2012

ROAD: A New Spatial Object Search Framework for Road Networks

Ken C. K. Lee
Wang-chien Lee
Baihua ZHENG
Singapore Management University, bhzheng@smu.edu.sg
Yuan Tian

Follow this and additional works at: http://ink.library.smu.edu.sg/sis_research

Citation
Available at: http://ink.library.smu.edu.sg/sis_research/1987

This Journal Article is brought to you for free and open access by the School of Information Systems at Institutional Knowledge at Singapore Management University. It has been accepted for inclusion in Research Collection School Of Information Systems by an authorized administrator of Institutional Knowledge at Singapore Management University. For more information, please email libIR@smu.edu.sg.
ROAD: A New Spatial Object Search Framework for Road Networks


Abstract—In this paper, we present a new system framework called ROAD for spatial object search on road networks. ROAD is extensible to diverse object types and efficient for processing various location-dependent spatial queries (LDSQs), as it maintains objects separately from an underlying network and adopts an effective search space pruning technique. Based on our analysis on the two essential operations for LDSQ processing, namely, network traversal and object lookup, ROAD organizes a large road network as a hierarchy of interconnected regional sub-networks (called Rnets). Each Rnet is augmented with (1) shortcuts and (2) object abstracts to accelerate network traversals and provide quick object lookups, respectively. To manage those shortcuts and object abstracts, two cooperating indices, namely, Route Overlay and Association Directory are devised. In this paper, we present (1) the Rnet hierarchy and a number of properties useful in constructing and maintaining Rnet hierarchy, (2) the design and implementation of the ROAD framework, and (3) a number of efficient search algorithms for single-source LDSQs and multi-source LDSQs. We conduct a theoretical performance analysis and carry out an empirical study to evaluate ROAD. The analysis and experiment results show the superiority of ROAD over the state-of-the-art approaches.

Index Terms—Location-Dependent Spatial Query, Spatial Road Network, Indexing Techniques, and Search Algorithms.

1 INTRODUCTION

While location-based services (LBSs) are booming in this decade, many vendors start to provide map and navigation services (e.g., Garmin, GoogleMap, MapQuest, NavTeq, Yahoo! Map) along with convenient geo-tagging tools that enable the content providers (e.g., retail stores, facilities and general users) to publish location-dependent information on digital maps [1], [2]. Here, we refer to location-dependent information (e.g., point of interest, traffic and local events) as spatial objects (or objects for short). We define queries that search for spatial objects with respect to user-specified locations as location-dependent spatial queries (LDSQs). Examples of LDSQs for conference participants include Q1: find hotels within one mile from the conference venue; Q2: locate the nearest bus station to the conference venue; and Q3: find a restaurant closest to the hotels of the conference participants.

As we analyzed, two basic operations, namely, network traversal and object lookup, are involved in processing LDSQs on a road network. The former visits network nodes and edges according to network proximity, while the latter accesses a road network. The former visits network nodes and edges against object search criteria. Objects collected during the course of a traversal form a query result. Logically, the more network traversals and object lookups are involved, the larger the query processing overhead is incurred. As shown in Figure 1 where a network is modeled as a graph, two objects $o_1$ and $o_2$ are on one side of the network. If a nearest neighbor (NN) query is issued far away on the other side, say at $n_q$, the search cost is apparently higher than another NN query issued somewhere close to the objects.

As network traversals and object placements are constrained by the network topology, nodes and edges (i.e., the entire network) conceptually form an object search space. Since some search subspaces (e.g., the middle portion bounded by dashed line in Figure 1) may not have objects of interest, we could facilitate network traversals by pruning those subspaces without objects of interest. This observation inspires an idea of search space pruning, based on which we design a novel, efficient and extensible system framework, called ROAD, for processing LDSQs on road networks.

![Fig. 1: Basic idea behind ROAD framework](image)

In ROAD, a network is first formulated as a set of interconnected regional subnets called Rnets, each representing a search subspace. On top of the Rnets, two kinds of additional information are derived: (1) selective (i.e., shortest) paths across an Rnet that enable any traversal to bypass Rnet if it has no object of interest, and (2) the existence and/or contents of objects that are inside Rnets to provide quick traversal guidelines. Both (1) and (2) are further elaborated into the notions of shortcuts and object abstract, respectively. Revisit Figure 1. Two highlighted shortcuts, one from $n_1$ to $n_3$, and the other from $n_2$ to $n_3$, direct the NN search issued at $n_q$ to bypass the Rnet $R$, and enable the traversal to continue at node $n_3$, since Rnet $R$ has no object of interest, as indicated by its empty object abstract.

To realize ROAD, we propose two novel index structures, namely, Route Overlay and Association Directory (and ROAD is named after these two key components). The former manages the physical network structure (i.e., nodes and edges) and the shortcuts, while the latter manipulates the mappings...
of objects and object abstracts on nodes, edges and Rnets. In this paper, we detail the design, implementation and evaluation of ROAD and provide a holistic solution to several important research issues that include organization of Rnets, search algorithms for various LDSQs and framework updates. We also perform an analysis and simulation to evaluate the ROAD performance. In summary, the significant contributions presented in this paper are seven-fold:

1) We present ROAD, a novel system framework to support spatial object searches on road networks. ROAD cleanly separates the road network and objects, exploits the idea of search space pruning, and supports searches with different distance metrics.

2) We formulate Rnet hierarchy and explore several properties to reduce indexing overhead and improve query and update performance.

3) We devise efficient search algorithms for single-source range queries and \(k\)-NN queries, i.e., classical types of LDSQs, upon the ROAD framework.

4) We devise efficient search algorithms for multi-source range queries and \(k\)-NN queries to illustrate the extensibility of ROAD for different LDSQs.

5) We develop efficient update techniques for ROAD maintenance to handle object and network updates.

6) We perform a theoretical analysis on the space and time efficiency of ROAD framework.

7) Besides, we conduct an extensive performance evaluation on ROAD.

The rest of the paper is organized as follows. Section 2 reviews related works. Section 3 presents the core concepts behind ROAD. Section 4 and Section 5 discuss the query processing algorithms for single-source LDSQs and multi-source LDSQs, respectively. Section 6 discusses the framework maintenance. Section 7 analyzes the ROAD performance. Section 8 evaluates ROAD compared with existing works through simulations. Finally, Section 9 concludes this paper.

## 2 RELATED WORK

Existing research works on processing LDSQs on road networks can be roughly categorized as solution-based approaches and extended spatial database approaches. They are reviewed as follows.

**Solution-based approaches** (e.g., VN\(^3\) [3], UNICONS [4], SPIE [5] and Distance Index [6]) utilize some pre-computed results to evaluate queries. While VN\(^3\), UNICONS, SPIE cater for NN queries, Distance Index supports both range and NN queries. Distance Index precomputes for all nodes the distances and pointers to subsequent nodes on paths towards individual objects, and encodes them as distance signatures. To reduce the storage overhead of distance signatures, distance ranges, rather than precise distances, are adopted such that distances within one range share the same signature. Figure 2 illustrates the distance signatures on objects \(o_1\) and \(o_2\) stored at \(n_q\) and \(n'_q\), with \(d_0 < d_1 < d_2 < d_3\). As we can observe, distance ranges maintained at some nodes about some objects located at nearby nodes can be very similar or even identical, that implies redundant storage. Thus, it incurs impractically large storage overhead.

In general, the pitfalls of solution based approaches include high pre-computation overhead, massive storage overhead, and expensive result maintenance cost. Besides, they adapt poorly to other types of queries, and to objects and network updates.

**Extended spatial database approaches** incorporate road networks to existing spatial databases. Due to the coexistence of object indices and road networks, two search strategies were studied. The first strategy is based on the idea of Euclidean distance bound that Euclidean distance is always the lower bound of network distance between any two locations. Approaches using this strategy [7], [8] first identify all the objects whose Euclidean distances to the query point are bounded by a certain distance threshold as a candidate set. Thereafter, the network distance between each candidate object and the query point is determined based on shortest path algorithms [9], [10] or materialized distances [11], [12]; and those with network distances larger than the threshold are eliminated. The second strategy is based on network expansion that gradually expands a search range on a network until all the nodes and edges that satisfy the search criteria are visited [7]. Along the traversal, objects indexed by spatial indexes (e.g., R-tree) associated with the visited nodes and edges form the result set; and the paths from a query node to those objects are the shortest paths. Although more efficient than Euclidean distance bound approaches, network expansion is still inefficient due to the slow node-by-node expansion towards all directions.

In this paper, we detail the design, implementation and evaluation of ROAD and provide a holistic solution to several important research issues that include organization of Rnets, search algorithms for various LDSQs and framework updates.
a neighboring node $n'_q$ with $T_{n_q}(n'_q)$ covering the objects and $d_{o,n}(n'_q)$ being the smallest. It avoids blind network traversal. However, this approach still needs to traverse the network in a node by node fashion. Even worse, bulky SPQIs accessed for all visited nodes make this approaches very I/O-inefficient. Further, all-pair shortest paths need to be computed in advance which is very computationally expensive.

Our ROAD differs from all those existing works as it considers a road network as an object space and utilizes search space pruning to enhance search performance, that is not explored by those works. Also, our ROAD is scalable to networks as it organizes a road network as a hierarchy, similar to HEPV [11] and HiTi [12]. However, the design and implementation of HEPV and HiTi only allow point-to-point shortest path searches. Our ROAD facilitates fast network expansion that can reach multiple destinations for objects, needed for LDSQs.

3 The ROAD Framework

In this section, we first introduce Rnets, shortcuts and object abstracts and discuss Rnet hierarchy formation, i.e., the key design in support of search space pruning in ROAD. Then, we present the core of ROAD implementation, namely, Route Overlay and Association Directory.

3.1 Preliminaries

We model a road network $\mathcal{N}$ as a weighted graph that consists of a set of nodes $\mathcal{N}$ and edges $\mathcal{E}$, i.e., $\mathcal{N} = (\mathcal{N}, \mathcal{E})$. A node $n \in \mathcal{N}$ represents a road intersection and an edge $(n, n') \in \mathcal{E}$ represents a road segment connecting nodes $n$ and $n'$. $[n, n']$ denotes the edge weight, which represents the travel distance, or trip time, or toll of $(n, n')$, and we assume all distances are positive. For simplicity, we use distance hereafter. A path $P(u, v)$ stands for a set of edges connecting nodes $u$ and $v$ and its distance $|P(u, v)| = \sum_{(n, n') \in P(u, v)} |n, n'|$. Among all paths connecting node $u$ and node $v$, the one with the smallest distance is referred to as the shortest path, denoted by $SP(u, v)$. The network distance $||u, v||$ between $u$ and $v$ is the distance of their shortest path $SP(u, v)$, i.e., $||u, v|| = |SP(u, v)|$. Given a set of objects, $\mathcal{O}$, we consider that objects (in $\mathcal{O}$) reside on edges (i.e., road segments) in a network. We denote a mapping function $L(n, n')$ on an edge $(n, n')$ to represent a set of objects on the edge. Additionally, we use $\delta(o, n)$ (or $\delta(o, n')$) to represent the distance between an object $o \in L(n, n')$ and the endpoint $n$ ($n'$) of the edge.

In our discussion, all LDSQs are assumed to be initiated at nodes without loss of generality. In general, each LDSQ is specified with a distance condition $D$ and an attribute predicate $A$. Given $\mathcal{O}$ mapped on $\mathcal{N}$ and a query node $n_q$, an object, $o$ (in $\mathcal{O}$), is collected as the answer to an LDSQ if (1) its distance from $n_q$, denoted by $||n_q, o||$ (i.e., $\min(||n_q, n|| + \delta(o, n), ||n_q, n'|| + \delta(o, n'))$) satisfies $D$ (e.g., $||n_q, o|| \leq 10$ miles); and (2) its attributes denoted by $o.a$ satisfy $A$ (e.g.,

1. Objects at nodes (i.e., road intersections) can be treated as they are located at the end of the corresponding edges.
2. This assumption can be easily relaxed to handle LDSQs issued on edges via searching objects on the edges followed by running the queries at the ending nodes of the corresponding edges.

---

### TABLE 1: Notations

<table>
<thead>
<tr>
<th>Notations</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mathcal{N} = (\mathcal{N}, \mathcal{E})$</td>
<td>a network $\mathcal{N}$ with nodes $\mathcal{N}$ and edges $\mathcal{E}$</td>
</tr>
<tr>
<td>$\mathcal{O}$</td>
<td>a set of objects</td>
</tr>
<tr>
<td>$\mathcal{R} = (\mathcal{N}_R, \mathcal{E}_R, B_R)$</td>
<td>an Rnet $\mathcal{R}$ with nodes $\mathcal{N}_R$, edges $\mathcal{E}_R$ and border nodes $B_R$ (see Def. 1)</td>
</tr>
<tr>
<td>$L(n, n')$</td>
<td>a subset of objects located on edge $(n, n')$</td>
</tr>
<tr>
<td>$L(R)$</td>
<td>an object abstract (i.e., objects located inside an Rnet $\mathcal{R}$) (see Def. 2)</td>
</tr>
<tr>
<td>$</td>
<td></td>
</tr>
<tr>
<td>$\delta(o, n)$</td>
<td>distance between an object $o$ to a node $n$</td>
</tr>
<tr>
<td>$S(b, b')$</td>
<td>a shortcut $S$ between border nodes $b$ and $b'$ (see Def. 3)</td>
</tr>
</tbody>
</table>

3.2 Rnet, Shortcut and Object Abstract

First of all, we introduce a notion of regional sub-networks (i.e., Rnets) as in Definition 1. Each Rnet encloses a set of edges bounded by a set of border nodes. Each border node serves as the entrance to and the exit of an Rnet.

**Definition 1: Rnet.** In $\mathcal{N} = (\mathcal{N}, \mathcal{E})$, an Rnet $\mathcal{R} = (\mathcal{N}_R, \mathcal{E}_R, B_R)$ captures a search subspace, where $\mathcal{N}_R, \mathcal{E}_R$ and $B_R$ stand for nodes, edges and border nodes in $\mathcal{R}$, and

1. $E_R \subseteq \mathcal{E}$,
2. $\mathcal{N}_R = \{n | (n, n') \in \mathcal{E}_R \land (n', n) \in \mathcal{E}_R\}$, and
3. $B_R = \mathcal{N}_R \cap \{n | (n, n') \in \mathcal{E}' \land (n', n) \in \mathcal{E}'\}$, where $E' = E - E_R$.

As in the previous example depicted in Figure 1, when a search reaches $n_1$ covered by an Rnet $R$, we need (1) a hint about what objects are in $R$ to decide if a detailed examination of $R$ is needed; and (2) an artifact at $n_1$ connecting the other border nodes of $R$ (e.g., $n_3$) to allow the search to bypass $R$ and to continue the traversal thereafter. Accordingly, we define object abstracts and shortcuts as in Definition 2 and Definition 3, respectively. Here, an object abstract is the summary of objects located on enclosed edges and a shortcut is a shortest path between two border nodes.

**Definition 2: Object Abstract.** The object abstract of an Rnet $\mathcal{R}$, $L(\mathcal{R})$ indicates all the objects residing on edges in $\mathcal{E}_R$, i.e., $L(\mathcal{R}) = \bigcup_{e \in \mathcal{E}_R} L(e)$.

**Definition 3: Shortcut.** The shortcut, $S(b, b')$, between two border nodes $b$ and $b'$ (in $B_R$) of an Rnet $\mathcal{R}$ is the precomputed shortest path $SP(b, b')$ and its distance is $||b, b'||$. Notice that the edges that contribute to $SP(b, b')$ might not necessarily be included in $E_R$.

3.3 Rnet Hierarchy

In ROAD, we structure a road network as a hierarchy of Rnets, where large Rnets at the upper levels enclose small Rnets at lower levels. At each level, a network can be viewed as a layer of interconnected Rnets. This design benefits search ranges of different sizes. To derive an Rnet hierarchy, we first treat the entire road network as a single level-0 Rnet that has no border node, and partition it into $p_1$ partitioned Rnets. Definition 4 formally defines Rnet partitioning. The partitioned Rnets are the children of the Rnet they partitioned from. At
each subsequent level \( i \), we partition each Rnet into \( p_i \) child Rnets. Then, at any level \( x \in [0, l] \) where \( l \) is the number of levels, the network is fully covered by \( \prod_{i=1}^{l} p_i \) interconnected Rnets. As a whole, there are \( \sum_{h=0}^{l} \prod_{i=1}^{h} p_i \) Rnets.

**Definition 4: Rnet partitioning.** Partitioning of an Rnet \( \mathcal{R} = (N, E, B) \) forms \( p \) child Rnets, \( \mathcal{R}_1, \mathcal{R}_2, \ldots, \mathcal{R}_p \), where \( p > 1 \) and \( \mathcal{R}_i = (N_i, E_i, B_i) \). Here, \( N = \bigcup_{1 \leq i \leq p} N_i \), \( E = \bigcup_{1 \leq i \leq p} E_i \), \( B \subseteq \bigcup_{1 \leq i \leq p} B_i \). Also, the following three conditions must hold.

1. Edges of all children Rnets are disjoint, i.e., \( \forall 1 \leq i, j \leq p, i \neq j \rightarrow E_i \cap E_j = \emptyset \).
2. Nodes in an Rnet are connected by edges in the same Rnet, i.e., \( \forall_i \forall_{(n, n')} \in E_i \ n \in N_i \land n' \in N_i \).
3. Border nodes in an Rnet are nodes, common to its parent Rnet border nodes or nodes in its sibling Rnets, i.e., \( B_i = N_i \cap (B \cup \bigcup_{j \in \{\{1, p\} - \{i\}\}} N_j) \). \( \square \)

As illustrated in Figure 4, a network \( N \) is first partitioned into three Rnets, namely, \( R_1, R_2 \) and \( R_3 \), each of which is then partitioned into 2 smaller Rnets, \( R_{ia} \) and \( R_{ib} \), where \( i \in [1, 3] \).

Consequently, \( R_1, R_2 \) and \( R_3 \) form the level-1 Rnets and \( R_{1a} \), \( R_{1b} \), \( R_{2a} \), \( R_{2b} \), \( R_{3a} \), and \( R_{3b} \) form the level-2 Rnets. Also, \( n_3 \), i.e., common to both \( R_2 \) and \( R_3 \), is a border node between them. Meanwhile, it is shared by both \( R_{2b} \) and \( R_{3a} \) and thus is also a border node of \( R_{2b} \) and \( R_{3a} \).

![Fig. 4: Example Rnet hierarchy](image)

As the goal of ROAD is to provide a general-purpose search platform for ad hoc tagged spatial objects and various LDSQs, we adopt a network partitioning that can generate equal-sized Rnets and the smallest number of border nodes, which in turn minimizes the number of shortcuts formed. This network partitioning problem is, however, known NP-complete. Heuristically, we adopt both geometric approach [15] and Kernighan-Lin algorithm (KL algorithm) [16]. The geometric approach first coarsely partitions a network into two by dividing edges spatially. KL algorithm is then used to refine the partitioned Rnets by exchanging edges between them until no further exchanges can reduce the number of border nodes. We set \( p_i \) to be power of 2 (i.e., \( p_i = 2^x \), for \( x \) being a positive integer) and recursively apply this binary partitioning until \( p_i \) Rnets are formed for each level \( i \). This network partitioning approach is also used in [11] as it provides a quick network partitioning in a reasonably good quality. Alternatively, partitioning can be based on network semantics. For instance, a country-wide road network can be partitioned into levels of states, counties, cities, and townships.

After an Rnet hierarchy is formed, object abstracts and shortcuts are constructed in a bottom-up fashion. As edges in Rnets are fully covered by their parent Rnet according to Definition 4, object abstracts of an Rnet can be constructed directly from their child Rnets. Lemma 1 states this property.

**Lemma 1:** The object abstract of a parent Rnet \( \mathcal{R} \) fully covers those of all its child Rnets \( \mathcal{R}_1, \ldots, \mathcal{R}_p \), i.e., \( L(\mathcal{R}) = \bigcup_{1 \leq i \leq p} L(\mathcal{R}_i) \). \( \square \)

The shortcuts from a border node to another can be determined by Dijkstra’s algorithm [10]. Here, we identify several unique properties of the shortcuts. First, the shortcuts in level-\( i \) Rnets can be calculated based on those in level-(\( i + 1 \)) Rnets. Thus, shortcuts in high-level Rnets can be presented as a sequence of shortcuts in immediate low-level Rnets. Second, determined shortcuts in Rnets can be used to compute other shortcuts of Rnets in the same level. Third, to alleviate the storage cost for shortcuts, those shortcuts \( S(b, b') \) that can be regenerated by other shortcuts in the same Rnets can be ignored. Please refer to [17] for the detailed statements and proofs of these properties and they are skipped for space saving.

3.4 Route Overlay and Association Directory

Based on Definition 4 that the border nodes in a parent Rnet are always the border nodes in some of its child Rnets, we propose a novel index structure, namely *Route Overlay*, which naturally flattens a hierarchical network into a plain structure to facilitate search space expansion over a network.

In Route Overlay, nodes are indexed by an one-dimensional index with unique node IDs as search keys. In our implementation, we use \( B^+ \)-tree\(^3 \). Each leaf entry of \( B^+ \)-tree points to one node, together with a *shortcut tree*, i.e., a specialized tree-based index structure that organizes shortcuts and edges to facilitate search traversals. If a given node \( n \) is a border node of an Rnet, all the shortcuts from \( n \) to other border nodes belonging to the same Rnet are captured by non-leaf entries of \( n \)’s shortcut tree. Also, shortcut trees preserve the Rnets hierarchy by placing shortcuts of parent Rnets right above those belonging to the corresponding child Rnets. On the other hand, a leaf entry stores all the physical edges to its neighboring nodes. This shortcut tree structure generalizes the adjacency lists in many conventional network storage schemes.

![Fig. 5: Route Overlay](image)

Figure 5 shows the Route Overlay for our network presented in Figure 4. Take a non-border node \( n_a \) as an example. Its shortcut tree has only one leaf entry that contains edges to

\(^3\) Besides \( B^+ \)-tree, alternatives such as Hash index can be used.
Similarly, associated with objects are not kept in the B-tree used to represent an object abstract with smaller storage techniques such as bloom filter [18] and signature [19].

Besides, shortcuts to two levels. The root entry contains shortcuts of Rnets \( R_{1a} \) and \( R_{1b} \). Since \( R_{1a} \) has only one border node, no shortcuts for \( R_{1a} \) are kept. Below it are two physical edges to \( n_q \) and \( n_q' \). Besides, shortcuts to \( n_1 \) and \( n_2 \) are kept for \( R_{1b} \) at the top level. Then, physical edges to \( n_3 \) and \( n_4 \) at \( R_{1b} \) are placed at the bottom. As will be explained later, this shortcut tree structure can effectively facilitate search processes.

Next, we propose Association Directory, an efficient object lookup mechanism in ROAD based on a one-dimensional index, e.g., B+-tree, with unique node IDs or Rnet IDs as the search key. Associated with node \( n \) (\( n' \)) are objects \( o \) in \( L(n, n') \) together with their distances \( \delta(o, n) \) (\( \delta(o, n') \)). Similarly, associated with \( R \) is the object abstract of an Rnet \( R \). As an Rnet may contain a number of objects, several techniques such as bloom filter [18] and signature [19] can be used to represent an object abstract with smaller storage overheads. Besides, those nodes and Rnets that do not have objects are not kept in the B+-tree to further reduce the storage cost. If the search cannot find a node (Rnet) in the Association Directory, no object is implied for the node (Rnet).

**Fig. 6:** Association Directory

Figure 6 depicts an Association Directory for objects \( o_1 \) and \( o_2 \) in our example. Object \( o_1 \) on edge \( (n_1, n_q) \) is pointed by the nodes \( n_f \) and \( n_q \) and it is associated with its corresponding distances to the nodes. Moreover, both Rnet \( R_{3b} \) and its parent Rnet \( R_3 \) that contain objects \( o_1 \) and \( o_2 \) are associated with \( \{o_1, o_2\} \) in the Association Directory. Subject to applications, other objects can be placed into the same or different Association Directory to facilitate the mappings of various objects on the same road network.

### 4 Single-Source LDSQ Algorithms

This section presents search algorithms to support single-source LDSQs that include range queries and \( k \)NN queries. A range query finds objects of interest within a specified distance range to the query point \( n_q \) (e.g., Q1 in Section 1). A \( k \)NN query returns the \( k \) objects of interest closest to \( n_q \) (e.g., Q2 in Section 1).

We first discuss the evaluation of \( k \)NN query. To illustrate the basic idea of our approach, we use a simple network that consists of a chain of nodes in Figure 7. In the figure, the network is partitioned into three Rnets and each of them is further divided into two smaller Rnets. An NN query is issued at \( n_2 \) and two objects \( o_1 \) and \( o_2 \) are located on edges \( (n_11, n_12) \) and \( (n_12, n_13) \), respectively. Nodes \( n_3, n_5, n_7 \) and \( n_9 \) are border nodes. The search first expands from \( n_2 \) to \( n_1 \) and \( n_3 \) inside \( R_{1a} \). The traversals are shown as a sequence of annotated arrows (as arranged vertically) in the figure.

Since \( n_3 \) is the border node of Rnets \( R_{1a} \) and \( R_{1b} \), the object abstract associated with \( R_{1b} \) is checked. As it indicates no object of interest within \( R_{1b} \), the shortcut \( S(n_3, n_5) \) is taken to bypass \( R_{1b} \). Next, the search resumes at node \( n_5 \), i.e., the border node of Rnets \( R_2 \) and \( R_{2a} \). Based on the object abstract, the shortcut \( S(n_5, n_9) \) is taken to bypass \( R_2 \) and reach \( n_9 \). Similarly, the search follows the shortcut \( S(n_9, n_{11}) \) to reach \( n_{11} \). Now, as \( R_{3b} \) contains objects, a traversal within \( R_{3b} \) is needed. The traversal follows the physical edges to find object \( o_1 \). Here, we can see the search only takes three jumps from \( n_3 \) to \( n_{11} \), that significantly saves the traversal cost, compared with the gradual network expansion.

Following the basic logic of network expansion, Algorithm \( k \)NNSearch incorporates shortcuts in Route Overlay and object abstracts in Association Directory for speedup. It repeatedly expands the search in the network from \( n_q \) by visiting the closest unexplored node to guarantee that the first \( k \) qualified objects visited are the \( k \)NN objects. We maintain a priority queue \( P \) to sort pending entries in the non-descending distance order from \( n_q \). Each entry \( (\epsilon, d) \) in \( P \) records a node or an object \( (\epsilon) \) and its distance \( (d) \) from \( n_q \).

The algorithm takes the Route Overlay (RO), Associate Directory (AD), a query node \( (n_q) \), and a desired number of NNS \( (k) \) as inputs, and defaults all nodes and objects as “unvisited”. To start with, \( P \) is initialized with \( (n_q, 0) \). Then, the algorithm repeatedly examines the head entry \( (\epsilon, d) \) from \( P \) until \( k \) answer objects are retrieved or the network is completely traversed. Since nodes and objects could be reached more than once via different paths, \( \epsilon \) already marked with “visited” is discarded. Otherwise, the examination of \( \epsilon \) begins. If \( \epsilon \) refers to a node, two tasks need to be performed.

1. \( AD \) is first accessed for objects \( o \) associated with the node \( \epsilon \), which will be put to \( P \) as \( (\epsilon, d+\delta(o, \epsilon)) \) for later examination.
2. Next, Algorithm ChoosePath is invoked to decide subsequent nodes to continue the network expansion from \( \epsilon \) that will be discussed next. If \( \epsilon \) is an object, it is collected into a result set \( Res \). After examination, \( \epsilon \) is marked “visited”. Finally, the answer objects are outputted and the search completes.

With shortcut trees organizing shortcuts and edges in accordance with the Rnet hierarchy, Algorithm ChoosePath can quickly identify appropriate shortcuts and edges to expand the search range from a node \( n \). In brief, it examines the shortcut tree of the node \( n \) in Route Overlay in the depth-first traversal order. If \( n \) is a border node, the shortcut tree must have multiple levels. For every non-leaf level, an Rnet \( R \) is checked against Association Directory. If no object of interest is found, \( R \), together with all its child Rnets, are bypassed. The border nodes reached by the shortcuts are enqueued to \( P \). Otherwise (i.e., \( R \) contains objects of interest), the lookup goes down to the next lower level to examine its child Rnets in a similar
fashion. When the search reaches the leaf level, all neighboring
nodes connected by physical edges are collected. If \( n \) is a
non-border node, its shortcut tree contains only one level (i.e.,
physical edges) and all the corresponding neighboring nodes
are put into \( P \). Please refer to [17] for the detailed pseudo-
codes of Algorithm \texttt{kNNSearch} and Algorithm \texttt{ChoosePath}.

Algorithm \texttt{RangeSearch} that supports range queries resembles
Algorithm \texttt{kNNSearch} except that the search ends when a
portion of the network within the distance bound (as specified
by a query) is completely traversed. All visited objects are the
answer objects. To save space, we omit the discussion of this
approach.

\section{Multi-Source LDSQ Algorithms}

A multi-source LDSQ finds objects with respect to \( m \) query
nodes, i.e., \( q_1, \ldots, q_m \) \((m > 1)\). A multi-source \( k \)NN query
finds \( k \) objects whose maximum distances from all query
nodes \((i.e., \max \{d_i, i \in [1, m]\})\) are the minimum, where
\( d_i = ||q_i, o|| \). Q3 discussed in Section I is an example.
A multi-source range query retrieves all objects of interest
within distance range \( r \) with respect to all query nodes \((i.e.,
\forall i \in [1, m] d_i \leq r)\). In the literature, [8] suggests to process
multi-source LDSQs as Euclidean distance bound approach
that first estimates candidate objects based on their Euclidean
distances, calculates the candidates’ network distances through
network traversals and filters out the false candidate objects.
This approach covers a larger search space and incurs longer
processing times than necessary.

\subsection{Concurrent Network Expansion}

\textit{ROAD} adopts a \textit{concurrent approach} that expands a search
space from all query nodes by exploring nodes with the
minimal overall network expansion, until all result objects are
obtained or the search range is completely traversed. Hereafter,
we call an expansion started from each query node, \( q_i \), as a
\textit{subquery}, \( q_i \). We first discuss our algorithm for multi-source
\( k \)NN query. It concurrently expands the search space from
individual query nodes. According to Lemma 2, the \( k \) first
visited objects are guaranteed to be the answer objects.

\textbf{Lemma 2}: With concurrent expansion, the first \( k \) objects
visited by all subqueries are the \( k \)NN objects. \qed

\textbf{Proof}. We prove this lemma by contradiction. Assume there
are \( k \) objects, i.e., \( o_1, \ldots, o_k \), just visited by all the subqueries.
We assume that \( o_i \ (i \in [1, k]) \) is not one of \( k \)NN as there
will be another object \( o_j \ (j \notin [1, k]) \) such that \( o_j \)’s maximum
distance to query points is smaller than that of \( o_i \). Suppose the
last subqueries visiting \( o_i \) and \( o_j \) are \( q_{a_1} \) and \( q_{a_2} \), respectively.
Since \( q_{a_1} \) visited \( o_i \) before \( q_{a_2} \) visits \( o_j \), the distance of \( o_i \)
from \( n_{q_i} \), i.e., its maximum distance (see Lemma 3) should
not be greater than that of \( o_j \) from \( n_{q_j} \). This contradicts the
assumption. Hence, \( o_j \) should not be a part of \( k \)NN query
result.

\textbf{Lemma 3}: With concurrent expansion, the maximum distance
of an object to all query nodes is determined by the last
subquery that visits it. \qed

\textbf{Proof}. The distances of an object, \( o \), to all \( m \) query nodes are
\( d_1, \ldots, d_m \). By concurrent expansion, \( d_i \leq d_j \) if the respective
subquery \( q_j \) reaches \( o \) earlier than \( q_j \). Thus, if \( q_j \) is the last
subquery visiting \( o \), \( d_j \) should be the largest.

\subsection{Rnet Visited Set and Border Node Visited Set}

Figure 8 shows a two-source \( 1 \)NN query based on the previous
example network but with different objects. The result object
is \( o_0 \) on \((n_5, n_9)\). Two subqueries, \( q_1 \) and \( q_2 \) proceed from \( n_2 \)
and \( n_1 \), respectively. However, as shown in the figure, before
they reach \( o_0 \), \( q_1 (q_2) \) may enter Rnet \( R_{1_k} (R_{3_k}) \) for an object
\( o_0 (o_c) \) based on the idea of single-source LDSQs. However,
\( o_0 \) and \( o_c \) are not the answer objects and thus the traversal
inside those Rnets is a waste.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig8.png}
\caption{Example two-source 1NN query}
\end{figure}

From this, we observe that the guidance of traversals by object
abstracts alone is \textit{inadequate} for multi-source LDSQs.
Instead, an Rnet is worth exploring only if it contains objects
of interest and it is reached by all subqueries. In our example,
\( R_2 \) is the first Rnet visited by both \( q_1 \) and \( q_2 \). According to the
latter condition, we introduce two additional data structures,
namely, \textit{Rnet visited set (RV)}, and \textit{border node visited set (BV)}.
An Rnet visited set is to keep track of subqueries that
have visited or reached a given Rnet. Referring to our example,
we keep \( q_1 \) with \( R_1 \) and \( R_{1_q} \), and \( q_2 \) with \( R_3 \) and \( R_{3_q} \) in \( RV \).
Now, as no Rnets are visited by both \( q_1 \) and \( q_2 \), no detailed
traversals within any Rnets are needed.

Conversely, Rnets \( R \) would be visited by all \( m \) subqueries at
different times. Some \( m - 1 \) subqueries have already bypassed
\( R \) and need to resume some of traversals in \( R \) when \( R \) is found
to be reached by all subqueries. This traversal resumption is
called \textit{backtracking}. To enable such backtracking, a border
node visited set is designed to keep track of the border nodes
of \( R \) via which each subquery \( q_i \) bypassed \( R \). Thus, whenever
a backtracking of an Rnet is triggered, each subquery knows
the border node to resume the network traversals.

\subsection{Search Algorithm}

Our Algorithm \texttt{MultiSource\textunderscore kNNSearch} exploits all the
above-discussed techniques for multi-source \( k \)NN query and its pseudo-code is listed in Figure 9. The algorithm main-
tains a priority queue \( P \) to sort pending entries in a non-
decreasing distance order from respective query nodes. Every
entry \((\epsilon, d, q_i)\) in \( P \) records a node or an object \((\epsilon)\), its distance
from \( n_{q_i} \) \((d)\), and the respective subquery \((q_i)\). We also keep
an Rnet visited list \((RV)\) and a border visited set \((BV)\). An
entry \((R, q_i)\) in \( RV \) indicates that \( R \) has been visited by \( q_i \).
An entry \((R, b, d, q_i)\) in \( BV \) records that a subquery \( q_i \) has
reached \( R \) via the border node \( b \), and \( d = ||b, n_{q_i}|| \). Similar to
\( RV \), we keep an object visited set, \( OV \), to record which
objects have been visited by which subqueries.

Initially, all nodes and objects are marked “unvisited by \( q_i \)”
\((i \in [1, m])\) and all the query nodes are enqueued as entries
into \( P \) (lines 1-2). Then, the search repeatedly evaluates the
head entry \((\epsilon, d, q_i)\) from \( P \) until \( k \) answer objects are retrieved
or the entire network is completely traversed (line 3-20). If \( \epsilon \)
has been visited by the same subquery \( q_i \), the evaluation on \( \epsilon \)
Algorithm MultiSource\textsubscript{NNSearch}(RO, AD, \{n_{q_1}, \ldots, n_{q_m}\}, k)
Input: Route Overlay (RO), Association Directory (AD), \{n_{q_1}, \ldots, n_{q_m}\}, k
Local: A set of m query nodes (\{n_{q_1}, \ldots, n_{q_m}\}), No. of NNs (k)
Output: Result set (Res)

Begin
1. foreach \(n_q \in \{n_{q_1}, \ldots, n_{q_m}\}\) do
2. enqueue(P, (\(o, q_i, \epsilon\)));
3. while (P is not empty AND \(|Res| < k\)) do
4. \((\epsilon, d, q_i, \epsilon)\) \(\leftarrow\) dequeue(P);
5. if (\(\epsilon\) is marked “visited by \(q_i\)”) then goto 3;
6. if (\(\epsilon\) is a node) then
7. \(O \leftarrow\) SearchObject(AD,\(\epsilon\)); // find objects with \(\epsilon\)
8. foreach \((\ldots, d(o, \epsilon), \epsilon)\) \(\in\) O do
9. enqueue(P, (\(o, d + (\delta(o, \epsilon), q_i))\));
10. foreach Rnet \(R\) containing \(\epsilon\) in \(O\) do
11. Rnet \(R\) visited by all subqueries
12. get (\(R, e', d', q'\) in BV, \(e'\) is the border nodes of \(R\);
13. enqueue(P, (\(e', d', q')));
14. mark \(\epsilon\) “unvisited by \(q'\)”;
15. MultiSource\textsubscript{ChoosePath}(RO, AD, \(\epsilon, q_i, d, P, RV, BV\));
16. else // \(\epsilon\) is an object.
17. adding (\(\epsilon, q_i\)) to OV;
18. if (\(\epsilon\) is visited by all subqueries) then
19. \(Res \leftarrow Res \cup \{\epsilon\}\);
20. mark \(\epsilon\) “visited by \(q_i\)”;
21. output Res;
End.

Fig. 9: Algorithm MultiSource\textsubscript{NNSearch}

is skipped (line 5). Otherwise, a detailed examination begins. If \(\epsilon\) is a node, three tasks need to be performed. First, its associated objects are fetched from Association Directory and enqueued to \(P\) for later examination (lines 7-9). Second, it records all Rnets that \(\epsilon\) belongs to in \(RV\) (line 10), followed by checking whether the visit of current node triggers the backtracking of any Rnet \(R\) (lines 11-14). If so, it resumes the traversal of \(R\) for all the subqueries at the border nodes \(b\) (of \(R, b, d', q'\)) maintained in \(BV\) (lines 12-13). Since border nodes \(b\) visited by each subquery \(q'\) have been marked “visited by \(q'\)” and are not visited by all subqueries, respectively.

To illustrate Algorithm MultiSource\textsubscript{ChoosePath}, we revisit the example as shown in Figure 8. First, subqueries, \(q_1\) and \(q_2\), expand from nodes \(n_2\) and \(n_11\), respectively. Each expansion is shown as an annotated arrow in Figure 11. At \(n_2\), \(q_1\) records its visit by adding (\(R_1a, q_1\)) to \(RV\). Similarly, at \(n_{11}\), \(q_2\) puts (\(R_{3a}, q_2\), (\(R_{3a}, q_2\) and (\(R_{3b}, q_2\) to \(RV\) and \(RV\)). \(R_1b\) is not yet visited by all the subqueries as informed by \(RV\). \(q_1\) bypasses it although it contains object \(o_a\). Then, \(q_2\) skips \(R_{3a}\) and \(R_{3b}\) since they have no object and are not visited by all the subqueries, respectively.

Fig. 10: Algorithm MultiSource\textsubscript{ChoosePath}

When \(\epsilon\) refers to an object, we update \(OV\) to indicate that object \(\epsilon\) has been accessed by the current subquery \(q_i\) (line 17). If it has been visited by all the subqueries, \(\epsilon\) is inserted to the result set \(Res\) (lines 18-19) which is outputted after the search completes (line 21). At the end of each iteration, \(\epsilon\) is marked “visited by \(q_i\)” (line 20).

Figure 10 outlines the pseudo-code of Algorithm MultiSource\textsubscript{ChoosePath}. The algorithm visits a shortcut tree associated with an input node \(n\) based on depth-first order and identifies appropriate shortcuts and edges to expand the search range. If an Rnet \(R\) in \(n\)’s shortcut tree (1) contains no object of interest as indicated by \(AD\); or (2) has not been visited by all the subqueries as tracked in \(RV\), the search keeps \(n\) and its distance from \(n_q\), in \(BV\) and takes the corresponding shortcuts to bypass \(R\) (line 7-9). Otherwise, the search continues to examine \(R\)’s child Rnets in the shortcut tree (line 10-11). When the leaf level is reached, all nodes connected by physical edges are collected.

Algorithm MultiSource\textsubscript{ChoosePath}(RO, AD, \(n, q, d, P, RV, BV\))
Input: Route Overlay (RO), Association Directory (AD), a node \(n\), a subquery \(q\), distance from \(n\) \(d\), Priority Queue (P), Rnet Visited Set (RV), Border Visited Set (BV)
Local: Stack (S);
Begin
1. \(T \leftarrow\) LoadShortcutTree(RO, \(n\));
2. push(S,T.root);
3. while (S is not empty) do
4. \(s \leftarrow\) pop(S);
5. if (\(s\) is not leaf) then
6. foreach \((R \in s)\) do
7. if (SearchObject(AD, \(R\)) has no object OR \(R\) is not visited by all subqueries in \(RV\)) then
8. add shortcuts (\(n, b'\)) (i.e., \((b', d + ||n, b'||, q)\)) to \(P\);
9. add (\(R, n, d, q\)) to \(BV\);
10. else
11. push all \(s\)’s children to \(S\);
12. else
13. add all edges \((n, n')\) in \(s\) as ((\(n', d + ||n, n'|, q)\)) to \(P\);
End.

Fig. 11: Example two-source 1NN query (in detail)

Then, \(q_2\) continues the traversal from \(n_9\) to \(n_5\) as at this moment, \(q_1\), has not yet reached \(R_2\). Here, (\(n_{52}, ||R_3, n_{11}||, q_2\)) is pending in \(P\) for next access. Therefore, \(q_1\) reaches \(n_{53}\), a border node of \(R_2\). It learns from \(RV\) and \(AD\) that \(R_2\) is visited by both \(q_1\) and \(q_2\) and it contains objects. Consequently, \(R_2\) needs detailed examination and its child Rnets are visited. As \(R_{2a}\) is not visited by \(q_2\), the shortcut is taken to bypass it and \(n_7\) is enqueued to \(P\) for later evaluation. Meanwhile, \(q_2\) resumes its traversal of \(R_2\) at the border node \(n_{93}\), as indicated by \(BV\). It takes the shortcut to \(n_7\) to visit \(R_{2a}\). As \(R_{2a}\) is

4. For brevity, we omit the descriptions of updating \(BV\), \(RV\) and \(OV\) hereafter.
already visited by \( q_1 \), \( q_2 \) navigates inside \( R_{2a} \) and \( q_1 \) resumes the traversal at \( n_5 \). Finally, the answer object \( o_b \) is reached by both subqueries and the search finishes.

Similar to Algorithm \textbf{MultiSourceRangeSearch}, Algorithm \textbf{MultiSourceRangeSearch} for multi-source range query traverses a network when all unexamined entries that include nodes or objects in the queue are beyond a specified distance range. Finally, the result objects are those visited by all the subqueries. We skip the algorithm details due to limited space.

6 ROAD FRAMEWORK MAINTENANCE

In this section, we present the ROAD maintenance in presence of network and object updates.

6.1 Object Update

Object changes are handled in Association Directory only. To insert an object on a certain edge \((n, n')\) in Rnet \( R \), we associate the object to nodes \( n \) and \( n' \) and update the object abstracts of \( R \) and \( R \)'s ancestor Rnets in an Association Directory. For object deletion, we simply remove the association of the objects from corresponding nodes and from the object abstracts of corresponding Rnets in an Association Directory. On the other hand, for the changes of object attributes, we update the object abstract associated with nodes and Rnets.

6.2 Network Update

Road condition and road network structure change over time. Instead of immediately rebuilding a Route Overlay upon changes, which is expensive, we develop several techniques to incrementally update Route Overlay for edge distance changes, and network structure changes.

6.2.1 Change of Edge Distance

When the distance of an edge changes (increases or decreases), some shortcuts have to be updated. To save unnecessary shortcut re-computations, ROAD adopts a filtering-and-refreshing approach. In the “filtering” phase, shortcuts possibly affected by an edge change are identified. Only the identified shortcuts will be considered to be updated. Then, in the “refreshing” phase, we perform necessary re-evaluations to update the shortcuts. According to Rnet properties stated in Section 3, the update of shortcuts related to level \( i \) Rnets in an Rnet hierarchy is not necessary unless shortcuts related to level \( i+1 \) Rnets are updated. Thus, we only explain how to re-compute shortcuts in the bottom level. The same idea can be applied to upper levels. Similarly, an edge, which is not covered by shortcuts in its own Rnet, is definitely not covered by shortcuts in other Rnets at the same level. Therefore, we examine the shortcuts in an Rnet that encloses the changed edge first. If no shortcut update is incurred, the update can be safely terminated. Suppose the distance \(|n, n'|\) of an edge is changed from \( d \) to \( d' \), detailed update procedures are as follows:

- **Edge distance increased** (i.e., \( d < d' \)). When an edge \((n, n')\) in an Rnet \( R \) increases its distance from \( d \) to \( d' \), only those shortcuts that cover \((n, n')\) might become invalid and need refreshed. In the filtering phase, we identify shortcuts that pass through \((n, n')\). Observing that a shortcut \( S(b, b') \) covering \((n, n')\) should have \(|b, b'|\) equal to \(|b, n| + |n, n'| + |n', b'|\) (where we consider \(|n, n'|\) before update, i.e., \( d \)), we search affected shortcuts by finding the shortest paths from both ending nodes \( n \) and \( n' \) to the border nodes in \( R \) and identifying shortcuts whose distances are equal to the path passing through \((n, n')\). In the refreshing phase, all the identified shortcuts are re-evaluated. Updates if any are then propagated to the parent level.

- **Edge distance decreased** (i.e., \( d > d' \)). When an edge \((n, n')\) in an Rnet \( R \) decreases its distance from \( d \) to \( d' \), it may contribute to paths shorter than some existing shortcuts. In the first filtering step, we test if the distance of a path from border node \( b \) via \((n, n')\) to another border node \( b' \) (with \(|n, n'| = d'\), the new edge distance) is shorter than the distance of the shortcut \( S(b, b') \). Here we expand from \( n \) and \( n' \) to reach border nodes and to determine the distances as shown in Figure 12(a). Once \(|b, n| + |n, n'| + |n', b'| < |b, b'|\), \( S(b, b') \) is identified to be affected. In the refreshing phase, those identified paths are replaced by the new paths passing by edge \((n, n')\). Again, updates are propagated to the upper level if shortcuts are updated.

6.2.2 Change of Network Structure

When new roads are constructed or existing roads are closed, the corresponding network topology is changed. We model these changes as addition or deletion of nodes and edges. Here, we treat changes of nodes as special cases of changes of edges, and only consider addition and deletion of edges below. Again, we update the network at the bottom level first and propagate the updates to the parent levels when necessary.

**Addition of a new edge.** A newly added edge \((n, n')\) directly connects nodes \( n \) and \( n' \), assuming that \( n \) and \( n' \) belong to Rnets \( R \) and \( R' \), respectively. Two possible cases: (1) \( R = R' \) and (2) \( R \neq R' \) are handled as follows.

- **Case 1:** \( R = R' \). Adding an edge connecting two nodes (e.g., \((n_a, n_b)\) in Figure 12(b)) can be treated as changing the edge distance from infinity to the current distance. Edge distance update mechanism discussed previously can be applied here. Accordingly, the Route Overlay stores the new edge.

- **Case 2:** \( R \neq R' \). Since an edge can only be included by one Rnet (say \( R \)), the node \( n' \) which does not belong to \( R \), has to be promoted to a border node between \( R \) and \( R' \). In Figure 12(b), the introduction of \((n_{a1}, n_d)\) to \( R \) gets \( n_d \) promoted to a border node. Also, the new edge \((n, n')\) might affect some shortcuts. The update approach for the change of edge distance is applied here. As a new border node is introduced, new shortcuts linking the new border node to other border nodes in the same Rnet have to be created.

**Deletion of an existing edge.** Deleting an edge \((n, n')\) breaks the link between two nodes \( n \) and \( n' \). Consider deleting \((n_a, n_{f_j})\) in Figure 12(b). Its deletion can be managed as handling the change of its edge distance to infinity and updating affected shortcuts. In addition, it is possible that one end node of a deleted edge is a border node. If all the edges of \( n \) are within one Rnet after the deletion of edge \((n, n')\), \( n \) is no longer a border node. As shown in Figure 12(b), after
As the storage overhead of shortcut trees highly depends on the storage cost of shortcuts, we can see from Equation (1) that given a fixed \( p \) for certain desired finest Rnet sizes, a smaller \( l \) together with a correspondingly larger \( p \) can reduce the storage overhead incurred by shortcuts. This observation is validated through experiments with real datasets presented in Section 8. Though it is used to estimate the storage cost, \( A \) can be reexpressed in terms of the number of nodes \( |N| \) as nodes are assumed to be uniformly distributed within \( A \). In the following discussion, we keep using \( A \) to formulate the cost and performance for simplicity.

### 7.2 Construction Time for Shortcuts

Next, we estimate the time for shortcut construction. In this analysis, we assume that Dijkstra’s algorithm is used, which has a run time complexity of \( O(V \cdot \log V) \) with \( V \) denoting the number of nodes traversed. At level \( l \) (i.e., the bottom level), each Rnet has \( A/p^l \) nodes among which \( (4 \cdot \sqrt{A/p^l}) \) are border nodes. By Dijkstra’s algorithm, the time complexity to compute all shortcuts in \( R \) is \( O(\sqrt{A/p^l} \cdot \log (A/p^l)) \). Hence, the time complexity for deciding all that shortcuts at level \( l \) having \( p \) Rnets is \( O(A \sqrt{A/p^l} \cdot \log (A/p^l)) \).

On the other hand, the time complexity for computing a shortcut in an Rnet, \( R \), at upper level \( i \) is \( O(\sqrt{A/p^i} \cdot \log \sqrt{A/p^i}) \), because there are \( O(\sqrt{A/p^i}) \) border nodes in \( R \)’s child Rnets. Again, there are \( (4 \cdot \sqrt{A/p^i}) \) border nodes in \( R \). As a result, the time complexity for shortcut computation at level \( i \) with \( p \) Rnets is \( O(A \cdot \sqrt{p} \cdot \log \sqrt{A/p^{i-1}}) \).

In summary, Equation (2) formulates the time complexity \( C_{spt} \) for shortcut computation.

\[
C_{spt} = O(A \sqrt{A/p} \cdot \log \sqrt{A/p}) + \sum_{i=1}^{l-1} O(A \cdot \sqrt{p} \cdot \log \sqrt{A/p^{i-1}}) = O(A \sqrt{A/p} \cdot \log \sqrt{A/p}) + A \cdot \sqrt{p} \cdot \sum_{i=1}^{l-1} \log \sqrt{A/p^{i-1}} \quad (2)
\]

We can see from Equation (2) that the computation time for shortcuts in the bottom level is the predominant factor to the total Rnet hierarchy construction time. This is also consistent with what we observed in our implementation. With bottom-up shortcut construction, time consumed for shortcut computation is the longest in the bottom level and then the time is significantly shortened in later upper levels.

### 7.3 LDSQ Processing Time

Next, we estimate the processing time for LDSQs. Here, we only consider single-source LDSQs. Typically, a query involves two phases, namely, (1) an expansion phase that expands a search range from a local smallest Rnet where a query is issued to larger Rnets that cover target objects, and (2) a drill-down phase that narrows down the search from large Rnets to the smallest Rnets that contain required objects. Assume that search expands up to Rnets in level \( t \), expecting that some level-\( t \) Rnets cover an object. By means of Dijkstra’s algorithm alike expansions, the processing time in terms of node visits in expansion phase, therefore,
is $O\left(\frac{A}{p} \log \frac{A}{p} + \sum_{i=1}^{l-1} \sqrt{\frac{A}{p^i}} \log \sqrt{\frac{A}{p^{i-1}}} \right)$. Here, the first term $\frac{A}{p} \log \frac{A}{p}$ denotes the time complexity for expanding physical edges and the second term does that for shortcuts in upper levels. Because it is symmetric to an expansion, drill down phrase results in the same time complexity. Further, we estimate $t$, the level of Rnet hierarchy that a search space needs to cover. Let $|O|$ be the number of objects evenly distributed in a network. Consider an NN query. We can expect that at the lowest level $t$, each Rnet with an area $\frac{A}{p^t}$ covers an NN object for a query. Hence, as $p' = |O|$, $t = \log_{p'} |O|$. Putting all of them together, we obtain the time complexity $C_{NN}$ in performing a single-source NN search as in Equation (3).

$$C_{NN} = O\left(\frac{A}{p'} \log \frac{A}{p'} + \sum_{i=\log_{p'} |O|}^{l-1} \sqrt{\frac{A}{p^i}} \log \sqrt{\frac{A}{p^{i-1}}} \right)$$

(3)

From Equation (3), we can see that if $p'$ is fixed, the first term is invariant but the second term will increase for $l$ while $p$ is reduced accordingly. We validated this observation in our experiments. Also, when $|O|$ is very large, we can anticipate that the second term will become very small, thus making NN searches more efficient. Meanwhile, for a single-source range query with a searched area of $a$, the time is determined as $\log_{p'} \frac{A}{a}$ such as the area of an Rnet at level $t$, i.e., $A/p^t$ sufficiently covers $a$.

8 Performance Evaluation

This section evaluates our proposed ROAD framework in terms of both indexing overhead and query performance. We applied ROAD (labeled as ROAD, hereafter) on four real road networks, namely, CA, NA, SF and PRS. CA and NA consist of highways in California and North America, respectively. SF and PRS correspond to streets and roads in San Francisco and Paris, respectively. Over those road networks are 100 to 100,100 objects following either uniform distribution or clustered distribution. To simulate clustered distribution, we select a set of nodes as cluster centroids and distribute objects within 10 nodes around them, with each cluster sharing the same number of objects. Table 2 lists all the evaluation parameters, their values and defaults used in the experiments.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Default</th>
</tr>
</thead>
<tbody>
<tr>
<td>Network $(N)$ (nodes,edges)</td>
<td>CA (21,048, 21,693)</td>
<td>NA</td>
</tr>
<tr>
<td>Distribution</td>
<td>NA (175,813, 179,179)</td>
<td>NA</td>
</tr>
<tr>
<td></td>
<td>SF (174,956, 223,001)</td>
<td>NA</td>
</tr>
<tr>
<td></td>
<td>PRS (327,402, 451,760)</td>
<td>NA</td>
</tr>
<tr>
<td># objects $(</td>
<td>O</td>
<td>)$</td>
</tr>
<tr>
<td># levels $(p)$</td>
<td>2, 4, 16</td>
<td>4</td>
</tr>
<tr>
<td># sources $(m)$</td>
<td>2, 4, 6</td>
<td>4 for CA 8 for others</td>
</tr>
<tr>
<td>Query</td>
<td>single-source kNN/range query</td>
<td>single-source kNN</td>
</tr>
<tr>
<td># NNs $(k)$</td>
<td>1, 10, 100, 1,000</td>
<td>10</td>
</tr>
<tr>
<td>Search range $(r)$</td>
<td>0.1 of net. diameter</td>
<td>0.1</td>
</tr>
</tbody>
</table>

TABLE 2: Evaluation parameters

5. CA, NA and SF are obtained from [20] and PRS is from [21].

Additional to ROAD, we implemented network expansion [7], Euclidean-based approach [7], [8], Distance Index [6] and Distance Browsing [13] (labeled as NetExp, Euclidean, DistIdx and DistBrws, respectively), all in GNU C++ for comparison. NetExp serves as the baseline approach in our evaluation. We adopt CCAM [22] to organize network nodes in disk storage for all the approaches. For NetExp, objects are stored with network nodes. For Euclidean, objects are indexed by an R-tree and A* algorithm [9] is used to determine objects’ network distances from query nodes. For DistIdx and DistBrws, distance signatures and shortest path quad-trees are stored with network nodes, respectively. For DistIdx, we adopt exact object distances in the distance signature to provide its optimal search performance.

Four performance metrics are measured in this evaluation. They are 1) index construction time: the time to construct an index; 2) index size: storage used to store an index; 3) query processing time: time duration from the time a query is initiated to the time a complete result is obtained; and 4) index update time: the time spent in maintaining the underlying indices when a update (either object update or network update) is experienced. All experiments were conducted upon Linux 2.6.9 servers with Intel Xeon 3.2GHz CPU and 4GB RAM. Unless stated explicitly, each experiment presented below evaluates one parameter while using the default values for other parameters.

8.1 Index Construction

The first experiment set evaluates the index construction time and index sizes for all the approaches with various number of objects and networks. Here, we use default $p$ and $l$ for ROAD and leave the evaluation of their impacts in the final set of experiments. Figure 13 shows the index construction time (in hours) and index sizes (in megabyte) for various number of objects on NA. Since the construction time is not affected by the object distribution, the experiment results are not presented here. In the figure, NetExp and Euclidean incur the smallest index construction times (in a few minutes) and index size (in a few MBs). ROAD takes around 1 hour construction time and about 20MB storage space. In contrast, due to the bulky shortest path quad-trees, DistBrws takes an extremely long construction time (over 100,000 hours) and a huge storage (over 10GB), though it is almost invariant to the number of objects. As for DistIdx, both the construction time and index size increase drastically as the number of objects evaluated increases. When 100,000 objects are experimented, DistIdx consumes 100GB storage size and takes more than 10,000 hours to build the index! This experiment result reveals that both DistBrws and DistIdx are impractical in real applications and the idea of query pre-computation and materialization of all-pair shortest paths and shortest paths towards objects is not appealing.

Figure 14 shows the index construction times and index sizes for different networks with the number of objects fixed at 10,000.
10,000 and the number of clusters fixed at 100, i.e., 100 objects per cluster. As shown in the figure, NetExp and Euclidean incur the shortest index construction times and smallest storage overhead. However, they both are not query efficient as will be evaluated next. On the other hand, DistIdx, DistBrws and ROAD incur different index construction time and index size as networks change but ROAD always outperforms the other two. For example, when the largest network PRS is evaluated, DistIdx takes over 1,000 hours to build the index and 10GB to store it; while DistBrws takes over a month to build the index and more than 15GB to store it. Differently, ROAD incurs significantly shorter construction time (less than 1 hour) and consumes less storage (about 18MB). Compared with DistIdx, ROAD only requires around 0.6% of its index construction time and 0.03% of its index size. In addition, the cost of DistIdx increases as the number of included objects increases. However, the index construction cost for ROAD is mainly attributed to the formation of Route Overlay, which is independent of the number of objects included.

Then, we evaluate the impact of object cardinalities and object distributions. With fewer objects and/or fewer clusters, more subspaces with no object of interest can be pruned so that ROAD can achieve a better performance. When we increase the number of objects from 100 up to 100,000 with the number of clusters fixed at 100, all the approaches (except Euclidean) have their search performance improved, as shown in Figure 15(b). This is because a larger object cardinality implies a higher density. Consequently, the average distance between query points and their k-th NN object becomes shorter which in turn cuts down the network traversal cost for kNN searches. ROAD consistently demonstrates the best performance. For example, it only requires 33% of NetExp’s processing time when 100,000 objects are evaluated. Besides, we evaluate the impact of objects distribution via varying the number of clusters from 10 up to 1,000 and examining the uniform distribution. Figure 15(c) plots the experiment results when 10,000 objects are evaluated. When objects are scattered in the network, the average distance from query points to objects is also shortened. As such, the performance of all the approaches is improved. When 10 clusters are experimented, ROAD takes only 1% processing time of NetExp.

Finally, we examine the impact of query parameter \( k \) (from 1 to 1,000) and the result is plotted in Figure 15(d). While all the approaches take more time when \( k \) is increased, ROAD consistently performs the best due to its strong pruning power. When \( k \) is 1, ROAD takes 1.7% processing time of NetExp.

8.2 Query Performance

The second set of experiments evaluate the search performance of ROAD and other approaches in answering single-source LDSQs and multi-source LDSQs on different (1) networks, (2) numbers of objects, (3) object distributions, (4) query parameters, and (5) the number of sources for multiple-source LDSQs. In the experiments, we generate 100 random queries and report the average query processing time.

8.2.1 Experiments on Single-source kNN Query

First, we evaluate single-source kNN queries. As depicted in Figure 15(a), when different networks are considered, Euclidean performs the worst because of exhaustive shortest path searches for a possibly large number of candidate objects. This is consistent with the observations made in [7]. Further, both DistIdx and DistBrws perform worse than NetExp and ROAD due to the accesses of bulky distance signatures and shortest path quad-trees and slow node-by-node network traversals. As expected, ROAD consistently performs the best. For clustered objects, ROAD can effectively bypass those Rnets with no object of interest. The improvement of ROAD over NetExp ranges from 1.6 (for CA) to 5.1 (for PRS).

8.2.2 Experiments on Single-source Range Query

Second, we examine the performance of different approaches for single-source range queries. As observations are very similar to those for kNN queries, we only report the performance over different networks and different object cardinalities for space saving, shown in Figure 16(a) and Figure 16(b) respectively. From the figures, we can see that ROAD consistently outperforms all the others and it benefits more from a larger network with a smaller number of objects. Again, Euclidean performs the worst as it has to examine a large number of candidate objects. Also, compared with NetExp, DistBrws and DistIdx do not improve the search performance as they both suffer from the massive access overhead for large networks and large numbers of objects.

8.2.3 Experiments on Multi-source kNN Query

Third, we study the performance of the various approaches for multi-source kNN queries. The results over different (1) networks, (2) numbers of objects, (3) object distributions, (4) query parameter \( k \) and (5) numbers of sources are shown in Figure 17. As there are no approaches on top of DistIdx and DistBrws presented in the literature can support multi-source LDSQs, we ignore them in the following experiments.
8.2.4 Experiments on Multi-source Range Query

Then, we evaluate the performance when multi-source range queries are issued. To save space, we focus on the impacts of networks and numbers of objects only with the number of sources fixed at two and the search range fixed at 0.1 of the network distance. The results are reported in Figure 18(a) and Figure 18(b) respectively. By pruning away those Rnets without objects of interest, ROAD outperforms the other approaches. When different networks are evaluated, ROAD, on average, takes only 4%-12% processing time of NetExp. When the number of objects changes, ROAD takes consistently 13% processing time of NetExp in NA with a fixed number of clusters (i.e., 100). This is because range queries request to explore all the nodes/edges within the search range, that is independent on the number of objects. As the search range is fixed, the search performance does not change even when the number of objects varies. Again, Euclidean performs the worst due to exhaustive candidate object distance searches.

8.3 Index Update

Further, we evaluate the index update cost upon object changes and/or network changes. First, we simulate object changes by removing 100 randomly-chosen objects from 10,000 installed objects and then inserting them back one by one. Each deletion and addition involves only one single object. We measure the time taken and report the average performance of deletions and insertions in Figure 19(a). As shown, the update cost incurred by DistIdx is several orders of magnitude higher than that of others, as DistIdx has to update the massive distance signatures. For NA, SF and PRS, it takes about 10 and 18 minutes to finish one object deletion and addition, respectively. In contrast, NetExp, Euclidean, DistBrws and ROAD can handle an update within 10 milliseconds for all the networks since they store objects separately from networks.

8.4 Evaluation on $p$ and $l$

Last but not least, we examine the impacts of factors $p$ and $l$ on the Rnet hierarchy formation, which in turn affects the performance of ROAD. In this experiment, we try different $(p,l)$ pairs with $p'$ fixed at 256 (i.e., 2$^8$, 4$^4$, and 16$^2$) for CA and 65536 (i.e., 2$^8$, 4$^4$, and 16$^2$) for NA, SF and PRS. The results in terms of query processing times for single-source $k$NN queries ($k=10$) and indexing overhead in terms of sources fixed at two and the search range fixed at 0.1 of the network distance are reported. The results in terms of query processing times for single-source $k$NN queries ($k=10$) and indexing overhead in terms of sources fixed at two and the search range fixed at 0.1 of the network distance are reported.
of index construction times and sizes are plotted in Figure 20. We can observe that ROAD performs similarly in terms of query processing times under different \((p, l)\) pairs. Meanwhile, a smaller \(l\) (with a corresponding larger \(p\)) results in a smaller index that takes a shorter construction time. This finding suggests the design of ROAD should adopt a smaller \(l\) and a larger \(p\), given a fixed number of finest Rnets targeted (i.e., \(p^l\)). Both observations are consistent with those made in our performance analysis discussed in the previous section.

(a) Query time (kNN)  
(b) Index overhead

Fig. 20: Combinations of \(p\) and \(l\)

From this evaluation, we can see the efficiency of ROAD to support single-source and multi-source LDSQs. It outperforms competitive approaches, namely, NetExp, Euclidean, DistIdx and DistBrws, owing to its effective search space pruning capability that is not explored by any of existing approaches. Meanwhile, ROAD provides moderate and very practical construction and maintenance cost compared with the state-of-the-art approaches, DistIdx and DistBrws.

9 CONCLUSION

The rapid growth of LBSs fosters a need of efficient search algorithms for LDSQs. In the mean time, the on-going trend of web-based LBSs demands a system framework that can be extended to accommodate diverse objects, provide efficient processing of various LDSQs, and support different distance metrics. To meet these needs, we propose ROAD, a new system framework for LDSQ processing, in this paper. The design of ROAD achieves a clear separation between objects and network for better system extensibility. It also exploits search space pruning, an effective and powerful technique for efficient object search. Upon the framework, efficient search algorithms for single-source and multi-source LDSQs are devised. Via a comprehensive performance evaluation on real road networks, ROAD is shown to significantly outperform the state-of-the-art techniques.

Recently, various LDSQs, such as continuous queries [4], skyline queries [23] and optimal location queries [24], were researched. However, existing works addressed them based on the solution-based approaches or extended spatial database approaches and thus suffered from the shortcomings of those approaches. In the future, we are going to extend our ROAD framework to support those emerged LDSQs.

REFERENCES

BIOGRAPHY

Ken C. K. Lee is currently an assistant professor at Department of Computer and Information Science, University of Massachusetts Dartmouth. In Fall 2009, he received his Ph.D. degree from the Pennsylvania State University. Besides, he obtained his BA and MPhil degrees from the Hong Kong Polytechnic University. He is now a member of the ACM and the IEEE.

Wang-Chien Lee is an Associate Professor of Computer Science and Engineering at Pennsylvania State University. He received his B.S. from the Information Science Department, National Chiao Tung University, Taiwan, his M.S. from the Computer Science Department, Indiana University, and his Ph.D. from the Computer and Information Science Department, the Ohio State University. Prior to joining Penn State, he was a principal member of the technical staff at Verizon/GTE Laboratories, Inc. Dr. Lee leads the Pervasive Data Access (PDA) Research Group at Penn State University to pursue cross-area research in database systems, pervasive/mobile computing, and networking.

Baihua Zheng received her B.S. degree from Zhejing University and her PhD in computer science from Hong Kong University of Science and Technology. She is a member of the IEEE and the ACM. Currently, she is an assistant professor in the School of Information Systems at Singapore Management University. Her research interests include mobile and pervasive computing, and spatial databases.

Yuan Tian received her BE degree in electrical engineering from Tsinghua University, China. She is currently working towards the PhD at the Department of Computer Science and Engineering, the Pennsylvania State University. Her research interests include spatial database, location based services and social network.