R$  have limited computing power,  $S$  cannot adopt signature for authentication purpose because of the large computing overhead. As a result,  $S$  computes hash values for messages with hash keys and uses these keys for authentication. Specifically,  $S$  divides the message transmission time into several continuous intervals. Each interval has the same length of  $p_d$  ( $p_d > 0$ ). Then,  $S$  sends the messages with their hash values in different time intervals and reveals the corresponding hash keys in later time intervals. For example,  $S$  sends  $\langle M_j, mac(M_j, k_i) \rangle$  in the  $i$ -th time interval and reveals the key  $k_i$  in the next interval. Since only  $S$  knows  $k_i$  before  $k_i$  is revealed, when  $k_i$  is check to be a hash key from  $S$ ,  $\langle M_j, mac(M_j, k_i) \rangle$  should be sent from  $S$ . In order to check the authenticity of the hash keys, TESLA requires these keys to form a chain such that  $k_i$  can be computed by  $k_{i+1}$  with a one-way function. Hence, when  $S$  can authenticate the first key  $k_0$  to  $R$ ,  $R$  can use  $k_0$  to authenticate newly received hash keys. Additionally, using this method, even if some hash key  $k_i$  is lost, once  $k_{i+x}$  ( $x > 0$ ) is received by  $R$ ,  $k_i$  can be computed from  $k_{i+x}$  for authentication. In order to provide sound security,  $S$  in TESLA does not send the hash keys directly. Instead, it sends the hash key generators  $\{k'_i\}$  and uses the generators to compute the actual hash keys  $\{k_i\}$ .



Unlike WMF and many other protocols, TESLA does not assume perfect clock synchronization. It rather requires loose time synchronization between  $S$  and  $R$ , where  $R$  knows the upper-bound of the local clock drift  $\delta$  between  $S$  and  $R$ . In order to obtain the upper-bound, TESLA adopts the following two-step protocol. Firstly,  $R$  reads its current time as  $t_r$ , generates a nonce (a random number)  $n$  and sends  $n$  to  $S$ . Secondly,  $S$  reads its current time as  $t_s$ , signs  $t_s$  and  $n$  with its private signing key  $sk_s$  and sends the signature back to  $R$ . When  $R$  receives the signature from  $S$ ,  $R$  can be sure that  $\delta$  has an upper-bound of  $t_s - t_r$ . Thereafter, when  $R$  receives a message from  $S$  at its local time  $t'_r$ , he can claim that the current time of  $S$  is upper-bounded by  $t'_r + t_s - t_r$ . Due to the limited space, the modeling details of TESLA are available in the full paper version [1].

**Verification Results.** When TESLA is checked with  $SR$  or no clock drift, it is verified as correct with the requirement  $2 \times p_n < p_d$ , i.e., the length of every interval  $p_d$  should be larger than twice of the minimal network latency  $p_n$ . To the best of our knowledge, this configuration requirement, justified in the following, has not been reported in any other literature before. According to the verification result from SPA, this protocol configuration requirement is necessary because of the over-approximation of  $S$ 's clock at  $R$ 's side in TESLA. When a payload is sent by  $S$  at  $t'_s$  and received by  $R$  at  $t'_r$  based on their local clocks respectively, the *clock synchronization* ensures that  $t'_s < t_s^{bound} = t'_r + t_s - t_r$ . Additionally, in order to receive and check the payload successfully,  $t'_s$  and  $t_s^{bound}$  should belong to the same interval. Hence, given an initial time  $t_0$  and an interval index  $i$ , we have  $t_0 + i \times p_d \leq t'_s < t'_r + t_s - t_r < t_0 + (i + 1) \times p_d$ , which implies that  $p_d$  should be larger than  $(t'_r - t_r) - (t'_s - t_s)$ . That is,  $2 \times p_n < p_d$ .

When TESLA is checked with  $VR$ , SPA automatically reports a new security requirement such that  $p_r + p_s \leq p_n$ , where  $p_r$  and  $p_s$  are the maximum clock drift of  $R$  and  $S$  respectively. This configuration requirement is necessary because the *clock synchronization* alone fails to guarantee the bounding  $t'_s < t'_r + t_s - t_r$ <sup>1</sup>. Hence, in order to prevent the adversary from using the published keys to construct legal payloads, the sum of the clock drift values from  $R$  and  $S$  should be smaller than the network latency. This new configuration largely limits the application of TESLA protocol when  $VR$  is assumed, which is also unreported in existing literatures.

## 6 Related Works and Conclusions

This work builds on our previous works [14, 15]. In this work, we extend the *timed applied  $\pi$ -calculus* with local clocks and clock drift. In order to verify the protocols specified in *timed applied  $\pi$ -calculus*, we define its semantics based on the *timed logic rules* [14, 15]. We introduce two clock drift scenarios based on whether the clock rate is shared or not. During the evaluation, we show that our framework is able to verify timed security protocols with clock drift

<sup>1</sup>  $2 \times p_n < p_d$  in SR has been updated to  $2 \times p_n < p_d + 2 \times (p_s + p_r)$  in VR.

automatically, which is unique comparing with other existing works. The analyzing framework closest to ours was proposed by Delzanno and Ganty [12] which applies  $MSR(\mathcal{L})$  to specify unbounded crypto protocols by combining first order multiset rewriting rules and linear constraints. According to [12], the protocol specification is modified by explicitly encoding an additional timestamp, representing the initialization time, into some messages. Thus the attack can be found by comparing the original timestamps with the new one in the messages. However, it is unclear how to verify timed protocol in general using their approach. Our method can be applied to verify protocols without any protocol modification. Many tools [5, 11, 19] for verifying *untimed* security protocols are related.

In this work, we develop a systematic method to formally specify as well as automatically verify timed security protocols with clock drift. We have integrated our method into SPA and used it to analyze several timed protocols. In the experiments, we have found new security threats related to clock drift in TESLA. Since the problem of verifying security protocols is undecidable in general, we cannot guarantee the termination of our method. However, similar to existing works on verifying security protocols [5, 14, 15], it has been shown that it often terminates for practical protocols.

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